

**1993 Paper II Question 8**

Let  $f(x) = \sqrt[3]{x^2 - x^3}$ .

- a. Find  $f'(x)$  and  $f''(x)$ . (2 marks)
- b. Show that both  $f'(0)$  and  $f'(1)$  do not exist. (2 marks)
- c. Determine the sets of values of  $x$  such that:
  - (i)  $f'(x) = 0$ ,
  - (ii)  $f'(x) > 0$ ,
  - (iii)  $f'(x) < 0$ ,
  - (iv)  $f''(x) = 0$ ,
  - (v)  $f''(x) > 0$ ,
  - (vi)  $f''(x) < 0$ .(3 marks)
- d. Find the relative extremum point(s) and the point(s) of inflexion on the curve  $y = f(x)$ . (3 marks)
- e. Find the asymptote(s) of the curve  $y = f(x)$ . (3 marks)
- f. Sketch the curve  $y = f(x)$ . (2 marks)