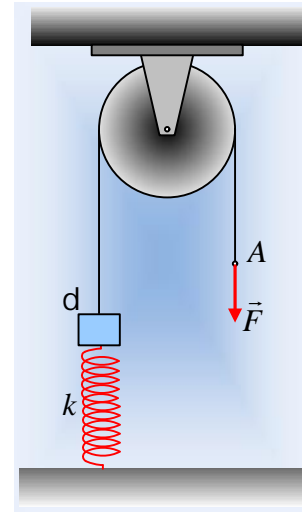


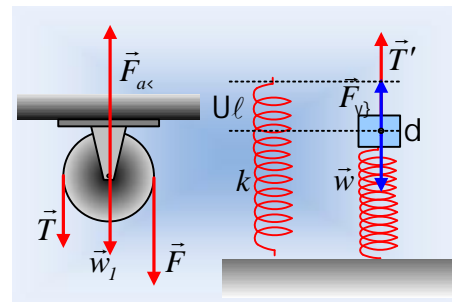
Μια μεταβλητή δύναμη επιταχύνει ένα σύστημα.

$m=2\text{kg}$
 $k=200 \text{ /m.}$
 $F = 32 - 40y$
 $=4\text{kg}$
 $y_1=0,1\text{m.}$
 $R=0,2\text{m}$
 $g=10\text{m/s}^2$



- i)
- ii)
- iii)
- iv)

U_{ℓ_0}
 $F=0 \quad F = w \quad kU_{\ell_0} = mg$
 $U_{\ell_0} = \frac{mg}{k} = \frac{2 \cdot 10}{200} \text{m} = 0,1\text{m}$



$$\mu : F = m \cdot a + (kU\ell - mg) = ma \quad (1)$$

$$: = \cdot F \cdot R - \cdot R = \frac{1}{2} R^2 \cdot F = \frac{1}{2} R \cdot \quad (2)$$

$$\mu \quad , \quad \mu \quad -$$

$$\mu \quad \mu \quad , \quad = R \quad -$$

$$\mu = \mu \quad (2) \quad \mu$$

(1), μ :

$$F = ma + \frac{1}{2}Ma \rightarrow a = \frac{F}{m + \frac{1}{2}M} = \frac{32}{2+2} m/s^2 = 8m/s^2.$$

ii) μ t₁ μ 0,1m, μ

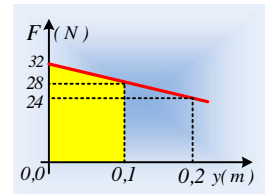
0,1m

μ . μ μ μ μ F

μ μ μ μ μ , μ

, μ , μ 0,1m, -

μ μ μ μ μ μ , y=0,1m, F₁=28 .



$$W_F = \frac{32+28}{2} \cdot 0,1 J = 3 J$$

iii) μ μ μ μ , μ , μ

μ t₁:

$$\mu : K_{d2} - K_{d1} = W_w + W_{FV} + W_{T'} \rightarrow$$

$$\frac{1}{2}m\hat{v}_1^2 - 0 = -mgy_1 + \left(\frac{1}{2}k(U\ell)^2 - 0 \right) + W_{T'} \quad (3)$$

$$: K_{\uparrow 2} - K_{\uparrow 1} = W_{w1} + W_{Fak} + W_T + W_F \rightarrow$$

$$\frac{1}{2}I\check{S}_1^2 = 0 = 0 + 0 + W_T + W_F \quad (4)$$

$$i = 1R, \quad W = -W \quad \mu \quad (3) \quad (4) \quad \mu :$$

$$\frac{1}{2}m\hat{v}_1^2 + \frac{1}{2}MR^2 \cdot \check{S}_1^2 = -mgy_1 + \frac{1}{2}k(U\ell)^2 + W_F$$

$$\left(m + \frac{1}{2}M \right) \hat{v}_1^2 = 2W_F + k(U\ell)^2 - 2mgy_1$$

$$\hat{v}_1 = \sqrt{\frac{2W_F + k(U\ell)^2 - 2mgy_1}{\left(m + \frac{1}{2}M \right)}} = \sqrt{\frac{2 \cdot 3 + 200 \cdot 0,1^2 - 2 \cdot 2 \cdot 10 \cdot 0,1}{2 + \frac{1}{2} \cdot 4}} m/s = 1m/s.$$

(1) (2) μ :

$$F - mg = ma_1 + \frac{1}{2}Ma_1 \rightarrow a_1 = \frac{F - mg}{m + \frac{1}{2}M} = \frac{28 - 20}{2 + 2} m/s^2 = 2m/s^2.$$

) μ :

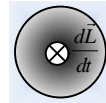
$$K_1 = \frac{1}{2} m \dot{\varphi}^2 = \frac{1}{2} \cdot 2 \cdot 1^2 J = 1J.$$

$$K_{\dot{\varphi}} = \frac{1}{2} I \dot{\varphi}^2 = \frac{1}{2} \cdot \frac{1}{2} MR^2 \dot{\varphi}^2 = \frac{1}{4} M \dot{\varphi}^2 = \frac{1}{4} \cdot 4 \cdot 1^2 J = 1J$$

$$\frac{dK_1}{dt} = (dF) \cdot \dot{\varphi} = ma \cdot \dot{\varphi} = 2 \cdot 2 \cdot 1J/s = 4J/s$$

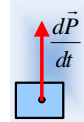
$$\frac{dK_{\dot{\varphi}}}{dt} = (d\dot{\varphi}) \cdot \dot{\varphi} = I a_{xS\epsilon} \cdot \dot{\varphi} = \frac{1}{2} MR a_{xS\epsilon} \cdot R \dot{\varphi} = \frac{1}{2} M a \cdot \dot{\varphi} = \frac{1}{2} \cdot 4 \cdot 2 \cdot 1J/s = 4J/s$$

) μ μ , μ



$$\frac{dL_{\dot{\varphi}}}{dt} = d\dot{\varphi} = l \cdot r_{xS\epsilon} = \frac{1}{2} MR^2 a_{xS\epsilon} = \frac{1}{2} MRa$$

$$\frac{dL_{\dot{\varphi}}}{dt} = \frac{1}{2} MRa = \frac{1}{2} \cdot 4 \cdot 0,2 \cdot 2kgm^2/s^2 = 0,8kgm^2/s^2.$$



(μ μ) μ :

$$\frac{dP}{dt} = dF = ma = 2 \cdot 2kgm/s^2 = 4kgm/s^2.$$

iv) μ μ 0,2m, μ μ

μ μ 0,2m, μ

$$U\ell_1 = 0, Im = U\ell_0.$$

μ μ 0,2m, y=0,2m, F₂=24 , :

$$W_{F_2} = \frac{32 + 24}{2} 0,2J = 5,6J$$

ii) μ μ μ :

$$\mu : K_{d2} - K_{d1} = W_w + W_{FV} + W_{T'} \rightarrow$$

$$\frac{1}{2} m \dot{\varphi}_2^2 - 0 = -mgy_2 + \left(\frac{1}{2} k(U\ell_0)^2 - \frac{1}{2} k(U\ell_1)^2 \right) + W_{T'} \quad (3)$$

$$: K_{\dot{\varphi}_2} - K_{\dot{\varphi}_1} = W_{w1} + W_{Fa\alpha} + W_T + W_{F_2} \rightarrow$$

$$\frac{1}{2} I \dot{\varphi}_2^2 = 0 = 0 + 0 + W_T + W_{F_2} \quad (4)$$

i= 1R, W = -W μ (3) (4) μ :

$$\frac{1}{2} m \dot{\varphi}_2^2 + \frac{1}{2} MR^2 \cdot \dot{\varphi}_2^2 = -mgy_2 + W_{F_2}$$

$$\left(m + \frac{I}{2}M\right) \dot{y}_2^2 = 2W_{F2} - 2mgy_2$$

$$\dot{y}_2^2 = \frac{2W_{F2} - 2mgy_2}{m + \frac{I}{2}M} = \frac{2 \cdot 5,6 - 2 \cdot 2 \cdot 10 \cdot 0,2}{2 + 2} m^2 / s^2 = 0,8 m^2 / s^2$$

μ , μ , μ , μ :
y₂

$$E_{\ddagger} = \frac{I}{2}ky_2^2 + \frac{I}{2}m\dot{y}_2^2 = \frac{I}{2}200 \cdot 0,2^2 J + \frac{I}{2}2 \cdot 0,8 J = 4,8 J$$

μ
μ 4,8J.

:

1) μ μ - , μ μ μ
μ F μ . μ iii) μ μ -
μ μ (. . .) :
μ : W_F=3J W_F = 1/2 k·(l)²= 1/2 200·0,1²J=1J

U=mgy₁=2J = 1/2 m v₁² + 1/2 I ω₁².
μ μ , μ
μ :

$$\frac{I}{2}m\dot{y}_1^2 + \frac{I}{2}I \cdot \dot{\theta}_1^2 + mgy_1 = \frac{I}{2}k(U\ell)^2 + W_F \dots$$

2) μ μ , μ μ μ
μ iii) μ , μ μ μ -
μ :

$$\frac{dL_{\ddagger}}{dt} = d\ddagger = F \cdot R - T \cdot R \dots$$

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