

# Active Pixel Sensors

EEL 5357 Analog CMOS/VLSI Design

## Absorption

The energy of a photon

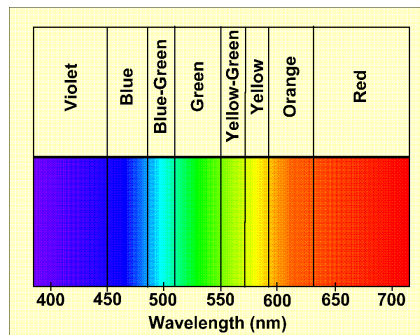
$$E = \frac{1240}{\lambda}$$

Where  $\lambda$  is the wavelength of light in nm

Example

Let  $\lambda = 450$  nm (blue)

$$E = \frac{1240}{450} = 2.75 \text{ eV}$$



Visible Spectrum (380-740 nm)

**Bandgap** of a semiconductor,  $E_g$ , is the energy required to raise an electron from the valence to conduction band

If  $E > E_g$ , a photon may be converted into an electron-hole (e-h) pair which is known as **optical absorption**

On the other hand, if  $E < E_g$ , the photon will pass through the material.

**Cut off wavelength**

$$\lambda_c = \frac{1240}{E_g}$$

Example

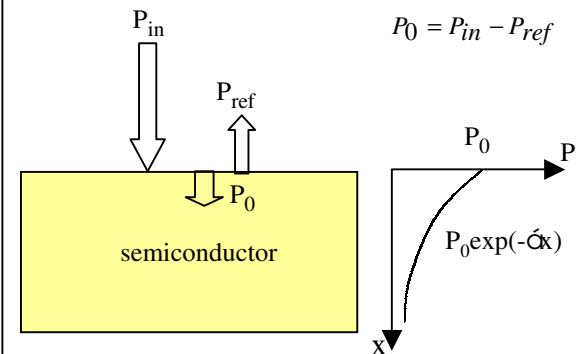
For Si  $E_g = 1.12$  eV

$$\lambda_c = \frac{1240}{1.12} = 1107 \text{ nm}$$

Wavelengths less than 1100 nm generate e-h pairs in Si

**Absorption Coefficient ( $\alpha$ )**

Defines the depth of penetration of the light in a material for a particular wavelength



$P_{in}$  is the incident and  $P_{ref}$  is the reflected optical power.

From Lambert-Beer law, the optical power at a distance  $x$  is

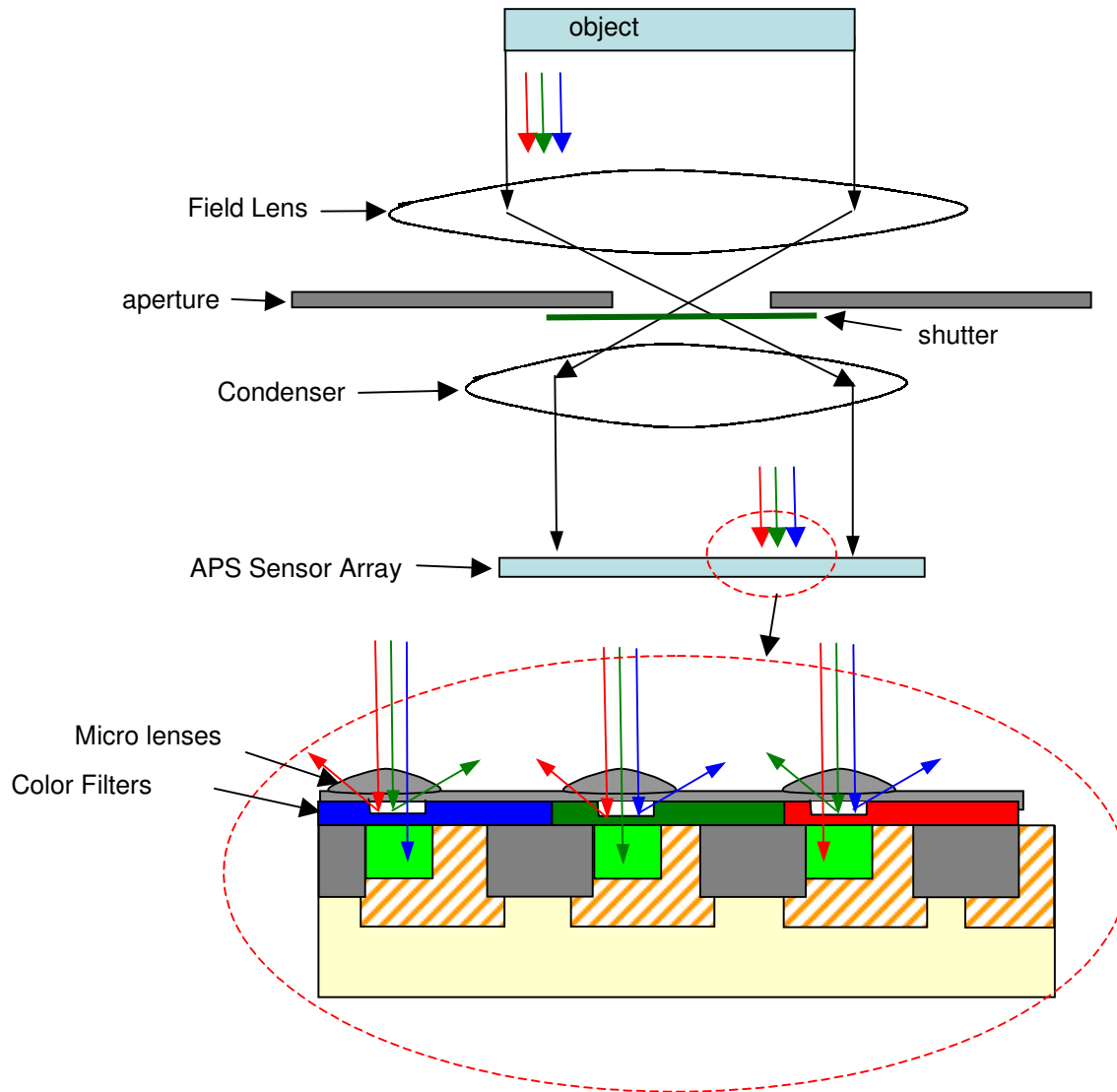
$$P(x) = P_0 e^{-\alpha x}$$

where  $P_0 = E \Phi_0 A$  and

$\Phi_0$  is the photon flux density (photons/s-cm<sup>2</sup>)

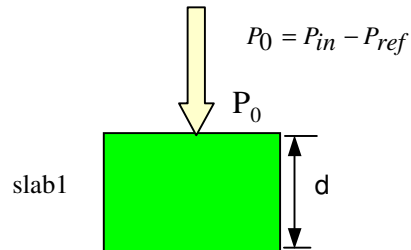
Prepared by: Ashok Rangaswamy

# Digital Camera Configuration



## Photodiode Model

### Semiconductor Slab



e-h pair generation rate per unit volume,

$$g(x) = \frac{\alpha}{A} \Phi_0 e^{-\alpha x}$$

$\Phi_0$  is the photon flux density (photons/s-cm<sup>2</sup>)

$$\Phi_0 = \frac{P_0}{A(h\nu)}$$

e-h pair generation rate per unit area,

$$G = \frac{\Phi_0}{A} [1 - e^{-\alpha d}]$$

The absorption efficiency is

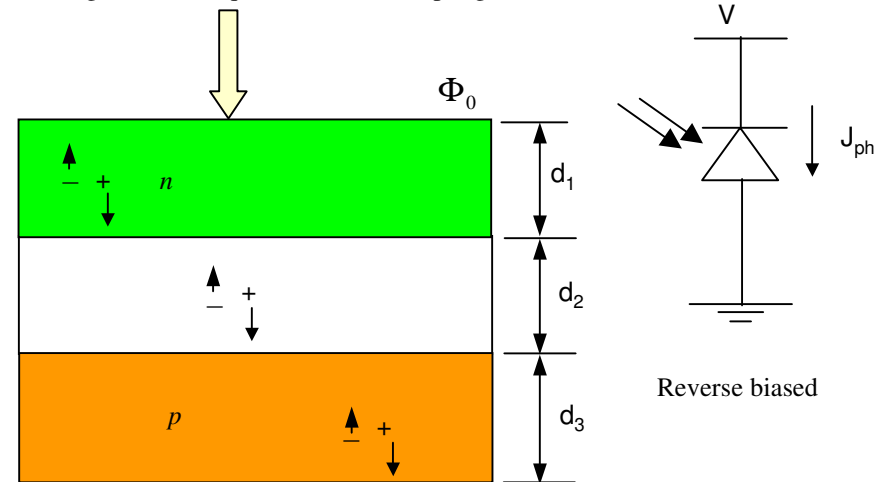
$$\eta_o = \frac{P_{absorbed}}{P_0} = (1 - e^{-\alpha d})$$

Internal quantum efficiency  $\zeta_i$  is the number of photogenerated electron-hole pair, that contribute to the photocurrent per incident photon

External quantum efficiency is

$$\eta_{ext} = \eta_o \zeta_i$$

Photo current components in photodiode are  
 Generated carriers in space charge region (SCR) –drift current  
 Minority carriers generated in quasi neutral n and p regions-diffusion current



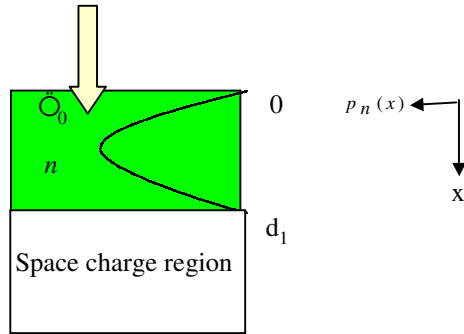
e-h pair generation rate per unit area in SCR

$$G_{SCR} = \Phi_0 [e^{-\alpha d_1} - e^{-\alpha d_2}]$$

Current density  $J_{SCR}$ , assuming all generated e-h pair are swept away by the junction potential (drift) and collected before they recombine

$$J_{SCR} = q \Phi_0 [e^{-\alpha d_1} - e^{-\alpha d_2}]$$

## Photodiode Model Contd...



$\Phi_0$  is the photon flux density (photons/s-cm<sup>2</sup>) at the semiconductor surface after reflection

$P_n(x)$  is the photo generated minority carrier density (hole) in n-region and  $D_p$  is the diffusion constant of holes in cm<sup>2</sup>/s

e-h pair generation rate per unit volume,

$$g(x) = \alpha \Phi_0 e^{-\alpha x}$$

Current density due to diffusion in n region,

$$J_{pn} = -qD_p \frac{\partial p_n(x)}{\partial x} \Big|_{x=d_1}$$

To find  $P_n(x)$  use continuity equation,

$$\frac{\partial p_n(x)}{\partial t} = D_p \frac{\partial^2 p_n(x)}{\partial x^2} + g_n(x) - R_n(x)$$

By short channel assumption, recombination rate is zero and under steady state the lhs is zero.

Therefore

$$D_p \frac{\partial^2 p_n(x)}{\partial x^2} + g_n(x) = 0$$

Integrating twice we get the solution of form,

$$p_n(x) = a + bx - \frac{\Phi_0}{\alpha D_p} e^{-\alpha x}$$

Using the boundary conditions  $p_n(0) = p_n(d_1) = 0$ , we get,

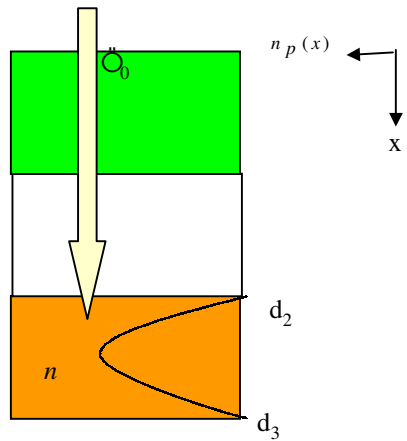
$$a = \frac{\Phi_0}{\alpha D_p} \quad \text{and} \quad b = \frac{-\Phi_0}{\alpha D_p d_1} [1 - e^{-\alpha d_1}]$$

$$p_n(x) = \frac{\Phi_0}{\alpha D_p} \left( 1 - \frac{x}{d_1} (1 - e^{-\alpha d_1}) - e^{-\alpha x} \right)$$

The current density due to the diffusion in the n- region,

$$\begin{aligned} J_{pn} &= -qD_p \frac{\partial p_n(x)}{\partial x} \Big|_{x=d_1} \\ &= \frac{-q\Phi_0}{\alpha} \left( \frac{-(1 - e^{-\alpha d_1})}{d_1} + \alpha e^{-\alpha d_1} \right) \\ &= \frac{q\Phi_0}{\alpha d_1} \left( 1 - (\alpha d_1 + 1) e^{-\alpha d_1} \right) \end{aligned}$$

## Photodiode model –Contd...



$n_p(x)$  is the photo generated minority carrier density (hole) in n-region and  $D_n$  is the diffusion constant of electrons in  $\text{cm}^2/\text{s}$

e-h pair generation rate per unit volume in p region,

$$g_p(x) = \alpha \Phi_0 e^{-\alpha x}$$

Current density due to diffusion in n region,

$$J_{np} = qD_n \frac{\partial n_p(x)}{\partial x} \Big|_{x=d_2}$$

Continuity equation under steady state,

$$D_n \frac{\partial^2 n_p(x)}{\partial x^2} + g_p(x) = 0$$

Using the boundary conditions  $p_n(d_3) = p_n(d_2) = 0$ , we get,

$$a = \frac{\Phi_0}{\alpha D_n (d_3 - d_2)} \left[ -e^{-\alpha d_3} + (d_3 - d_2 + 1)e^{-\alpha d_2} \right]$$

$$b = \frac{\Phi_0}{\alpha D_n (d_3 - d_2)} \left[ e^{-\alpha d_3} - e^{-\alpha d_2} \right]$$

$$n_p(x) = \frac{\Phi_0}{\alpha D_n} \left( a + \frac{x \left[ e^{-\alpha d_3} - e^{-\alpha d_2} \right]}{(d_3 - d_2)} - e^{-\alpha x} \right)$$

Hence the current density due to the diffusion in the p- region,

$$\begin{aligned} J_{np} &= qD_n \frac{\partial n_p(x)}{\partial x} \Big|_{x=d_2} \\ &= \frac{q\Phi_0}{\alpha(d_3 - d_2)} \left( \alpha(d_3 - d_2) - 1 \right) \left( e^{-\alpha d_2} + e^{-\alpha d_3} \right) \text{A/cm}^2 \end{aligned}$$

By adding  $J_{SCR}$ ,  $J_{pn}$ , and  $J_{np}$ , we obtain the total photo generated current density as

$$J_{photo} = \frac{q\Phi_0}{\alpha} \left( \frac{1 - e^{-\alpha d_1}}{d_1} + \frac{e^{-\alpha d_3} - e^{-\alpha d_2}}{d_3 - d_2} \right) \text{A/cm}^2$$

Then the internal efficiency (e-h pairs/photon) is given by

$$\eta_i(\lambda) = \frac{1}{\alpha} \left( \frac{1 - e^{-\alpha d_1}}{d_1} + \frac{e^{-\alpha d_3} - e^{-\alpha d_2}}{d_3 - d_2} \right) \text{electrons / photon}$$

and is a function of the wavelength (through  $\alpha(\lambda)$ ).

We may nominally define  $\zeta_i = q\eta_{max}$

## Junction Capacitance and Depletion width

$$x_n = \left\{ \frac{2\epsilon(V_{bi} + V)}{q} \frac{N_a}{N_d} \left[ \frac{1}{N_a + N_d} \right] \right\}^{1/2}$$

$$x_p = \left\{ \frac{2\epsilon_s(V_{bi} + V)}{q} \frac{N_d}{N_a} \left[ \frac{1}{N_a + N_d} \right] \right\}^{1/2}$$

Depletion width

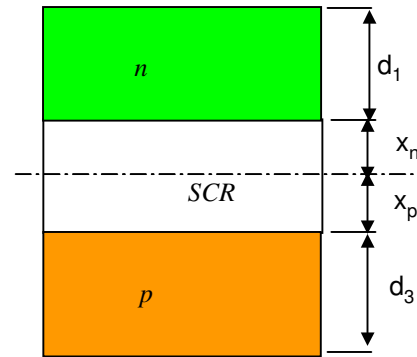
$$W = \left\{ \frac{2\epsilon(V_{bi} + V)}{q} \left[ \frac{N_a + N_d}{N_a N_d} \right] \right\}^{1/2}$$

Junction capacitance

$$C_D = \frac{\epsilon}{W}$$

Built in Potential,

$$V_{bi} = \frac{kT}{q} \log \left( \frac{N_a N_d}{n_i^2} \right)$$



Example

Consider a *p-n* diode with

$$N_a = 1 \times 10^{20} / \text{cm}^3 (p+)$$

$$N_d = 1 \times 10^{16} / \text{cm}^3 (n)$$

$$n_i = 1 \times 10^{10} / \text{cm}^3$$

Reverse biased for 2.2V at room temperature(300k),

$$V_{bi} = \frac{1.38E-23 \times 300}{1.6 \times 10^{-19}} \left( \log \left( \frac{1 \times 10^{20}}{1 \times 10^{10}} \right) + \log \left( \frac{1 \times 10^{16}}{1 \times 10^{10}} \right) \right)$$

$$= 0.9533V$$

$$\epsilon_{si} = 11.7 \times 8.85 \times 10^{14}$$

Therefore

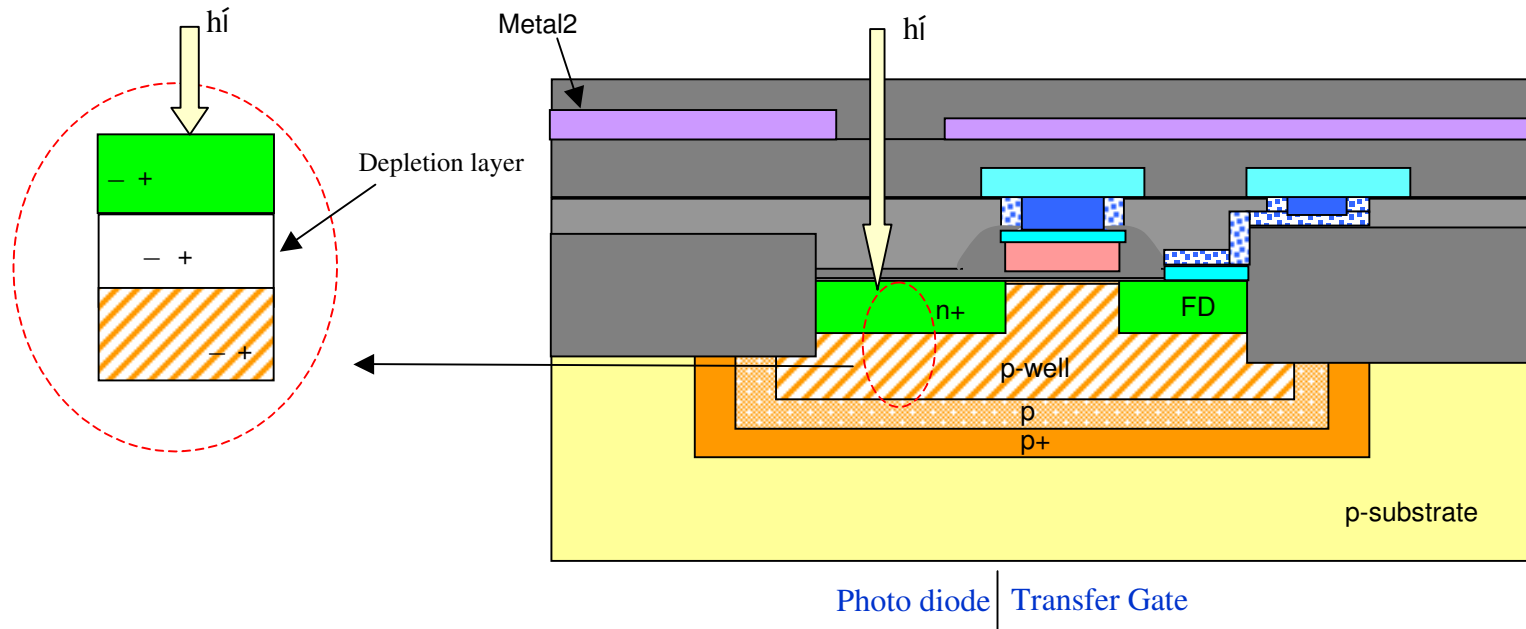
$$X_n = 0.639 \text{ microns}$$

$$X_p = 0.639 \times 10^{-4} \text{ microns}$$

$$W = 0.639 \text{ microns}$$

$$C_D = 16.21 \text{ nF}$$

## Active Pixel



### 1. Photon Collection

SiO<sub>2</sub>-with bandgap of 8 eV allows the visible light spectrum to pass through to the photodiode

Metal 2 acts as a light shield

Si with bandgap 1.12 eV collects the photons in the visible spectrum (400-700 nm)

The amount of photons getting converted into electrons depends on light intensity and transfer rate

This photo generated charge is transferred from the photodiode to the Floating Diffusion (FD) output node, when the transfer gate becomes active

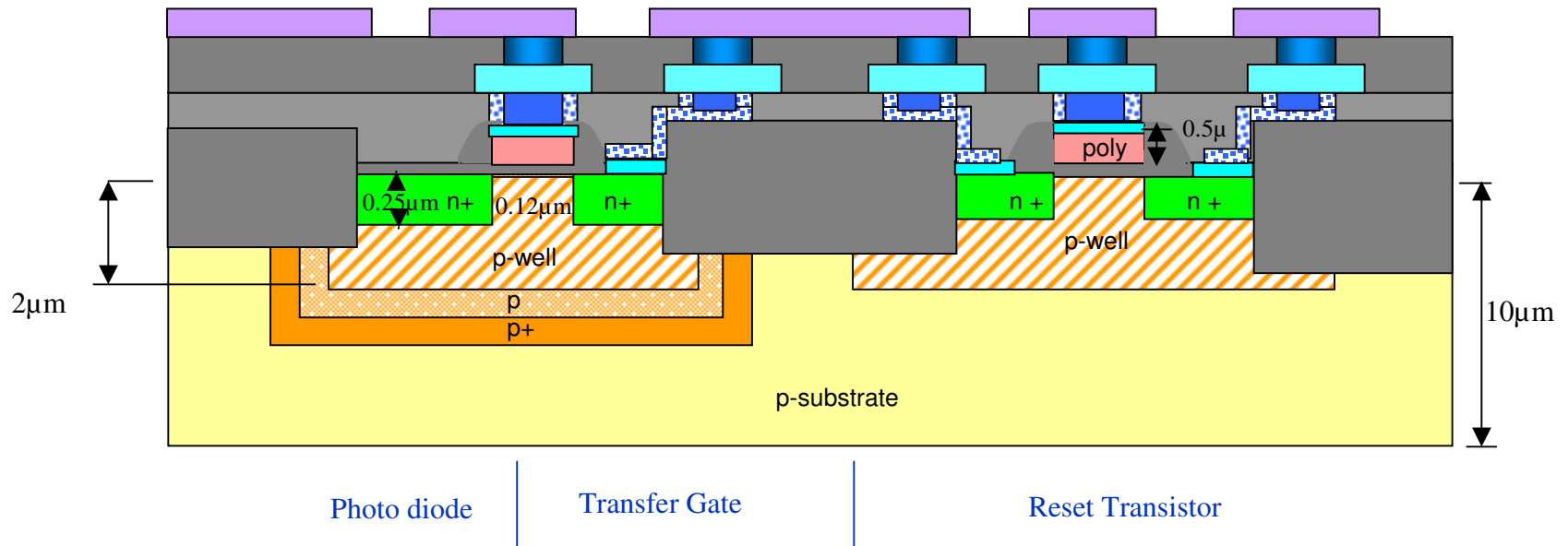
Noise from high-speed circuits is normally coupled to low-level analog circuits via references, substrate, and ground

***Triple well formation is one technique to isolate the most sensitive analog circuits from the digital circuits to avoid such noise***

IEEE Tran.Electron Devices, April 1998, p.889

<http://www.mosis.org/Technical/Designrules/scmos/scmos-contact.html#6>

## APS Fabrication



### Dimensions:

• of SCMOS Rule	0.25µm
Gate Oxide Thickness	4nm
Poly Thickness	0.5µm
Well Width	10 •
Metal1 Width	3 •
Via	2 • x 2 •
Metal2 Width	3 •
Active Contact	2 • x 2 •

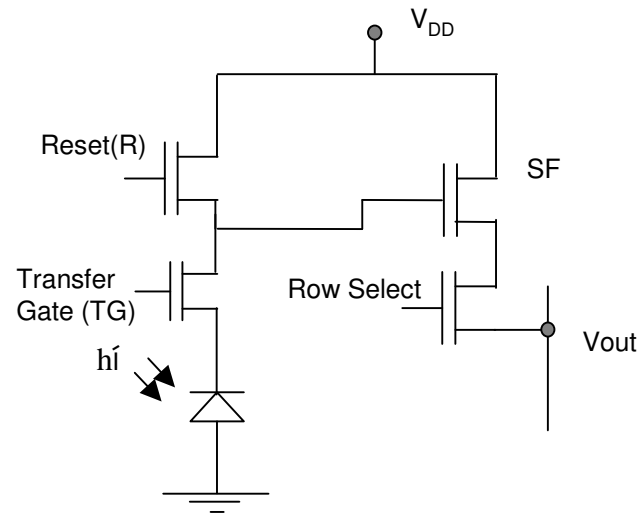
### Impurity Concentrations:

p-substrate	$10^{15}/\text{cm}^3$
p-well	$10^{16}/\text{cm}^3$
n+	$10^{20}/\text{cm}^3$
p+	$10^{20}/\text{cm}^3$

IEEE Tran.Electron Devices, April 1998, p.889  
<http://www.mosis.org/Technical/Designrules/scmos/scmos-contact.html#6>



## Active pixel Read out circuit



After charge integration, all pixels in a row are readout simultaneously onto column lines.

Reset **R** is pulsed briefly to HIGH which resets the floating diffusion output node (drain of TG MOSFET)

**Row Select** is biased briefly at HIGH; this activates the source follower **SF**

**TG** is then pulsed to HIGH

Thus gate potential of SF changes; output of **SF** depends on the amount of integrated charge

## Image Pixel

Instantaneous current is proportional to the incident photon flux

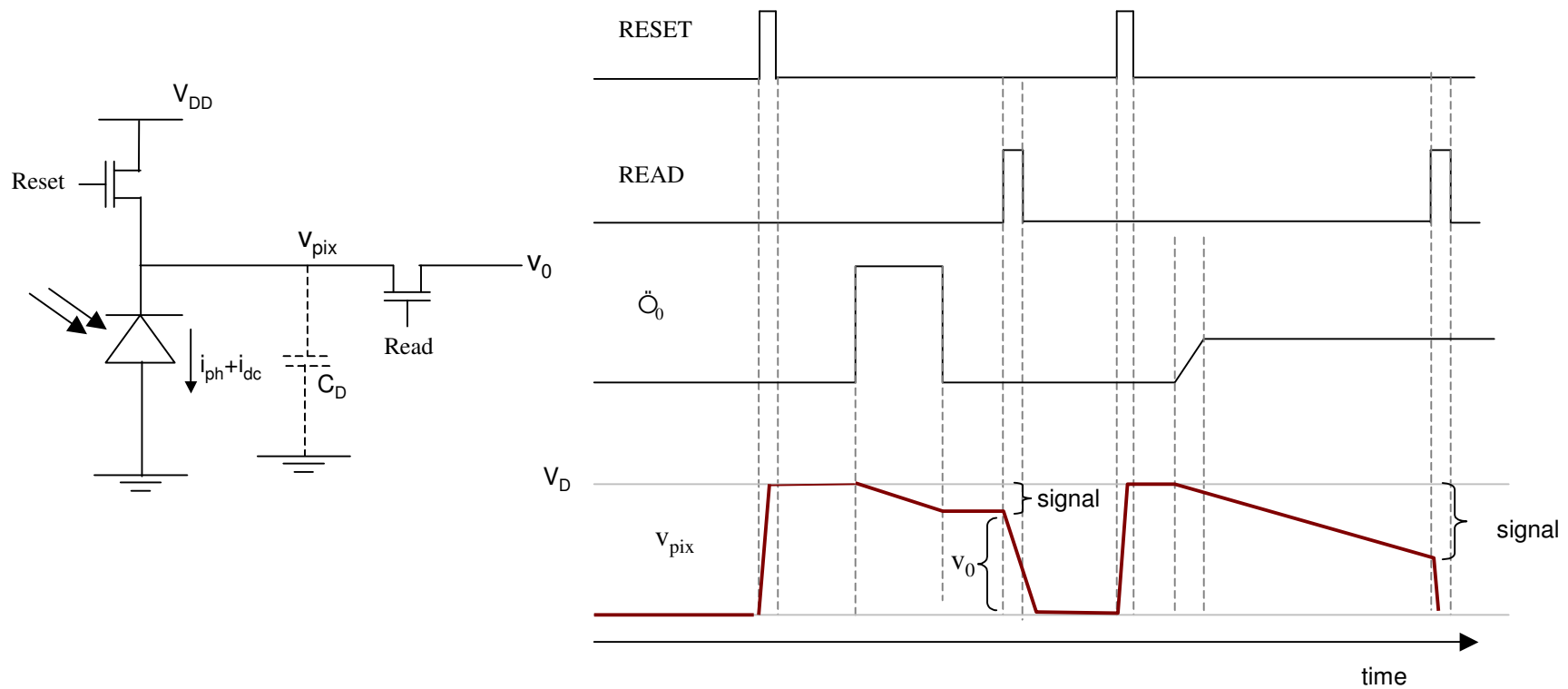
Reverse biased, but only to form a 'photo-capacitor' from the junction capacitance

When allowed to float (disconnected from reverse bias), this capacitance holds its charge

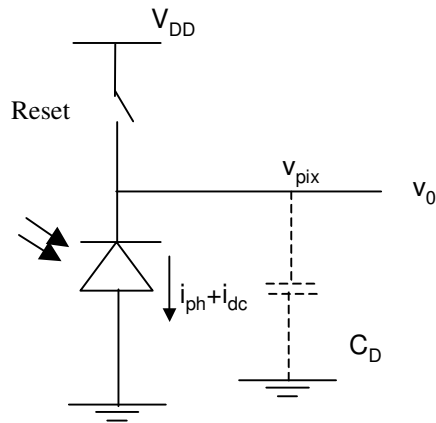
With incident light, photogenerated electrons bleed off the charge on the capacitance of the junction at a rate proportional to the incident photon flux

The **charge that bleeds is proportional to the "Exposure"**, time accumulated photon flux

This is then read out by conversion circuit which converts charge to voltage



## Direct Integration



Photodiode is reset to reverse bias voltage  $V_{DD}$   
 Diode current discharges  $C_D$  for  $t_{int}$  sec (integration time or exposure time)  
 At the end of integration time, the voltage  $v_0$  is read out  
 Assume photo ( $I_{ph}$ ) and dark current ( $I_{dc}$ ) do not change with reverse bias voltage,

$$Q(t_{int}) = (i_{ph} + i_{dc}) t_{int} \quad \text{Columbs}$$

### Dark Current ( $i_{dc}$ )

It is the photodetector leakage current, i.e., current not induced by photogeneration (under no illumination)

It limits the photodetector dynamic range  
 reduces signal swing  
 introduces unavoidable noise  
 can vary widely over the image sensor array causing fixed pattern noise (FPN)

Assume that  $C_D$  does not vary with reverse bias voltage

$$v_0(t_{int}) = V_D - \frac{(i_{ph} + i_{dc}) t_{int}}{C_D} \quad \text{Volts}$$

To avoid blooming ( overflowing of charges to the neighboring diodes), the diode should be reverse biased before exposure.

### Example

$$C_D = 1.55 \text{ fF}$$

$$i_{ph} = 167 \text{ fA}$$

$$i_{dc} = 2 \text{ fA}$$

$$t_{int} = 20 \text{ ms}$$

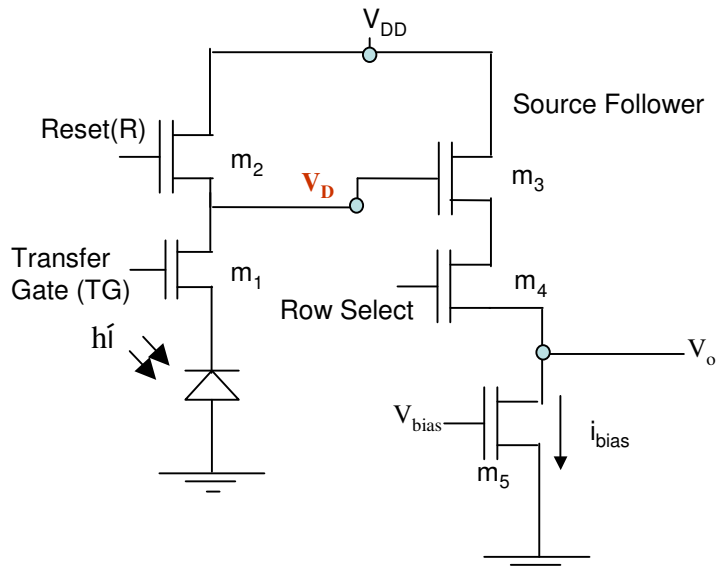
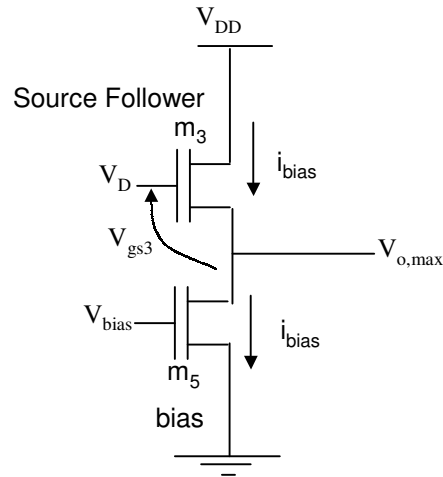
$$Q = (167 + 2) \times 10^{-15} \times 20 \times 10^{-3}$$

$$= 3.38 \times 10^{-15} \text{ Columbs}$$

$$V_o = V_{DD} - \frac{Q}{C_D}$$

$$= 5 - \frac{3.38}{1.5} = 2.25 \text{ V}$$

## Output Swing



$I_{bias}$  is m5 bias current

Assume first order MOS transistor model

$$I_{bias} = \frac{\beta_{n3}}{2} (V_{gs3} - V_{t3})^2$$

where  $\hat{Q}_{h3}$  is the device transconductance of  $m_3$ . Therefore

$$V_{gs3} = V_{t3} + \sqrt{\frac{2 I_{bias}}{\beta_{n3}}}$$

Let  $Q$  be the charge accumulated from PD at the end of integration.

Assume that the drop across access transistors is negligible. Then the output is

$$V_o = V_D - V_{gs3}$$

where

$$V_D = V_{DD} - V_{t2}$$

$V_{gs3}$  is the source follower transistor gate to source voltage

$V_{t2}$  is the reset transistor threshold voltage including body effect

$V_{t5}$  is the source follower transistor gate to source voltage

**Output swing is given by**

$$V_{o,min} = V_{bias} - V_{t5}$$

$$V_{o,max} = V_{DD} - V_{t2} - V_{gs3}$$

## APS Read Out

### Example

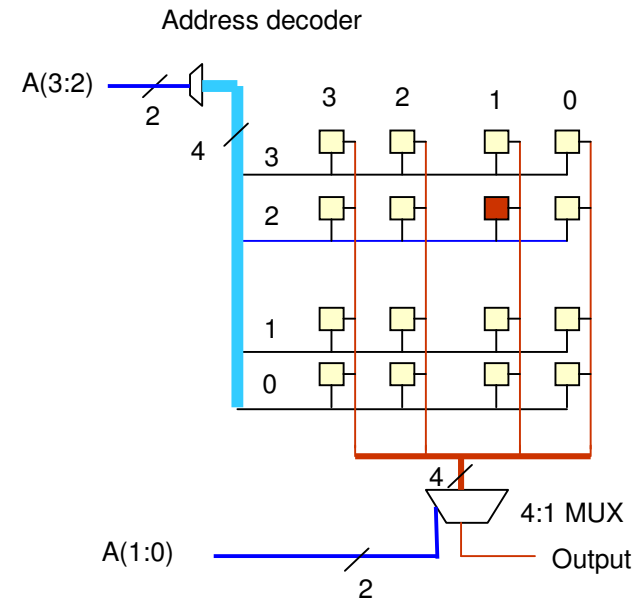
Consider a  $4 \times 4$  APS matrix

2:4 row decoder

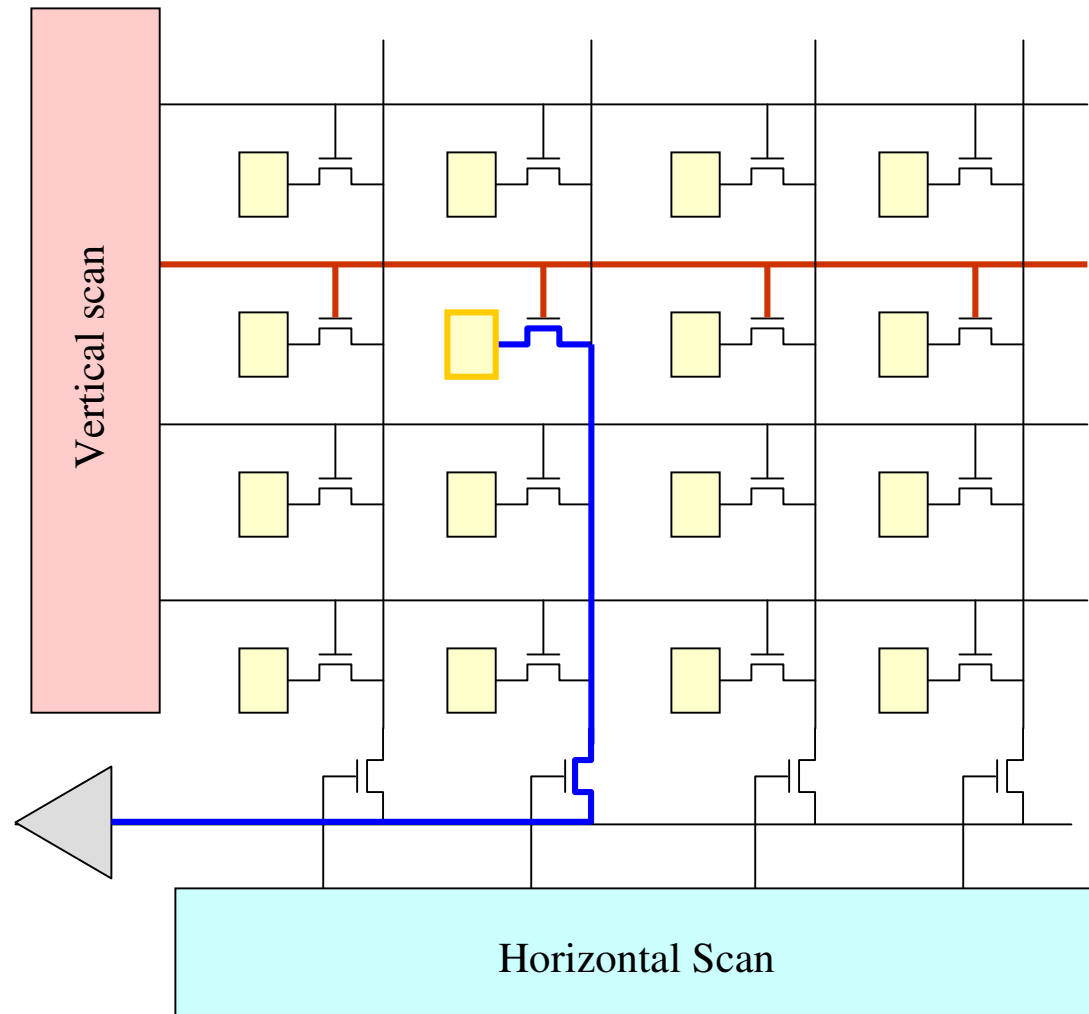
Direct integration of voltage is readout of the pixel, somewhat like a RAM

Readout is done in two stages:

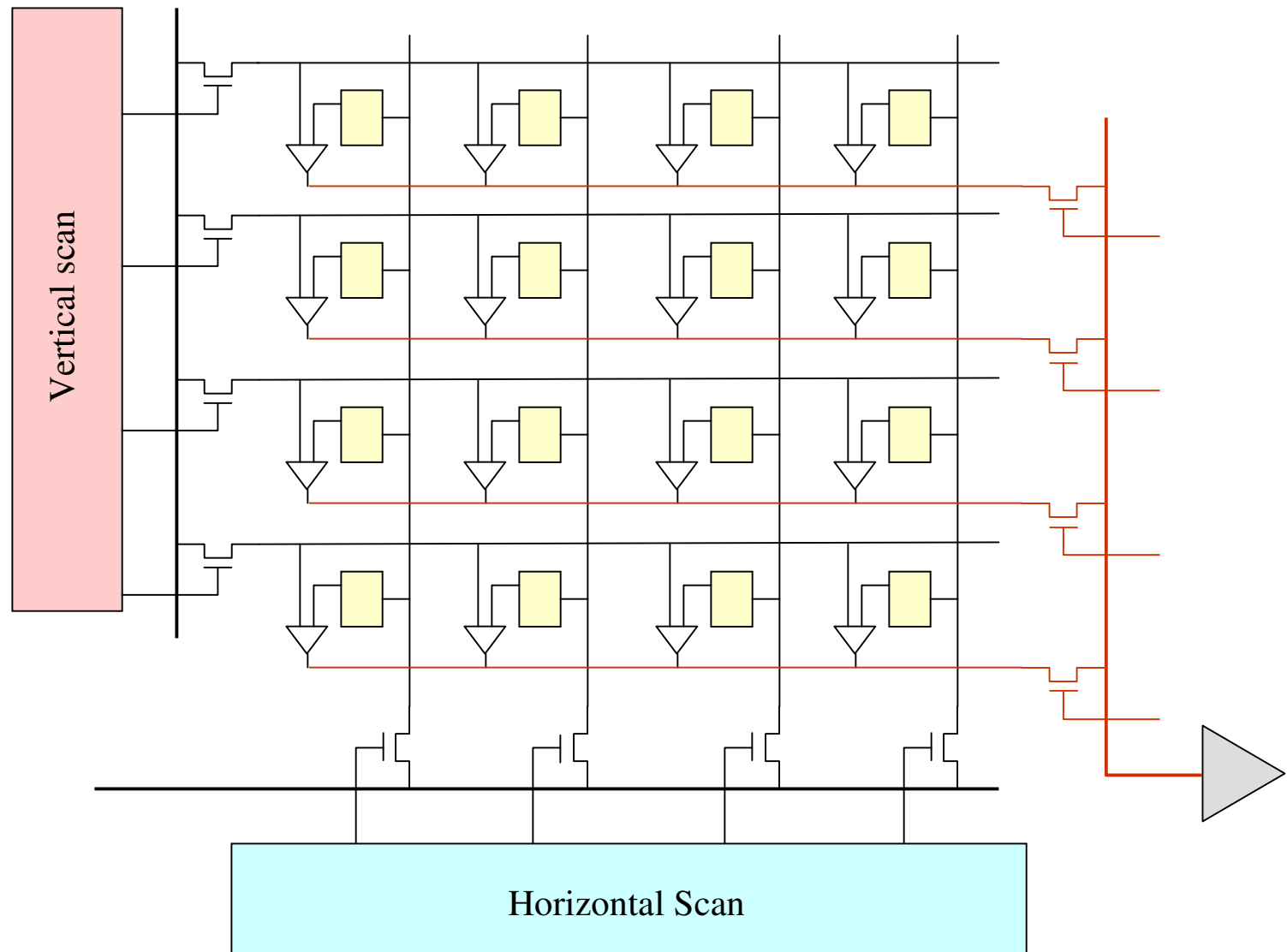
Initially, a row is selected using the row decoder the data and transferred to column multiplexer  
Then the data is transferred to data output, serially, using the column multiplexer.

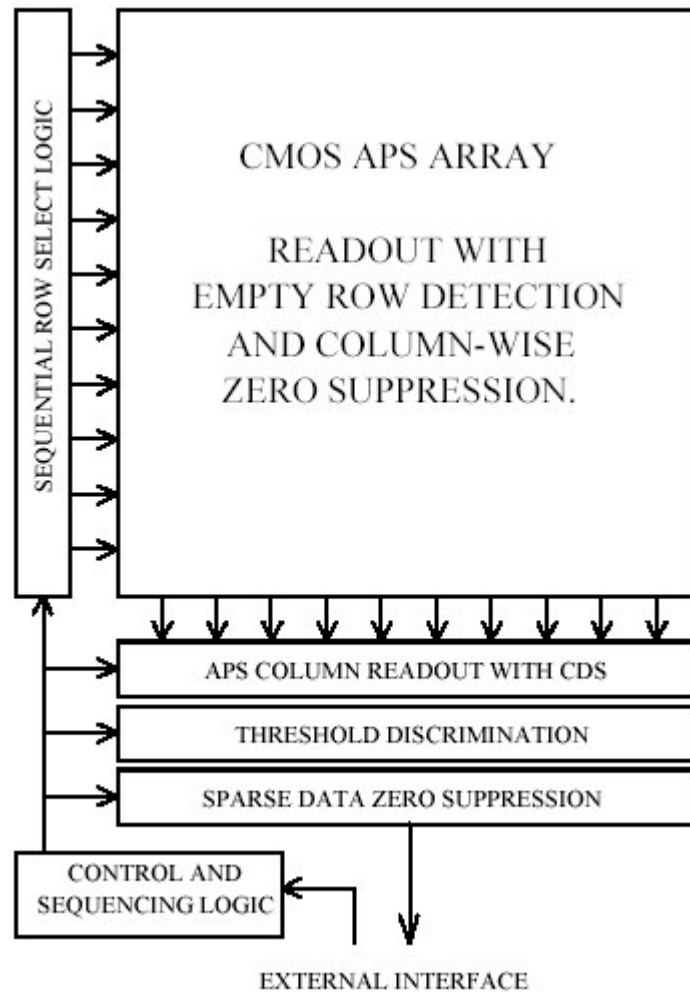


## Passive Pixel CMOS



## Active Pixel CMOS

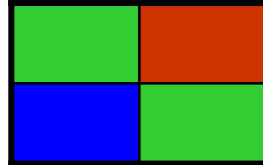




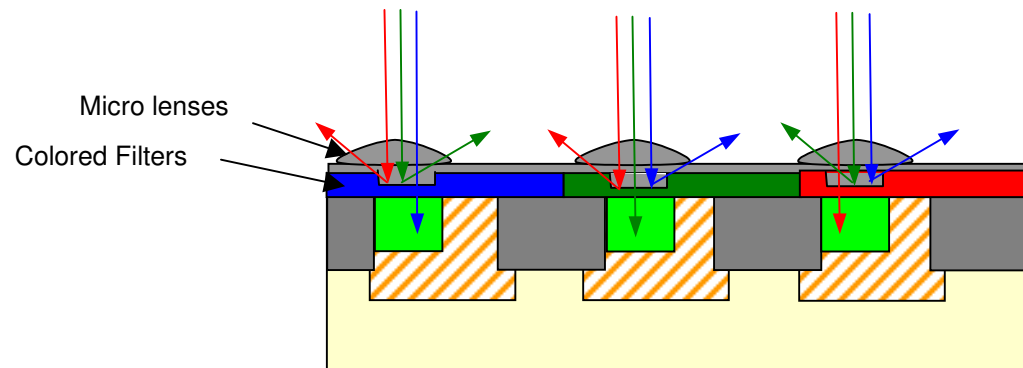


## Color Filter

- To enable Color imaging, each active pixel can be used to store one color, preferably in bayer's format



- This can be achieved using color filters for each pixel



## Microlens

- Microlens is fabricated over each pixel to focus light to active region of each pixel
- The ratio of the active region area ( photodiode area) to the total area of each pixel is called *the Fill Factor*

