

MENGAPA BILANGAN EULER $e = 2,718281 \dots$?

$$\left. \begin{aligned} f(x) &= e^x \rightarrow f(0) = e^0 = 1 \\ f'(x) &= e^x \rightarrow f'(0) = e^0 = 1 \\ f''(x) &= e^x \rightarrow f''(0) = e^0 = 1 \\ f'''(x) &= e^x \rightarrow f'''(0) = e^0 = 1 \\ f^{(4)}(x) &= e^x \rightarrow f^{(4)}(0) = e^0 = 1 \\ f^{(5)}(x) &= e^x \rightarrow f^{(5)}(0) = e^0 = 1 \end{aligned} \right\} f^{(n)}(x) = e^x \rightarrow f^{(n)}(0) = e^0 = 1$$

DERET MAC LAURIN

$$f(x) = f(0) + \frac{f'(0)}{1!}x + \frac{f''(0)}{2!}x^2 + \frac{f'''(0)}{3!}x^3 + \frac{f^{(4)}(0)}{4!}x^4 + \frac{f^{(5)}(0)}{5!}x^5 + \frac{f^{(6)}(0)}{6!}x^6 + \frac{f^{(7)}(0)}{7!}x^7 + \frac{f^{(8)}(0)}{8!}x^8 + \frac{f^{(9)}(0)}{9!}x^9 + \dots$$

$$e^x = 1 + \frac{1}{1!}x + \frac{1}{2!}x^2 + \frac{1}{3!}x^3 + \frac{1}{4!}x^4 + \frac{1}{5!}x^5 + \frac{1}{6!}x^6 + \frac{1}{7!}x^7 + \frac{1}{8!}x^8 + \frac{1}{9!}x^9 + \dots$$

$$e^x = 1 + \frac{x}{1!} + \frac{x^2}{2!} + \frac{x^3}{3!} + \frac{x^4}{4!} + \frac{x^5}{5!} + \frac{x^6}{6!} + \frac{x^7}{7!} + \frac{x^8}{8!} + \frac{x^9}{9!} + \dots$$

UNTUK $|x|=1$

$$\rightarrow e = 1 + \frac{1}{1} + \frac{1^2}{2 \cdot 1} + \frac{1^3}{3 \cdot 2 \cdot 1} + \frac{1^4}{4 \cdot 3 \cdot 2 \cdot 1} + \frac{1^5}{5 \cdot 4 \cdot 3 \cdot 2 \cdot 1} + \frac{1^6}{6 \cdot 5 \cdot 3 \cdot 2 \cdot 1} + \frac{1^7}{7 \cdot 6 \cdot 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1} + \frac{1^8}{8 \cdot 7 \cdot 6 \cdot 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1} + \frac{1^9}{9 \cdot 8 \cdot 7 \cdot 6 \cdot 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1} + \dots$$

$$e = 1 + 1 + \frac{1}{2} + \frac{1}{6} + \frac{1}{24} + \frac{1}{120} + \frac{1}{720} + \frac{1}{5040} + \frac{1}{40320} + \frac{1}{362880} + \dots$$

$$e = 2 + 0.5 + 0.166666667 + 0.041666667 + 0.008333333 + 0.001388889 + 0.000198413 + 2.48016 \text{ E-05} + 2.75573 \text{ E-06} + \dots$$

$$e = 2.718281526 \dots$$

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