## Study of Tangent Handrail Geometry

## Unequal Slopes, Rectangular Footprint ( $90^{\circ}$ Corner Angle)

Development of Hexahedral Prismatic Solid
(or Post Type Model) ... Page 2
Superposition of Prismatic Solid (or Post Type Model)
and Trirectangular Tetrahedron
... Page 3
Construction of the Dihedral Angles
... Page 4
Superposition of Level Plane and Oblique Plane and Construction of the Ellipse
... Page 5

## Supplementary: Images of Prismatic Solids Comparison of Tetrahedral and Post Type Models

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| Images of Tetrahedral and Post Type Models | ... | Page 7 |




Superposition of Level Plane and Oblique Plane: Unequal Slopes, $90^{\circ}$ Corner Angle. Hip Run $=10$, Hip Length $=11.08321$ Unless otherwise noted, the centroid of the ellipse is the origin
Semi - minor Axis $=$ Radius $=5.73462$ Semi-major $A x i s=6.35580$ Foci: $F 1=(0,2.74049), F 2=(0,-2.74049)$ External Point: $P=(-7.98658,1.56206)$ Points of Tangency: $T 1=(-3.28859,5.20688)$ $T 2=(-4.69799,-3.64481)$
From circle center...
$T 2=(-4.69799,-3.28859)$


# Table of Angles used in Developments and Construction of Models 

## 10/12 Side

$\mathbf{S S}=39.80557^{\circ}$
DD $=34.99202^{\circ}$
$\mathbf{R 1}=25.54245^{\circ}$
$\mathbf{R 4 B} \mathbf{m}=32.27594^{\circ}$
R4Pm $=52.19482^{\circ}$
R5Bm $=21.38029^{\circ}$
R5Pm $=15.32559^{\circ}$
A5Bm $=14.31575^{\circ}$
A5Pm $=20.68538^{\circ}$

## 7/12 Side

$\mathbf{S}=30.25644^{\circ}$
$\mathbf{D}=55.00798^{\circ}$
$\mathbf{R 1}=25.54245^{\circ}$
$\mathbf{R 4 B a}=52.19482^{\circ}$
$\mathbf{R 4 P a}=32.27594^{\circ}$
R5Ba $=15.32559^{\circ}$
R5Pa $=21.38029^{\circ}$
$\mathbf{A 5 B a}=20.68538^{\circ}$
$\mathbf{A 5 P a}=14.31575^{\circ}$

Main Slope $=10 / 12$ Adjoining Slope $=7 / 12$

$$
\text { Corner Angle }=90^{\circ}
$$

Development of Hip Rafter Side Cut and Compound Angle at Hip Rafter Peak or Valley Rafter Foot

Developments of
Main (10/12) Side Angles


Development of Hip Rafter Side Cut and Compound Angle at Hip Rafter Foot or Valley Rafter Peak



$$
\begin{aligned}
& \text { shbstz } 8 L 6 L 8 \\
& \text { is } \\
& \text { \& } 8 \text { dhe }
\end{aligned}
$$

