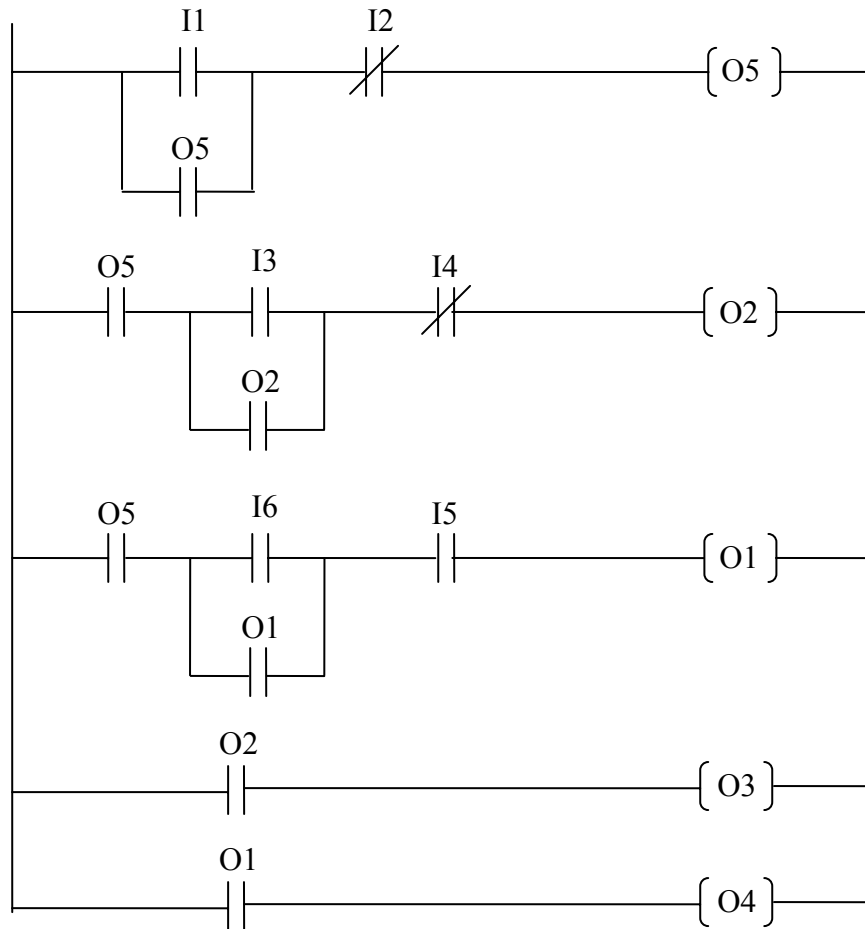


1-a)



1-b)

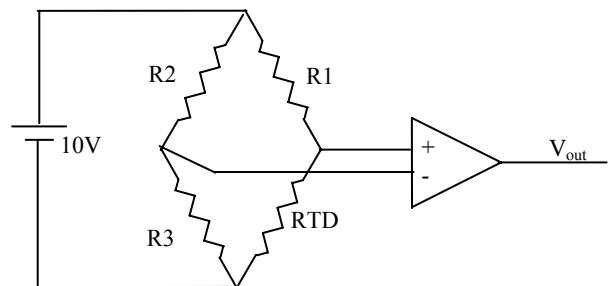
$$RTD_{20} = RTD_5 (1 + \alpha \Delta t)$$

$$= 150(1 + 0.02 * (35 - 5)) = 240 \Omega$$

$$R2 * RTD = R1 * R3$$

Let $R2 = 20k\Omega$, $R1 = 15K\Omega$

$$R3 = R2 * RTD / R1 = 240 / 15 = 320\Omega$$



2-a)

$$V3 = V1$$

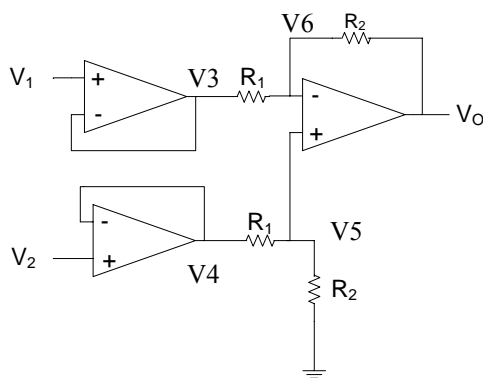
$$V4 = V2$$

$$V6 = V5 = V4 \frac{R2}{R2 + R1} = V2 \frac{R2}{R2 + R1}$$

$$\frac{V3 - V6}{R1} = \frac{V6 - V0}{R2}$$

$$\begin{aligned}
V_o &= V_6 + V_6 \frac{R_2}{R_1} - V_3 \frac{R_2}{R_1} \\
&= V_6 \frac{R_2 + R_1}{R_1} - V_3 \frac{R_2}{R_1} \\
&= V_4 \frac{R_2}{R_2 + R_1} \frac{R_2 + R_1}{R_1} - V_3 \frac{R_2}{R_1} \\
&= \frac{R_2}{R_1} (V_4 - V_3) \\
&= \frac{R_2}{R_1} (V_2 - V_1)
\end{aligned}$$

The voltage follower is used to make a high input impedance to avoid loading effect.



2-b)

1) $0V \rightarrow 0mA$

$7.5V \rightarrow 10mA$

$I = mV$

$$m = I/V = 10 \cdot 10^{-3} / 7.5 = 1/750 = 0.001333$$

$I = 0.001333V$

$$I = -V_1 \frac{R_2}{R_1 R_3}, \quad R_1(R_3 + R_5) = R_2 R_4$$

Let $R = 1k\Omega$

So

$$V = -V_1$$

$$\text{So } I = V \frac{R_2}{R_1 R_3}$$

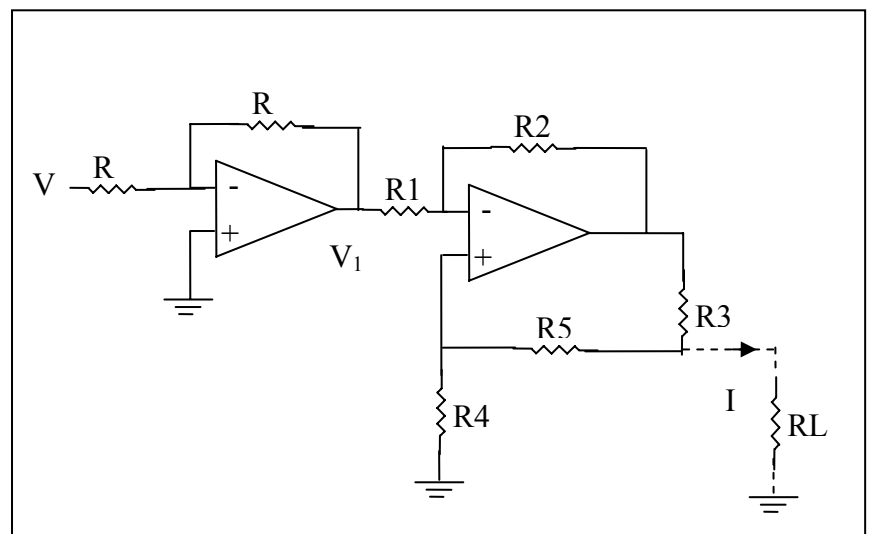
Let $R_1 = R_2 = 1k\Omega$, $R_5 = 0$

$$\text{So } I = V \frac{1}{R_3} = \frac{V}{750}$$

So $R_3 = 750\Omega$

$$R_1(R_3 + R_5) = R_2 R_4$$

$$R_3 = R_4 = 750\Omega$$



II) $0V \rightarrow 4mA$

$7.5V \rightarrow 20mA$

$I = mV + I_0$

As $0V \rightarrow 4mA$

$$.004 = m \cdot 0 + I_0$$

$$I_0 = 0.004$$

As $7.5V \rightarrow 20mA$

$$.020 = m \cdot 7.5 + I_0$$

$$.020 = m \cdot 7.5 + 0.004$$

$$m = 0.016 / 7.5 = 0.0021333$$

so $I = 0.0021333V + 0.004$

$$= 0.0021333(V + 1.875)$$

$$= -0.021333 V_1$$

$$V_1 = -(V + 1.875)$$

$$I = -V_1 \frac{R_2}{R_1 R_3}, \quad R_1(R_3 + R_5) = R_2 R_4$$

Let $R = 1k\Omega$

Let $R_1 = R_2 = 1k\Omega, R_5 = 0$

$$\text{So } I = -V_1 \frac{1}{R_3} = -0.0021333V_1$$

So $R_3 = 468\Omega$

$$R_1(R_3 + R_5) = R_2 R_4$$

$$R_3 = R_4 = 468\Omega$$

$0 \text{ ft} \rightarrow 4mA$

$20 \text{ ft} \rightarrow 20mA$

$I = m L + I_0$

As $0 \text{ ft} \rightarrow 4mA$

$$.004 = m \cdot 0 + I_0$$

$$I_0 = 0.004$$

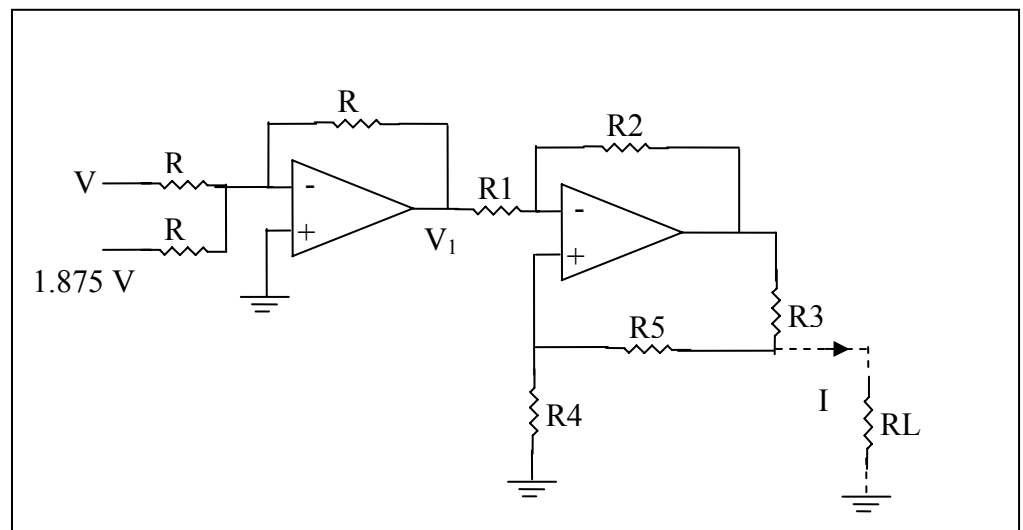
As $20 \text{ ft} \rightarrow 20mA$

$$.020 = m \cdot 20 + I_0$$

$$.020 = m \cdot 20 + 0.004$$

$$m = 0.016 / 20 = 0.0008$$

$$I = 0.0008 L + 0.004 = 0.0008 (L + 5) \text{ A} = .8(L + 5) \text{ mA}$$



3-a) Let $V_{max}=5V$
 $V=m*V_i+V_o$
 As $V_i = 2.5 \rightarrow V=0$
 $0=2.5m+V_o \quad \rightarrow 1$

As $V_i = 7 \rightarrow V=5$
 $5=7m+V_o \quad \rightarrow 2$

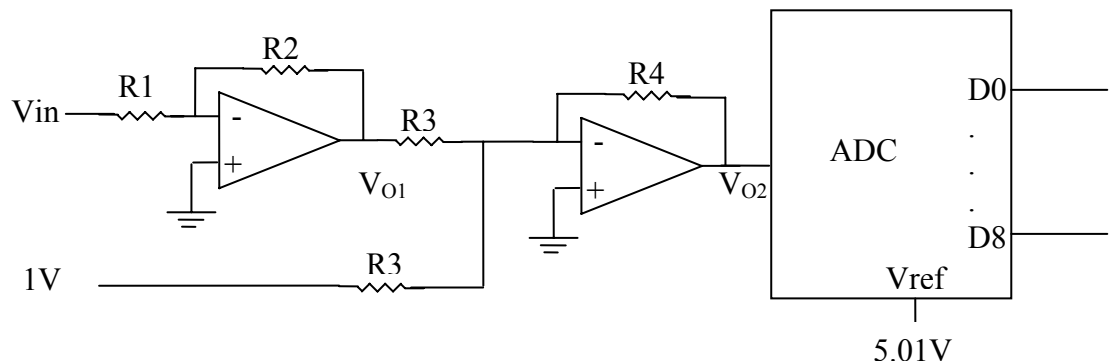
Subtract 2 from 1
 $4.5m=5$
 $m= 1.111$
 $V_o=-2.5m=-2.7775$

So $V=1.111V_i-2.7775=2.7775(.4V_i-1) \quad \rightarrow 3$

Let $V_{ref} \approx V_{max}$
 $\Delta V=1.111*\Delta V_i=0.01111=2^{-n}*V_{ref}$
 $2^{-n}=0.002222$
 $-\log_2=\log 0.002222$
 $n= 8.81= 9\text{bit}$

$V_{max}=\frac{(2^n-1)}{2^n} V_{ref}$

$V_{ref}=5.01V$



$V_{O1}=-\frac{R2}{R1} V_{in}$

$V_{O2}=-\frac{R4}{R3}(V_{O1}+1) \quad \rightarrow 4$

$=\frac{R4}{R3}\left(\frac{R2}{R1}V_{in} - 1\right)$

Comparing 3,4

$\frac{R2}{R1} = .4$

So let $R2=4k\Omega$ and $R1=10k\Omega$

And $\frac{R4}{R3}=2.7775$

So let $R4=277.75K\Omega$ and $R3=100K\Omega$

3-a –another solution --) Let $V_{max}=10V$

$$V=m*V_i+V_o$$

As $V_i = 2.5 \rightarrow V=0$

$$0=2.5m+V_o \quad \rightarrow 1$$

As $V_i = 7 \rightarrow V=10$

$$10=7m+V_o \quad \rightarrow 2$$

Subtract 2 from 1

$$4.5m=10$$

$$m= 2.222$$

$$V_o=-2.5m=-5.555$$

$$\text{So } V=2.222V_i-5.555=5.555(.4V_i-1) \quad \rightarrow 3$$

Let $V_{ref} \approx V_{max}$

$$\Delta V=2.222*\Delta V_i=0.02222=2^{-n}*V_{ref}$$

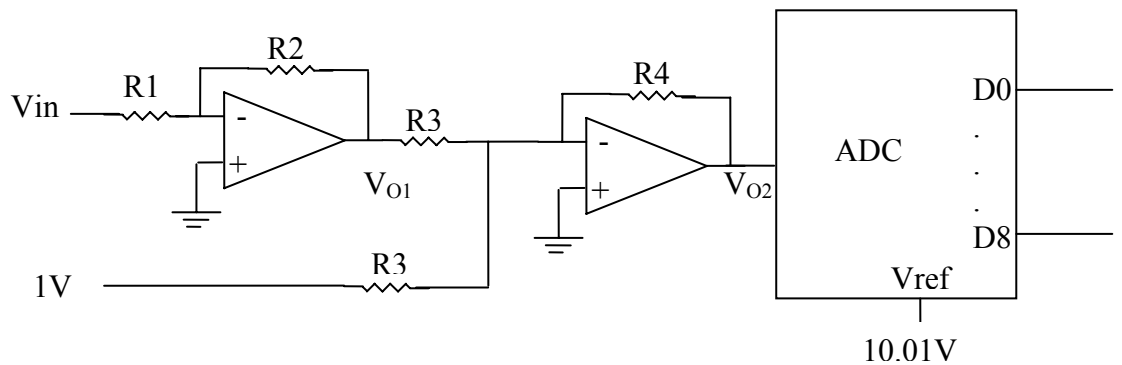
$$2^{-n}=0.02222$$

$$-n\log 2=\log 0.02222$$

$$n= 8.81= 9\text{bit}$$

$$V_{max}=\frac{(2^n-1)}{2^n} V_{ref}$$

$$V_{ref}=10.01V$$



$$V_{O1}=-\frac{R2}{R1} V_{in}$$

$$V_{O2}=-\frac{R4}{R3}(V_{O1}+1) \quad \rightarrow 4$$

$$= \frac{R4}{R3} \left(\frac{R2}{R1} V_{in} - 1 \right)$$

Comparing 3,4

$$\frac{R2}{R1} = .4$$

So let $R2=4k\Omega$ and $R1=10k\Omega$

$$\text{And } \frac{R4}{R3} = 5.555$$

So let $R4=55.55K\Omega$ and $R3=10K\Omega$

3-b)

$$I) N = \text{int} \left(2^n \left(\frac{V}{V_{\text{ref}}} + \frac{1}{2} \right) \right)$$

$$\text{At } V = -3.4 \quad N = 40.96 \approx 40$$

$$\text{At } V = 4 \quad N = 230.4 \approx 230$$

$$II) V = V_{\text{ref}} \left(\frac{N}{2^n} - 0.5 \right)$$

$$\text{For } N = C_6H_6 = 6 + 12 \cdot 16 = 198$$

$$\text{So } V(N=198) \leq V < V(N=199)$$

$$V(N=198) = 2.734V$$

$$V(N=199) = 2.773V$$

$$\text{So } 2.734 \leq V < 2.773$$