

SOLUTIONS TO SELECTED EXERCISES

EXERCISES FOR SECTION 2.1

PART I

1. Given the form p . Case (a): Let p be the statement 'Salt Lake City is in Utah'. Then p is true. Case (b): Let p be the statement 'Salt Lake City is in Nevada'. Then p is false.
2. Given the form *It's not the case that p* . Case (a): Let *It's not the case that p* be the statement 'It's not the case that Salt Lake City is in Nevada'. Then *It's not the case that p* is true. Case (b): Let *It's not the case that p* be the statement 'It's not the case that Salt Lake City is in Utah'. Then *It's not the case that p* is false.
4. Given the form p or q . Case (a): Let p or q be the statement 'Tim is a philosopher or he's an electrician'. Then p or q is true. Case (b): Let p or q be the statement 'Tim is a sociologist or he's a taxidermist'. Then p or q is false.
5. Given the form p if and only if q . Case (a): Let p if and only if q be the statement 'Sheila is a bachelor if and only if she's an unmarried male'. Then p if and only if q is true. Case (b): Let p if and only if q be the statement 'Sheila is a bachelor if and only if she's a married male'. Then p if and only if q is false.
6. Given the form *If p , then it's not the case that q* . Case (a): Let *If p , then it's not the case that q* be the statement 'If Sheila is a bachelor, then it's not the case that she's married'. Then *If p , then it's not the case that q* is true. Case (b): Let *If p , then it's not the case that q* be the statement 'If Sheila is a bachelor, then it's not the case that she's unmarried'. Then *If p , then it's not the case that q* is false.
7. Given the form *Either not p or not q* . Case (a): Let *Either not p or not q* be the statement 'Either Tim is not a philosopher or he's not an electrician'. Then *Either not p or not q* is true. Case (b): Let *Either not p or not q* be the statement 'Tim is not a philosopher or he's not a teacher'. Then *Either not p or not q* is false.
8. Given the form *If it's not the case that p , then q* . Case (a): Let *If it's not the case that p , then q* be the statement 'If Stan's not married, then he's a bachelor'. Then *If it's not the case that p , then q* is true. Case (b): Let *If it's not the case that p , then q* be the statement 'If Stan's not married, then he's a husband'. Then *If it's not the case that p , then q* is false.
10. Given the form *If p , then q and not r* . Case (a): Let *If p , then q and not r* be the statement 'If Stan is a bachelor, then he's male and he's not married'. Then *If p , then q and not r* is true. Case (b): Let *If p , then q and not r* be the statement 'If Stan is a bachelor, then he's married and he's not male'. Then *If p , then q and not r* is false.

PART II

11. $p \rightarrow q$

$$\begin{array}{l} p \\ \setminus q \end{array}$$

12. $p \rightarrow q$

$$\begin{array}{l} q \\ \setminus p \end{array}$$

13. Either it's raining or it's raining.

\ It's raining.

EXERCISES FOR SECTION 2.2

1. Truth-functionally simple.

2. Truth-functionally compound. The simple statements are 'Melody teaches Marxism' and 'Melody is happy'.

4. Truth-functionally simple.

5. Truth-functionally compound. The simple statements are 'Betty will get up early' and 'Circumstances are extreme'.

6. Truth-functionally compound. The simple statements are 'There is nobody in the shower' and 'The water is on'.

7. Truth-functionally compound. The simple statement is 'The television is working'.

8. Truth-functionally compound. The simple statements are 'The television is working' and 'The radio is working'.

10. Truth-functionally simple.

11. Truth-functionally simple.

12. Truth-functionally simple.

14. Truth-functionally compound. The simple statement is 'I have been involved in wrongdoing'.

15. Truth-functionally simple.

16. Truth-functionally compound. The simple statements are 'The man walked up to the stand' and 'The man ordered an ice cream cone'.
17. Truth-functionally simple.
18. Truth-functionally simple.
20. Truth-functionally compound. The simple statement is 'Ellen is known to avoid a good book on transformational grammar'.
21. Truth-functionally simple. (See p. 41 of the textbook.)
22. Truth-functionally compound. The simple statement is 'Jack's father is unhappy'.
23. Truth-functionally simple.
24. Truth-functionally simple.
25. Truth-functionally compound. The simple statements are 'The fire started because a match was lit' and 'The fire was soon put out'.
26. Truth-functionally simple.
27. Truth-functionally simple.

EXERCISES FOR SECTION 2.3

1. M: I went to the Moon yesterday. $\sim M$
2. M: I went to the Moon yesterday. $\sim M$
4. B: I have eaten the last banana. $\sim B$
5. T: It is possible to travel backward in time. $\sim T$
6. S: Socrates' argument is valid. $\sim S$
7. C: There is a computable utility function. $\sim C$
8. I: Inkyo will wear socks. $\sim I$
10. B: Betty is macabre; O: Bob is macabre. (**B & O**)
11. B: Betty is macabre; O: Bob is macabre. (**B & O**)

12. S: Tom is six foot two; E: Tom has eyes of blue. (**S & E**)
13. S: Smoking is permitted; N: No one is smoking. (**S & N**)
14. F: We have free will; G: God knows everything we're doing. (**F & G**)
15. W: Women have studied logic; M: Men have studied logic. (**W & M**)
16. F: The first little piggy had roast beef; S: The second little piggy had none.
(**F & S**)
17. C: The cat is away; M: The mice are away. (**C ∨ M**)
18. Y: Sylvia will show up at the party; A: Sally will show up at the party. (**Y ∨ A**)
20. M: You have won a million dollars; F: You have won a faux diamond necklace.
(**M ∨ F**)
21. C: My cat ate my shoes; D: My dog ate my shoes. (**C ∨ D**)
22. S: Smoking is allowed; L: I am leaving. (**S → L**)
23. C: Creationism is a good theory; N: All good theories are naively falsifiable.
(**C → N**)
24. M: Bernice has music; E: Bernice really enjoys life. (**E → M**)
26. U: Ratso understands Maxwell's equations for electromagnetism; S: Ratso can solve the equation. (**U → S**)
27. A: Annie will solve the problem before Ratso; R: Ratso tries to use linear regression analysis. (**R → A**)
28. M: Miracles exist; O: Omnipotent Olivia has the power to change the laws of physics. (**O → M**)
29. L: Lovely promises undying passion; C: Candice will reconsider the proposal of marriage. (**C → L**)
30. L: Lovely promises undying passion; C: Candice reconsiders the proposal of marriage. (**L ↔ C**)
32. T: Tachyons exist; F: There are faster-than-light particles. (**(T & F) ∨ (~T & ~F)**
-or- (**T ↔ F**)

33. R: I will allow you to read the comics; G: You give me the front page. $(R \leftrightarrow G)$

EXERCISES FOR SECTION 2.4

PART I

2. L: Luc will stay at the party; A: Andy will stay at the party. $(L \vee A) \& \sim(L \& A)$

3. L: Luc will stay at the party; A: Andy will stay at the party; S: Sam will stay at the party. $[(L \& A) \vee (L \& S) \vee (A \& S)] \& \sim[L \& (A \& S)]$

4. S: Some laws of physics are deterministic; A: All laws of physics are deterministic. $S \& \sim A$

6. S: Special relativity is generally thought to be compatible with complete physical determinism; Q: Quantum mechanics is generally thought to be compatible with complete physical determinism. $S \& \sim Q$

7. W: Light is a wave phenomenon; P: Light is a particle phenomenon. $\sim(W \& P)$

8. E: Some existentialists are theists; S: Sartre was a theist; F: Sartre believed that faith plays a fundamental role in all our beliefs. $[(E \& \sim S) \& F]$

9. P: Heidegger's *Sein und Zeit* was possible; R: Heidegger had read the works of Husserl; U: Heidegger had understood the works of Husserl. $P \rightarrow (R \& U)$

10. S: A person's hidden motives are often revealed by slips of the tongue; R: We have good reason to try to interpret slips of the tongue. $S \& (S \rightarrow R)$

12. D: Larson deals with his hurt feelings; S: Larson completely suppresses his hurt feelings; F: Larson will be able to function. $(\sim D \& \sim S) \rightarrow \sim F$ *or* $\sim(D \vee S) \rightarrow \sim F$

13. M: I am mistaken; C: You have a large, multilegged creature crawling on your shoulder. $\sim M \rightarrow C$

14. K: Kate wins a karate title; W: Williams wins a karate title; C: Kelly competes this summer; T: Kelly will have a tough pair of challengers to face.
 $(K \& W) \rightarrow (C \rightarrow T)$

16. W: War will occur; N: There are nuclear weapons. $\sim(W \leftrightarrow N)$

17. P: World peace will be achieved; E: Every country has equal power; R: Russia has nuclear missiles; C: China has nuclear missiles. $(P \rightarrow E) \rightarrow [(R \& \sim C) \rightarrow \sim P]$

PART II

18. E: Sam is still full of energy; T: Luc is tired; G: Sam can have a good time.

E & T
T → **~G**
\
~G

20. C: Coke is a carbonated drink; P: Pepsi is a carbonated drink; M: Carbonated drinks upset Martin's stomach; U: Martin's stomach will be upset; O: Martin drinks Coke; E: Martin drinks Pepsi.

C & P
M
\
(O ∨ E) → U

21. O: Martin drinks Coke; E: Martin drinks Pepsi; A: Martin falls asleep; B: Martin burps a lot; D: Maurice is disgusted.

[(O & E) → A] & [(O ∨ E) & ~(O & E)] → B
B → D
\
[D → ~(O & E)]

22. M: The mockingbird will sing; D: I will buy you a diamond ring; B: The diamond ring turns brass; L: I will buy you a looking glass; G: The looking glass breaks; A: I will buy you a billy goat; C: The billy goat takes logic; S: The billy goat is pretty smart.

~M → D
B → L
G → A
C → S
~M
\
S

24. W: William does his homework before ten o'clock; T: William watches television; V: William will see images of violence; A: William will see advertising.

W → T
T → (V & A)
\
W → A

25. N: There is a nuclear war; U: It will be started by the United States; R: It will be started by Russia.

$$\begin{aligned} & \mathbf{N \rightarrow (U \vee R)} \\ & \mathbf{\sim U \ \& \ \sim R} \\ & \backslash \ \mathbf{\sim N} \end{aligned}$$

26. G: The game will be won; S: Samson is allowed to play; T: Samson is tied up for a while.

$$\begin{aligned} & \mathbf{G \leftrightarrow S} \\ & \mathbf{T \ \& \ (T \rightarrow \sim S)} \\ & \backslash \ \mathbf{\sim G} \end{aligned}$$

27. O: The concert will be given outside; R: There is rain; A: The concert will be held in the auditorium; H: Many people will stay at home; W: The concert will be well attended.

$$\begin{aligned} & \mathbf{\sim R \rightarrow O} \\ & \mathbf{R \rightarrow A} \\ & \mathbf{\sim A \rightarrow H} \\ & \mathbf{H \rightarrow \sim W} \\ & \backslash \ \mathbf{W \rightarrow R} \end{aligned}$$

28. E: Einar opens his diner, called 'The Forty-Niner'; F: There will be finer food; D: Del will have a real choice for dining out; H: Hoggy Diner will be the best buy for fast food; G: Hoggy Diner fast food is very good; C: Hoggy Diner fast food gives Del a real choice for dining out; A: Del will stay around.

$$\begin{aligned} & \mathbf{E \rightarrow (\sim F \ \& \ D)} \\ & \mathbf{\sim E \rightarrow H} \\ & \mathbf{\sim G \ \& \ \sim C} \\ & \mathbf{\sim D \rightarrow \sim A} \\ & \backslash \ \mathbf{\sim E \rightarrow \sim A} \end{aligned}$$

30. **SKIP!**

31. E: Ethical relativism is true; O: There are objective moral values; K: Kantianism is true; S: Some other ethical theory is true.

$$\begin{aligned} & \mathbf{E \rightarrow \sim O} \\ & \mathbf{K \rightarrow O} \\ & \mathbf{\sim(E \ \& \ K)} \\ & \backslash \ \mathbf{(O \ \& \ \sim K) \rightarrow S} \end{aligned}$$

32. V: Exercise 32 is a valid argument; P: Exercise 32's premises are true; C: Exercise 32's conclusion is true.

$$\begin{aligned} &V \leftrightarrow \sim(P \ \& \ \sim C) \\ &\sim C \ \& \ P \\ \setminus \ \sim V \end{aligned}$$

EXERCISES FOR SECTION 2.4

PART I

1. We are given the form p .
 - a) This statement *can* be obtained from the given form p .
 - b) This statement *can* be obtained from the given form p .
 - c) This statement *can* be obtained from the given form p .
2. We are given the form $\sim(p \ \& \ q)$.
 - a) This statement *cannot* be obtained from the given form $\sim(p \ \& \ q)$.
 - b) This statement *can* be obtained from the given form $\sim(p \ \& \ q)$.
 - c) This statement *cannot* be obtained from the given form $\sim(p \ \& \ q)$.
3. See the solution in the back of the textbook, p. 433.
4. We are given the form $((p \ \& \ q) \vee r)$.
 - a) This statement *can* be obtained from the given form $((p \ \& \ q) \vee r)$.
 - b) This statement *cannot* be obtained from the given form $((p \ \& \ q) \vee r)$.
 - c) This statement *cannot* be obtained from the given form $((p \ \& \ q) \vee r)$.
5. We are given the form $(p \ \& \ (\sim p \rightarrow q))$.
 - a) This statement *cannot* be obtained from the given form $(p \ \& \ (\sim p \rightarrow q))$.
 - b) This statement *cannot* be obtained from the given form $(p \ \& \ (\sim p \rightarrow q))$.
 - c) This statement *cannot* be obtained from the given form $(p \ \& \ (\sim p \rightarrow q))$.

PART II

6. This is an *SL* statement. It is a statement letter, and all statement letters are *SL* statements.
7. See the solution in the back of the textbook, p. 433.
8. This is *not* an *SL* statement. ‘,’ is not an *SL* connective.
9. This is an *SL* statement. It has the logical form of a biconditional; ‘ \leftrightarrow ’ is its main connective.
10. This is an *SL* statement. It has the logical form of a disjunction; ‘ \vee ’ is its main connective.
11. This is *not* an *SL* statement. Parentheses are needed around either ‘ $A \rightarrow B$ ’ or

- ' $B \rightarrow C$ '.
12. This is an *SL* statement. It has the logical form of a conjunction; '&' is its main connective. (The parentheses around 'B' are OK (since 'B' is a statement letter and therefore an *SL* statement), but we might just as well have done without them.)
 13. See the solution in the back of the textbook, p. 433.
 14. This is an *SL* statement. It has the logical form of a biconditional; ' \leftrightarrow ' is its main connective.
 15. This is an *SL* statement. It has the logical form of a biconditional; ' \leftrightarrow ' is its main connective. (Here again, the parentheses around 'A' are OK (since 'A' is a statement letter and therefore an *SL* statement), but we might just as well have done without them. The parentheses around ' $\sim R$ ' are OK, too, since that's an *SL* statement, but we might just as well have done without *them*, too, as in #21.)
 16. This is an *SL* statement. It has the logical form of a conditional; ' \rightarrow ' is its main connective.
 17. This is *not* an *SL* statement. ' \sim ' can immediately precede *only* a statement letter or a punctuation symbol (or another tilde, as in #21), and so it *cannot* immediately precede a different connective symbol.
 18. This is *not* an *SL* statement. It seems here that ' \rightarrow ' is used as a *one*-place connective (like ' \sim '), but it is a *two*-place connective; it connects one statement with another.
 19. See the solution in the back of the textbook, p. 433.
 20. This is *not* an *SL* statement. It seems here that ' \sim ' is used as a *two*-place connective (like '&', ' \vee ', ' \rightarrow ', and ' \leftrightarrow '), but it is a *one*-place connective.
 21. This is an *SL* statement. It has the logical form of a negation; ' \sim ' is its main connective.