

Name _____

Algebra 2
Lesson 1-1
Properties of Real Numbers
Part 1: Sets of Numbers

A **set** is a collection of things called **elements**.

Examples: the set of all numbers on a die are {1, 2, 3, 4, 5, 6}
the set of days in a week are {Mon., Tues., Wed., Thurs., Fri., Sat., Sun.}

A **subset** is a set of elements whose elements all belong to another larger set.

Examples: the set of all even numbers on a die are {2, 4, 6}
the set of weekend days are {Sat., Sun.}

An **empty** or null set $\{\emptyset\}$ is a set containing no elements.

Examples: the set of negative numbers between 1 and 10 $=\{\emptyset\}$
the set of months that have six weeks $=\{\emptyset\}$

There are five (5) sets of numbers that form the foundation for all of the mathematics. The three dots (. . .) is a notation used to mean "and so on and so on into infinity."

Natural Numbers = {1, 2, 3, 4, ...}

Whole Numbers = {0, 1, 2, 3, 4, ...}

Integers = {...-4, -3, -2, -1, 0, 1, 2, 3, 4, ...}

Rational Numbers = {all numbers that can be expressed as a ratio of two integers} = All integers + all fractions. Examples: {-2, 6, 25, $\frac{1}{3}$, 4, 7.5}

Irrational Numbers = {all numbers that are NOT rational and their decimal forms do NOT terminate or repeat. Examples: $\{\pi, \sqrt{3}, 6\sqrt{7}\}$

Notice that some numbers can belong to several sets of numbers while others can belong to only one set of numbers. For example, 3 can belong to all of the sets of numbers except Irrational Numbers. Why?

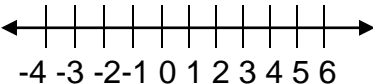
The number 0.25 can belong to only the _____ numbers. Then number $\sqrt{11}$ can only belong to the Irrational Numbers.

Number sets can be represented in several ways:

Words: The set of numbers on a six-sided die are 1 through 6.

Roster: {1, 2, 3, 4, 5, 6}

Interval: [1,6]

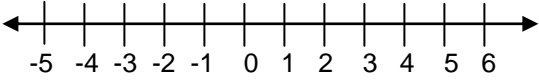
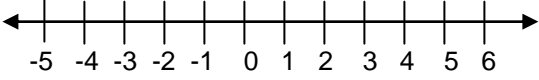
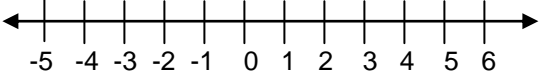
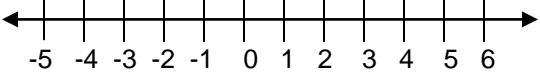
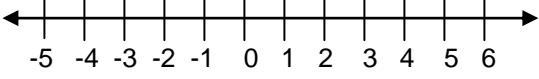
Number Line: 

Set Builder notation: $\{x \mid x \text{ is an integer and } 1 \leq x \leq 6\}$ read as "the set of all x's such that x is an integer between 1 and 6 inclusive."

Interval notation: [or] means the number is included, while (or) means number is not included.

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Algebra 2
Problem Set 1-1 part 1

<p>1. Classify each number to the sets of number it belongs.</p> <p>a) -2.4</p> <p>b) $\sqrt{30}$</p> <p>c) 2π</p> <p>d) $\frac{-5}{2}$</p> <p>2. Order the list of numbers from least to greatest.</p> <p>5, $\sqrt{17}$, -2.3, $-2\frac{3}{7}$, $\frac{2\pi}{3}$, 6.3333</p>	<p>5. Fill in the number lines.</p> <p>a) $-2 \leq x \leq 4$</p>  <p>b) The set of integers between -3 and 5.</p>  <p>c) $y \neq 2$.</p> 
<p>3. a) Rewrite $x \geq -1$ in interval notation.</p> <p>b) Rewrite $[-2,3]$ as a number line.</p>  <p>c) Rewrite the set of even integers between 6 and 24 inclusive in roster notation.</p> <p>d) Rewrite $\{2, 4, 6, \dots, 20\}$ in words.</p>	<p>6. Use a number line to represent $[-1,2)$ and $(3, +\infty)$ on a number line.</p>  <p>7. Translate, "the multiples of 4 up to 100" into a roster.</p> <p>8. What is the main difference between an undefined quantity and an irrational number?</p>
<p>4. Answer with True or False.</p> <p>a) Every integer is a whole number</p> <p>b) Every integer is a rational number</p> <p>c) Every irrational is not a whole number.</p> <p>d) A repeating decimal like 2.3333.... is an example of a rational number.</p> <p>e) A number like $\frac{4}{0}$ is an irrational number.</p>	<p>9. The formula for the area of a circle is: πr^2. Will the area for circle ever be a rational number? Briefly explain.</p> <p>10. Will the product of two irrational numbers ever be rational? Briefly explain.</p>