

MATH3 (814013) – SPRING 2007

WORKSHEET 10

Question (1): Simplify each of the following as much as possible:

<u>1</u>	$(3x^2)(5x^4)(4x^5)$	<u>2</u>	$(2x^4y^2z^{-3})^2$
<u>3</u>	$(3u^{-3}v^2)^{-2}$	<u>4</u>	$\left(\frac{r^2s^3}{pq^4}\right)^5$
<u>5</u>	$\frac{10^{-9} \cdot 10^{-12}}{10^{-17} \cdot 10^5}$	<u>6</u>	$\left(\frac{w^{-2}}{w^{-4}}\right)^{-2}$
<u>7</u>	$\frac{6a^{-3}b^{-5}}{2a^{-7}b^{-2}}$	<u>8</u>	$\frac{20x^6y^{-2}z^4}{5x^3y^{-3}z^2}$
<u>9</u>	$\left(\frac{6mn^{-2}}{3m^{-1}n^2}\right)^{-3}$	<u>10</u>	$\left[\left(\frac{x^{-2}y^3t}{x^{-3}y^{-2}t^2}\right)^2\right]^{-1}$

Question (2): Simplify each of the following as much as possible:

1	$\left(\frac{x^{m^2}}{x^{2m-1}}\right)^{\frac{1}{m-1}}$	2	$(x^2 - y)(x + xy - y^2)$
3	$\left(\frac{a^{-2}}{b^{-1}} + \frac{b^{-2}}{a^{-1}}\right)^{-1}$	4	$\frac{4 - \frac{s^2}{r^2}}{\frac{s}{r} + 2}$
5	$\left(\frac{3x^2y^{-3}z^9}{2x^{-1}y^6z^{-3}}\right)^3$	6	$\left(\frac{a^{-1}b^{-3}}{a^m b^m} \cdot \frac{-2}{a^n b^m}\right)^{-mn}$
7	$\left(\frac{12m^{-3}n^2}{8m^{-2}n^3}\right)^{-2}$	8	$\left(\frac{-12x^3y^5z^{10}}{4x^6y^{-1}z^3}\right)^{-2}$
9	$\left(\frac{x^{n^2}x^n}{x^{-n}x^{-1}}\right)^{-\frac{1}{n+1}}$	10	$\frac{u^{-2}v^{-6}w^3}{vw^{-5}}$
11	$\left(\frac{(ab)^{-1}c^2}{(ac^{-2})^{-1}b^2}\right)^{-2}$	12	$\left[\frac{(x^2y)^{-1}(5^3x^3y^{-2})^2}{5^2(xy)^{-3}(x^5y^{-2})^{-1}}\right]^{-2}$

Question (3): What is the difference between the result of 2^{3^2} and 2^{2^3} ?

Question (4): Complete the following table.

Expression	$(-4)^2$	$-(4)^2$	-4^2	$-(-4)^2$
The value				

Question (5): Complete the following table.

Expression	$(-4)^3$	$-(4)^3$	-4^3	$-(-4)^3$
The value				

Question (6): Circle the correct answer.

(1) $\left(\frac{6x^2y}{3xy^{-1}}\right)^3 =$

(A) $8y^6x^3$

(B) $8x^3y^{-6}$

(C) $8y^6x^{-3}$

(D) None

(2) $\left(\frac{16xwry}{32xtuy^{-1}}\right)^0 =$

(A) 0

(B) 1

(C) $\frac{1}{2}$

(D) None

(3) $(3x^2y)(-2xy) =$

(A) $6x^3y^2$

(B) $-6x^2y^3$

(C) $-6x^3y^2$

(D) None

(4) $(3x^2y)(-2xy) =$

(A) $6x^3y^2$

(B) $-6x^2y^3$

(C) $-6x^3y^2$

(D) None

Question (7):

(1) The average of a , b and c is $\frac{4}{3}$, that is, $\frac{a+b+c}{3} = \frac{4}{3}$. Compute $3^a 3^b 3^c$.

(2) If $x = 1 + 2^m$ and $y = 1 + 2^{-m}$, then prove that $y = \frac{x}{x-1}$.

(3) Evaluate the number $\frac{(4444)^4}{(2222)^4}$.

(4) Prove that $4^{x+1} + 4^{x+2} = (20)4^x$.

(5) Simplify the following expression and write your answer using positive exponents.

$$\left[\frac{(r^{-1}s)^4 (rs)^{-1}}{r^5 (sr^0)} \right]^2$$