

## 2005 SIX SIGMA – TEST II

Time: 50 minutes, Max marks:25

Use of approved Six Sigma Tables is permitted

- 1) Explain the deficiencies of a one factor at a time experiment. (2 marks)
- 2) It is planned to study the variables that affect abrasive jet machining. The factors and possible levels are Nozzle dia 2 and 3 mm, stand-off distance 5 and 25mm, jet pressure 1 and 4 kg/sqcm. Design a Data Collection form for a two level Full Factorial experiment with two replications randomised in two blocks using uncoded variables, so that the machine operator can easily carry out the experiment. (3 marks)
- 3) Judge the significance of the following effects using a normal probability plot: A=17, B=2, AB=1, C=6, AC=1, BC=0.5, ABC=-4, D=42, AD=-58, BD=-3, ABD=4, CD=1, ACD=2, BCD=-3, ABCD=-2. (5 marks)
- 4) An experiment was conducted to study the factors affecting tensile strength after aging of a Beryllium Bronze with results as follows

A	B	C	Rep	Rep	Effects	
Be content %	Aging temp °C	Aging time min	1	2		
1	300	20	80	76	50	1
2	300	20	16	24	-19.5	a
1	400	20	76	80	0.5	b
2	400	20	22	18	1	ab
1	300	80	44	39	2	c
2	300	80	64	57	38.5	ac
1	400	80	41	42	-2.5	bc
2	400	80	62	59	-1	abc

Only the factors A and AC statistically significant. Develop a linear model and predict the strength for a Beryllium content of 1.75%, Aging Temp of 325°C and Aging Time of 60min.

- 5) Calculate the residuals for the above problem (Q4). (5 marks)
- 6) Determine the Curvature and test for its significance in the following experiment. (5 marks)

A	B	R1	R2
-1	-1	-6	0
1	-1	35	31
-1	1	22	24
1	1	25	29
0	0	22	24
0	0	23	26

- 7) An experiment was carried out to determine the factors affecting tool life. In order to establish the validity of results over mild steels with different carbon content, it was treated as a blocking factor. Determine the significant factors from the results given below:

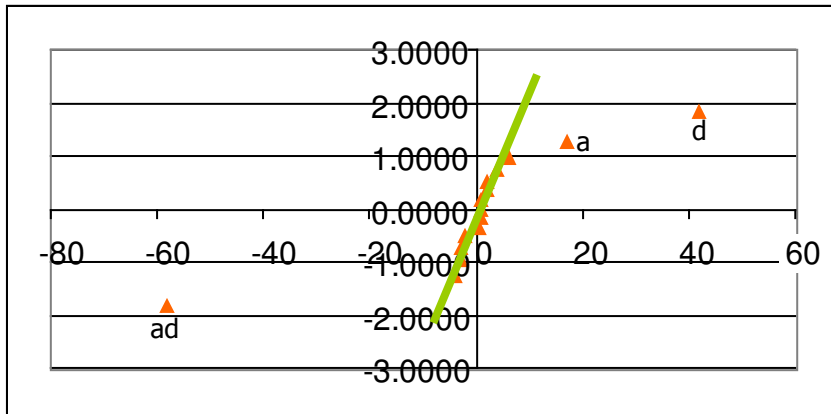
Speed (m/min)	Depth of cut (mm)	Carbon %	Tool Life (min)
5	2	0.05	44
20	2	0.05	48
5	6	0.05	50
20	6	0.05	59
5	2	0.1	28
20	2	0.1	23
5	6	0.1	31
20	6	0.1	40

(5 marks)

### SOLUTIONS TO PROBLEMS

3.

ad	-58	1	0.0333	-1.8339
abc	-4	2	0.1000	-1.2816
bd	-3	3	0.1667	-0.9674
bcd	-3	4	0.2333	-0.7279
abcd	-2	5	0.3000	-0.5244
bc	0.5	6	0.3667	-0.3407
ab	1	7	0.4333	-0.1679
ac	1	8	0.5000	0.0000
cd	1	9	0.5667	0.1679
b	2	10	0.6333	0.3407
acd	2	11	0.7000	0.5244
abd	4	12	0.7667	0.7279
c	6	13	0.8333	0.9674
a	17	14	0.9000	1.2816
d	42	15	0.9667	1.8339



4.

To predict at	1.75	325	60
Centre	1.50	350	50
Coded to predict	0.500	-0.500	0.333

$$Y_{pred} = 50 - 4.875 + 0.3333 + 3.2083 = 48.666$$

5.

Effects	last col	deleting insig	Reversing	1	2	3	div/8	Reversing	Res 1	Res 2
50	400	400	0	0	162	484	60.5	78	2	-2
-19.5	-78	-78	0	162	322	332	41.5	20	-4	4
0.5	2	0	154	0	-146	484	60.5	78	-2	2
1	4	0	8	322	478	332	41.5	20	2	-2
2	8	8	0	0	162	160	20	41.5	2.5	-2.5
38.5	154	154	0	-146	322	624	78	60.5	3.5	-3.5
-2.5	-10	0	-78	0	-146	160	20	41.5	-0.5	0.5
-1	-4	0	400	478	478	624	78	60.5	1.5	-1.5

6.

Average	Variance	dof	Curvature	3.7500
-3	18	1	Sp <sup>2</sup>	6.3929
33	8	1	Sp	2.5284
23	2	1	Sc	1.5483
27	8	1	t	2.4220
23.75	2.9167	3	tcrit	2.3646

Curvature is significant.

7.

1	2	3	Effects		
92	201	323	40.375	1	t
109	122	17	4.25	S	2.252
51	13	37	9.25	D	4.901
71	4	19	4.75	SD	2.517
4	17	-79	-19.75	C	
9	20	-9	-2.25	SC	
-5	5	3	0.75	DC	
9	14	9	2.25	SDC	
				Sumsq BI	10.6875
				Se <sup>2</sup>	3.5625
				Se	1.8875
				tcrit	3.182449291

Only D is significant.