

## S.4 Add Maths Quiz 1

(Quadratic Equations)

Time allowed: 30 minutes

Total Mark: 30

Unless otherwise stated in the question, numerical answers must be given in exact value.

1. If the quadratic equation  $(mx)^2 + 2mx + x^2 + 2ax + a^2 + 1 = 0$  has equal roots,
  - (a) show that  $ma = 1$ ,
  - (b) find the double root in terms of  $m$ .

(3 + 3 marks)
  
2. Let  $f(x) = 4x^2 - 7x - k$ .
  - (a) Find the range of values of  $k$  for which  $f(x) > 2$  for all values of  $x$ .
  - (b) Using the method of completing the square, show that  $f(x)$  attains its minimum value when  $x = \frac{7}{8}$  for all values of  $k$ .

(3 + 1 marks)
  
3. Find the values of  $k$  so that the roots of the equation  $(x - k)^2 - 4(x - 3k - 7) + 8 = 0$  are reciprocals of each other. For the larger value of  $k$ , solve the corresponding equation.

(6 marks)
  
4. Solve the equation  $(x - 1)^2 + |x - 1| - 2 = 0$ .

(4 marks)
  
5. If  $\alpha^2$  and  $\beta^2$  are the roots of the equation  $x^2 - 30x + 9 = 0$ , find the equation(s) in  $x$  whose roots are  $\frac{1}{\alpha}$  and  $\frac{1}{\beta}$ .

(10 marks)

**End of Quiz**