

Secondary 4 Mathematics 2nd Term Pre-exam

Time allowed: 1 hour 20 minutes

Total Mark: 66

Instructions:

1. This paper consists of 3 sections, A(1), A(2) and B. Each section carries 22 marks.
2. Attempt ALL questions. Write your answers in the spaces provided in this Question/Answer paper.
3. Unless otherwise specified, all workings must be clearly shown.
4. Unless otherwise specified, numerical answers must either be exact or correct to 3 significant figures.
5. The diagrams in this paper are not necessarily drawn to scale.

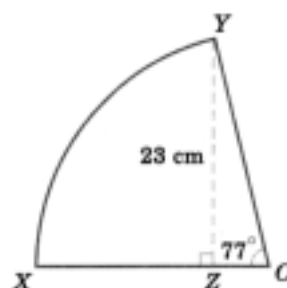
SECTION A(1) (22 marks)

1. Solve the equation $4 \cos 3\theta = 1$ where $0^\circ < \theta < 30^\circ$.

(3 marks)

2. Find the perimeter of the sector OXY as shown.

(3 marks)

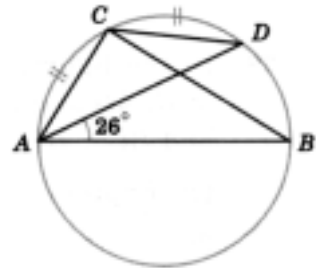


3. The 12th term of an arithmetic sequence is twice the 3rd term. The sum of first 3 terms is 24. Find the first term of the arithmetic sequence.

(4 marks)

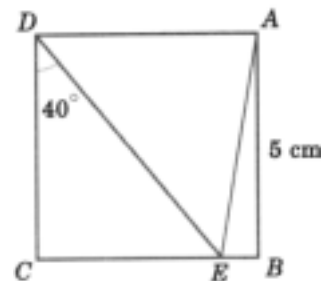
4. In the figure, AB is a diameter of the circle. If $\widehat{CA} = \widehat{CD}$ and $\angle DAB = 26^\circ$, find $\angle ADC$.

(4 marks)



5. In the figure, ABCD is a square of side 5 cm and $\angle EDC = 40^\circ$. Find the length of AE correct to 3 significant figures.

(4 marks)

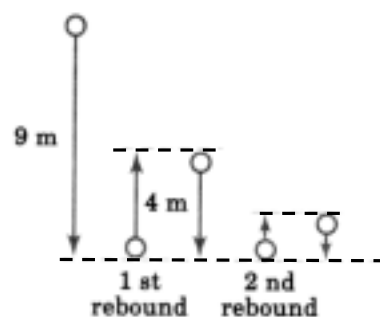


6. Solve the quadratic inequality $x(x-1) \leq x(2x+1)$ and represent the solution on the number line.

(4 marks)

SECTION A(2) (22 marks)

7. A ball falls from a height of 9 m and rebounds to a height of 4 m. The ball continues to fall and rebound such that each time the height of the rebound is $\frac{4}{9}$ of the height from which it previously fell.



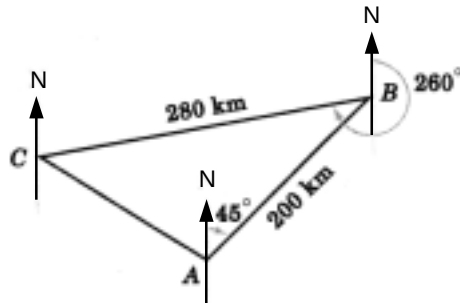
- (a) How high does the ball reach after the fifth rebound?

(3 marks)

- (b) What is the total distance travelled by the ball before it comes to rest?

(3 marks)

9. In the figure, a ship sails 200 km from point A on a true bearing 045° to point B. From B, it sails 280 km on a true bearing 260° to point C.



- (a) Find $\angle CBA$.

(2 marks)

- (b) Find the distance AC, correct to the nearest km,

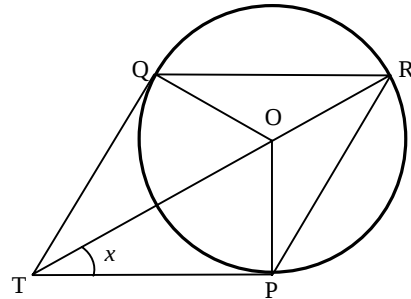
(2 marks)

- (c) Find the true bearing of A from C, correct to the nearest degree.

(4 marks)

SECTION B (22 marks)

10. In the figure, TP and TQ are tangents drawn from the point T to a circle with centre O and radius 1 unit. TO is produced to cut the circle at R.



- (a) Given that $\angle PTO = x$, write down expressions, in terms of x , for
- (i) $\angle TOP$;
 - (ii) $\angle QOP$;
 - (iii) $\angle QRP$.

(6 marks)

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10. (b) Given that TPRQ is a parallelogram.

(i) Find the value of x .

(ii) Find the length of TR.

(5 marks)

11. An association plans to build a hostel with x single rooms and y double rooms satisfying the following conditions

(I) The hostel will accommodate at least 48 persons.

(II) Each single room will occupy an area of 10 m^2 , each double room will occupy an area of 15 m^2 and the total available floor area for the rooms is 450 m^2 .

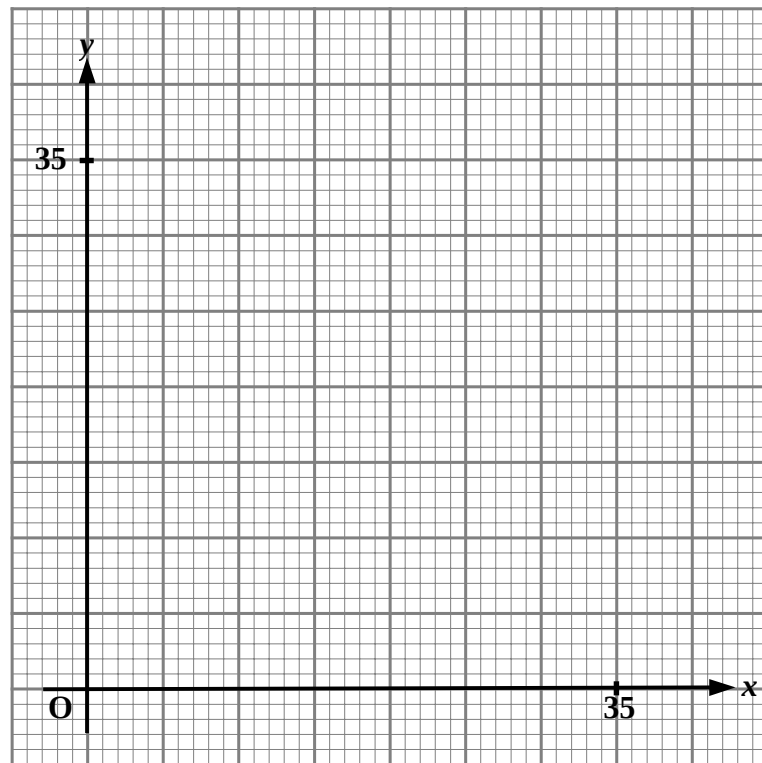
(III) The number of double rooms should not exceed the number of single rooms.

(a) (i) Write down the inequalities in x and y to represent the above constraints.

(ii) Hence, draw and shade the region that satisfies the inequalities.

(7 marks)

11. (a) (ii)



- (b) If the profits on a single room and a double room are \$3000 and \$4000 per month respectively, find the values of x and y so that the total profit will be a maximum.

(4 marks)

END OF PAPER