

Name _____

Algebra 2

Lesson 2-5

Absolute Value Functions and Graphs

An **absolute value function** is a function that contains an absolute value expression. This function is also a parent function that has the form of $y = |x|$. Graphed, it has a distinctive “V” shape with a minimum point or maximum point depending on the expression. The following examples are variations or “children” of absolute value functions.

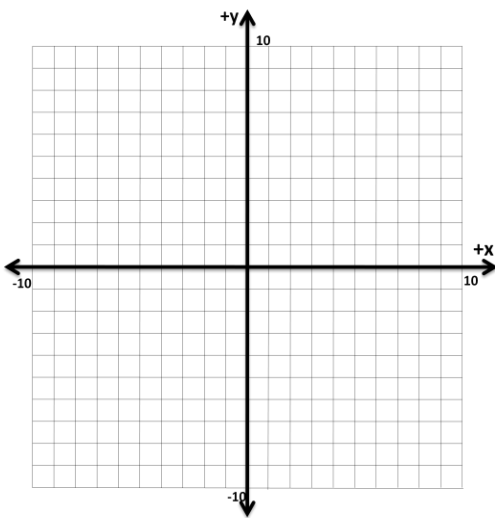
Examples: $f(x) = |x| + 3$

$$g(x) = |x + 1| - 4$$

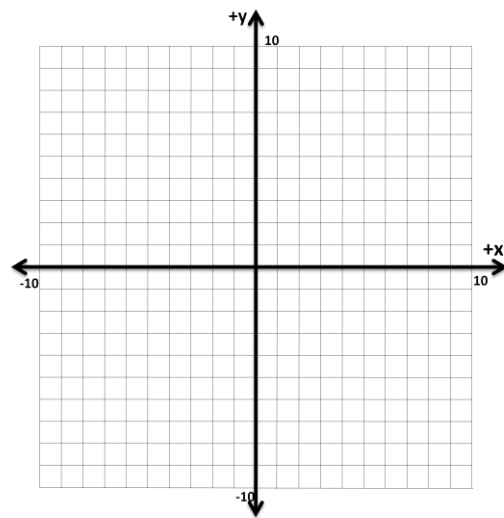
$$h(x) = -2|x| + 6$$

Like all other parent functions, absolute value functions can have variations that move left, right, up, down, compress, stretch, or a combination of several variations. When absolute value functions move up or down (translate), they will have the form of $f(x) = |x| + c$

$$f(x) = |x| - 3$$

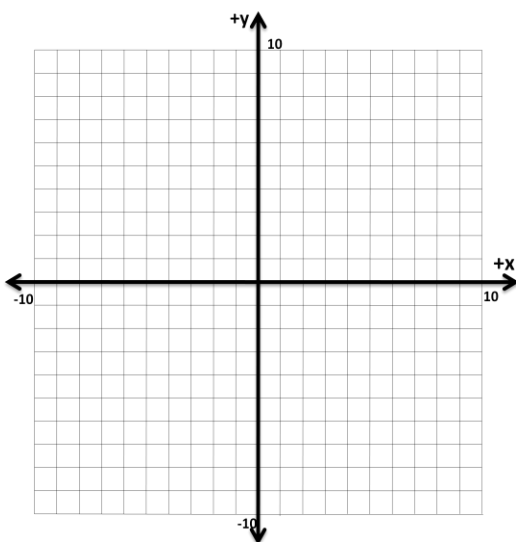


$$g(x) = |x| + 2$$

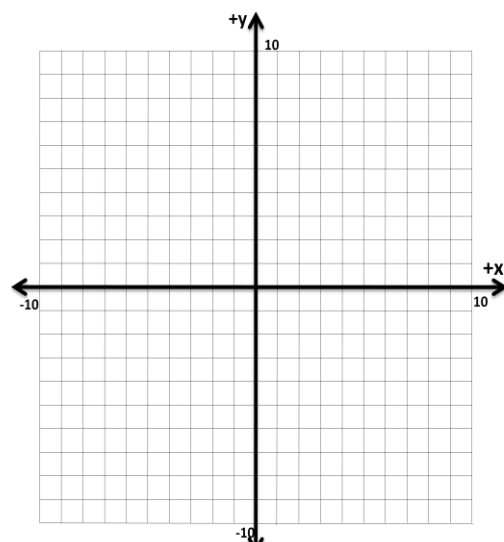


Absolute value functions that move left or right have the form: $f(x) = |mx + b| + c$.

$$f(x) = |x + 3|$$



$$g(x) = |x - 4|$$



Notice the “vertex”, the maximum or minimum point, of the graphs above is located at the point $(-\frac{b}{m}, c)$.

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Graphing an absolute value function can be accomplished using the tried and true method by selecting x or y values and solving the equation for the remaining variable and graph the x-y coordinates.

Absolute value functions can also be graphed on a graphing calculator:

1. Y= <enter>
2. MATH →1 <enter>
3. type equation
4. ZOOM 5

your graph should appear!

An absolute value function may also be graphed by using the two linear equation method: $y = |x - 3| + 5$

<ol style="list-style-type: none"> 1. isolate the absolute value (get it by itself) 2. using the definition of absolute value write 2 equations in the general forms: $x \pm _ \leq 0$, and $x \pm _ \geq 0$ 3. incorporating the first equation we get 2 situations 4. graph each equation for the appropriate domain (remember the domain comes from the definition) 	$y - 5 = x - 3 $ $x - 3 \geq 0, \text{ and } x - 3 \leq 0$ <div style="display: flex; justify-content: space-around;"> <div style="text-align: center;"> <p>when $x - 3 \geq 0$</p> $y - 5 = x - 3$ $y = x + 2$ <p>domains: $x \geq 3$</p> </div> <div style="text-align: center;"> <p>when $x - 3 \leq 0$</p> $y - 5 = -(x - 3)$ $y = -8 + x$ <p>$x \leq 3$</p> </div> </div>
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