

1. Assuming the horizontal velocity of the ball is constant, the horizontal displacement is

$$\Delta x = v \Delta t$$

where  $\Delta x$  is the horizontal distance traveled,  $\Delta t$  is the time, and  $v$  is the (horizontal) velocity. Converting  $v$  to meters per second, we have  $160 \text{ km/h} = 44.4 \text{ m/s}$ . Thus

$$\Delta t = \frac{\Delta x}{v} = \frac{18.4 \text{ m}}{44.4 \text{ m/s}} = 0.414 \text{ s}.$$

The velocity-unit conversion implemented above can be figured “from basics” ( $1000 \text{ m} = 1 \text{ km}$ ,  $3600 \text{ s} = 1 \text{ h}$ ) or found in Appendix D.

4. If the plane (with velocity  $v$ ) maintains its present course, and if the terrain continues its upward slope of  $4.3^\circ$ , then the plane will strike the ground after traveling

$$\Delta x = \frac{h}{\tan \theta} = \frac{35 \text{ m}}{\tan 4.3^\circ} = 465.5 \text{ m} \approx 0.465 \text{ km}.$$

This corresponds to a time of flight found from Eq. 2-2 (with  $v = v_{\text{avg}}$  since it is constant)

$$t = \frac{\Delta x}{v} = \frac{0.465 \text{ km}}{1300 \text{ km/h}} = 0.000358 \text{ h} \approx 1.3 \text{ s}.$$

This, then, estimates the time available to the pilot to make his correction.

5. (a) Denoting the travel time and distance from San Antonio to Houston as  $T$  and  $D$ , respectively, the average speed is

$$s_{\text{avg } 1} = \frac{D}{T} = \frac{(55 \text{ km/h})\frac{T}{2} + (90 \text{ km/h})\frac{T}{2}}{T} = 72.5 \text{ km/h}$$

which should be rounded to  $73 \text{ km/h}$ .

- (b) Using the fact that time = distance/speed while the speed is constant, we find

$$s_{\text{avg } 2} = \frac{D}{T} = \frac{D}{\frac{D/2}{55 \text{ km/h}} + \frac{D/2}{90 \text{ km/h}}} = 68.3 \text{ km/h}$$

which should be rounded to  $68 \text{ km/h}$ .

- (c) The total distance traveled ( $2D$ ) must not be confused with the net displacement (zero). We obtain for the two-way trip

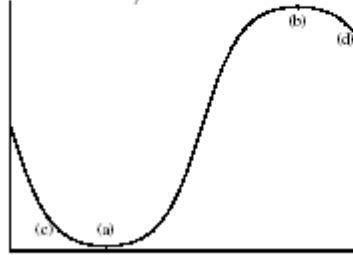
$$s_{\text{avg}} = \frac{2D}{\frac{D}{72.5 \text{ km/h}} + \frac{D}{68.3 \text{ km/h}}} = 70 \text{ km/h}.$$

- (d) Since the net displacement vanishes, the average velocity for the trip in its entirety is zero.
- (e) In asking for a *sketch*, the problem is allowing the student to arbitrarily set the distance  $D$  (the intent is *not* to make the student go to an Atlas to look it up); the student can just as easily arbitrarily set  $T$  instead of  $D$ , as will be clear in the following discussion. In the interest of saving space, we briefly describe the graph (with kilometers-per-hour understood for the slopes): two contiguous line segments, the first having a slope of 55 and connecting the origin to  $(t_1, x_1) = (T/2, 55T/2)$  and the second having a slope of 90 and connecting  $(t_1, x_1)$  to  $(T, D)$  where  $D = (55 + 90)T/2$ . The average velocity, from the graphical point of view, is the slope of a line drawn from the origin to  $(T, D)$ .

10. The velocity (both magnitude and sign) is determined by the slope of the  $x$  versus  $t$  curve, in accordance with Eq. 2-4.

- (a) The armadillo is to the left of the coordinate origin on the axis between  $t = 2.0$  s and  $t = 4.0$  s.
- (b) The velocity is negative between  $t = 0$  and  $t = 3.0$  s.
- (c) The velocity is positive between  $t = 3.0$  s and  $t = 7.0$  s.
- (d) The velocity is zero at the graph minimum (at  $t = 3.0$  s).

14. From Eq. 2-4 and Eq. 2-9, we note that the sign of the velocity is the sign of the slope in an  $x$ -vs- $t$  plot, and the sign of the acceleration corresponds to whether such a curve is concave up or concave down. In the interest of saving space, we indicate sample points for parts (a)-(d) in a single figure; this means that all points are not at  $t = 1$  s (which we feel is an acceptable modification of the problem – since the datum  $t = 1$  s is not used).



Any change from zero to non-zero values of  $\vec{v}$  represents increasing  $|\vec{v}|$  (speed). Also,  $\vec{v} \parallel \vec{a}$  implies that the particle is going faster. Thus, points (a), (b) and (d) involve increasing speed.

23. The constant-acceleration condition permits the use of Table 2-1.

- (a) Setting  $v = 0$  and  $x_0 = 0$  in  $v^2 = v_0^2 + 2a(x - x_0)$ , we find

$$x = -\frac{1}{2} \frac{v_0^2}{a} = -\frac{1}{2} \left( \frac{5.00 \times 10^6}{-1.25 \times 10^{14}} \right) = 0.100 \text{ m} .$$

Since the muon is slowing, the initial velocity and the acceleration must have opposite signs.

- (b) Below are the time-plots of the position  $x$  and velocity  $v$  of the muon from the moment it enters the field to the time it stops. The computation in part (a) made no reference to  $t$ , so that other equations from Table 2-1 (such as  $v = v_0 + at$  and  $x = v_0t + \frac{1}{2}at^2$ ) are used in making these plots.

