

MODULE MATHEMATICS SPM: Transformation

- 1 (a) Transformation **R** is a rotation  $90^\circ$  anticlockwise at  $(5, 5)$  and transformation **T** is a translation  $\begin{pmatrix} 4 \\ 2 \end{pmatrix}$ .

State the coordinates of the image of point  $(1, 4)$  under each of the following transformations:

- (i) Translation **T**,                      (ii) Combined transformations **TR**.

[3 marks]

- (b) Diagram 1 shows three quadrilaterals, *JKLM*, *PQRS* and *TUVW* drawn on a Cartesian plane.

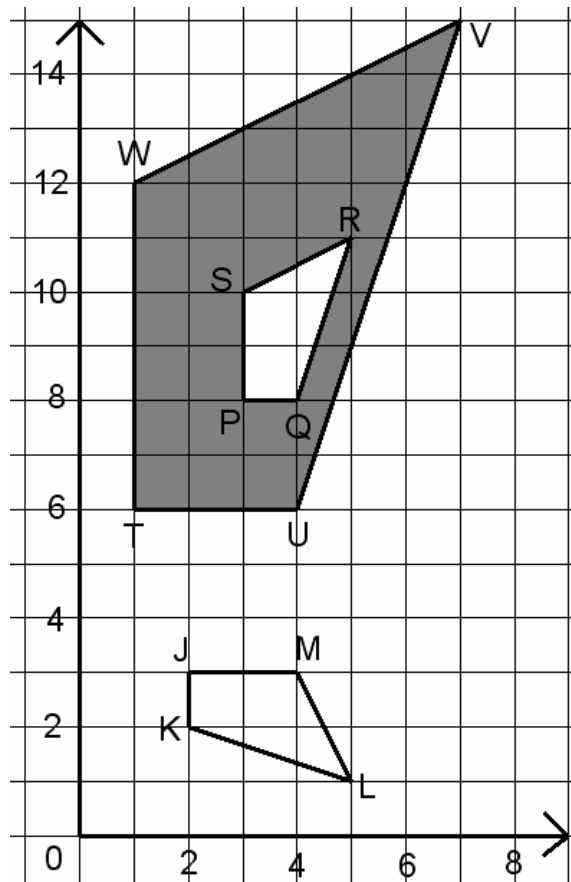


DIAGRAM 1

*PQRS* is the image of *JKLM* under transformation **Q**.

*TUVW* is the image of *PQRS* under transformation **M**.

- (i) Describe in full the transformation:

(a) **Q**,

(b) **M**.

[6 marks]

- (ii) Given that quadrilateral *JKLM* represents a region of area  $343 \text{ cm}^2$ . Calculate the area, in  $\text{cm}^2$ , of the shaded region. [3 marks]

2. The Diagram 2 shows pentagons ABCDE, GFCDH, PQRST and JKLMN on a Cartesian plane.

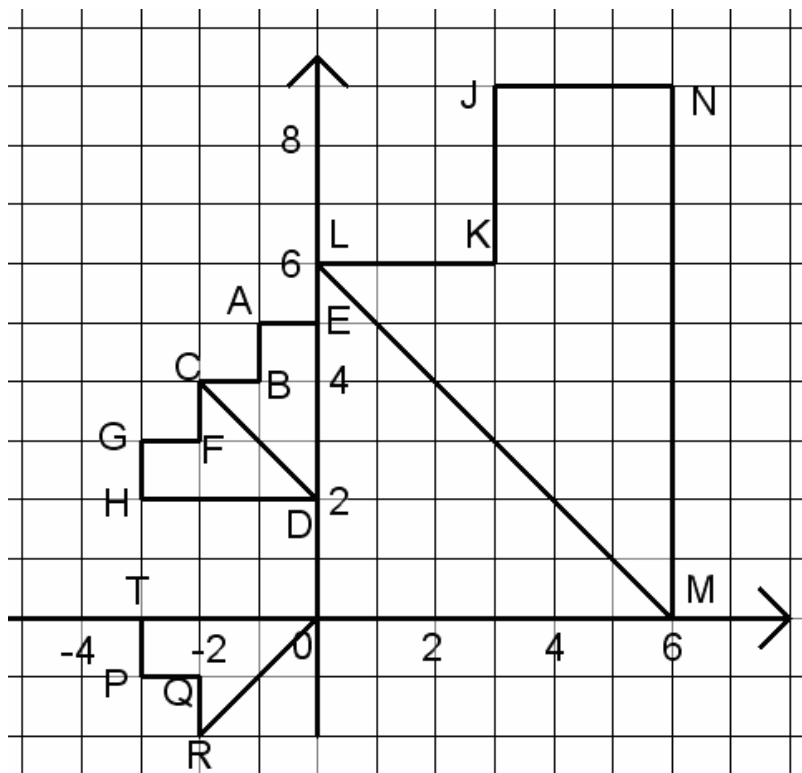


Diagram 2

- a) Transformation V is a reflection in the line  $y = 4$ . Transformation U is a translation  $\begin{pmatrix} -4 \\ -2 \end{pmatrix}$ .

State the coordinates of point S under the following transformation.

- i. V
  - ii. VU
- b) GFCDH is the image of ABCDE under a transformation X and PQRST is the image of ABCDE under a transformation Y. Describe in full
- i. the transformation X,
  - ii. the transformation Y.
- c) JKLMN is the image of ABCDE under an enlargement.
- i. State the center of enlargement.
  - ii. Given that the area of JKLMN is  $76.95 \text{ unit}^2$ , find the area of ABCDE.

3. Diagram 3 shows quadrilaterals,  $ABCD$ ,  $PQRS$  and  $KLRM$ , drawn on a Cartesian plane.

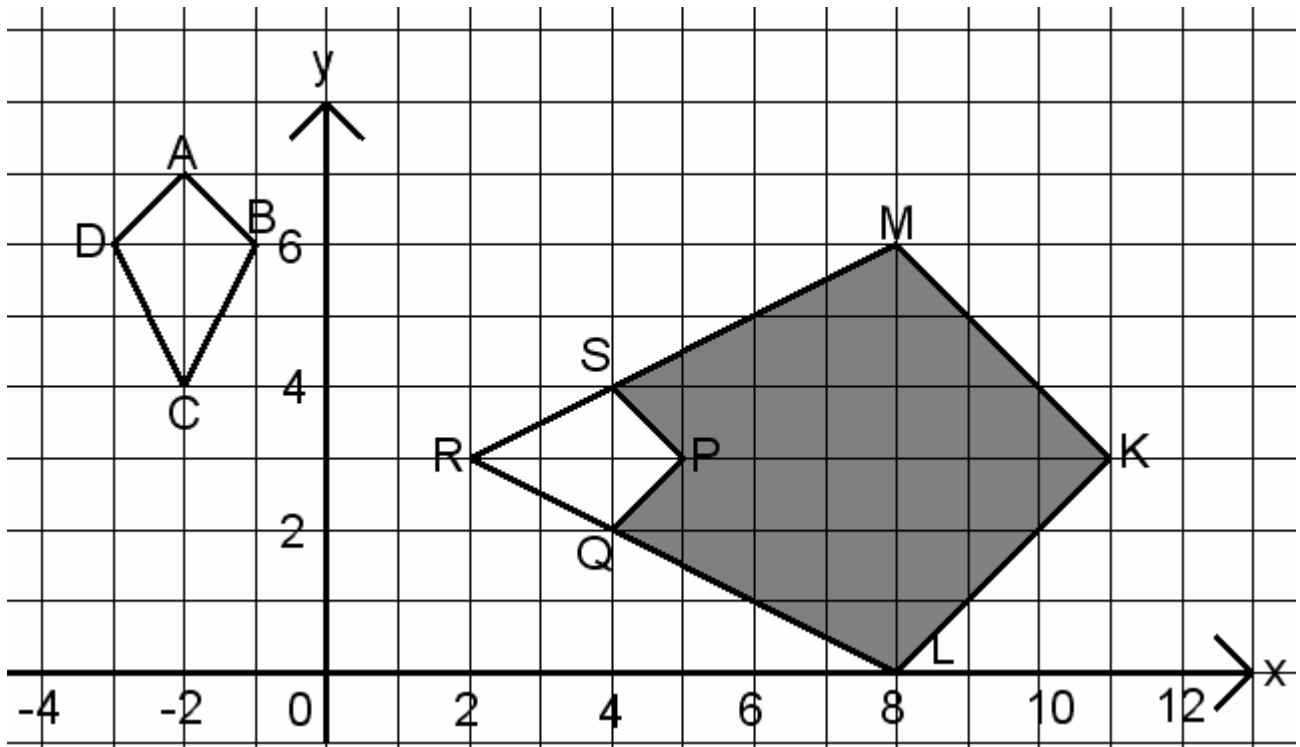


DIAGRAM 3

a) Transformation  $\mathbf{T}$  is a translation  $\begin{pmatrix} 4 \\ 2 \end{pmatrix}$ .

Transformation  $\mathbf{V}$  is a reflection in the line  $y = 1$ .

State the coordinates of the image of point  $A$  under each of the following transformations:

- i) Translation  $\mathbf{T}$ ,
- ii) Combined transformations  $\mathbf{VT}$ .

b) i)  $KLRM$  is the image of  $ABCD$  under the combined transformations  $\mathbf{WU}$ .

Describe in full, the transformation  $\mathbf{U}$  and the transformation  $\mathbf{W}$ .

ii) Given that the shaded region  $KLQPSM$  represents a region of area  $120 \text{ m}^2$ , calculate the area, in  $\text{m}^2$ , of the region represented by  $PQRS$ .

4. a) Diagram 4(i) shows two points,  $M$  and  $N$ , on a Cartesian plane.

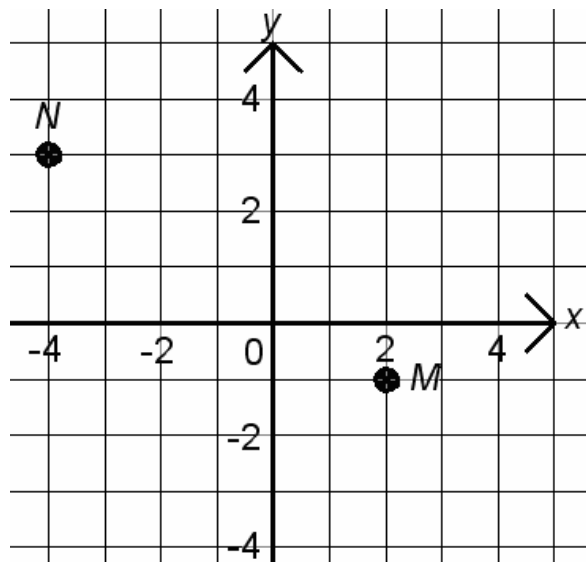


DIAGRAM 4(i)

Transformation  $T$  is a translation  $\begin{pmatrix} 3 \\ -1 \end{pmatrix}$ .

Transformation  $R$  is an anticlockwise rotation of  $90^\circ$  about the center  $(0, 2)$ .

- i) State the coordinates of the image of point  $M$  under transformations  $R$ .
- ii) State the coordinates of the image of point  $N$  under following transformation:
  - a.  $T^2$
  - b.  $TR$

b) Diagram 4(ii) shows three quadrilaterals,  $ABCD$ ,  $EFGH$  and  $PQRS$  on Cartesian plane.

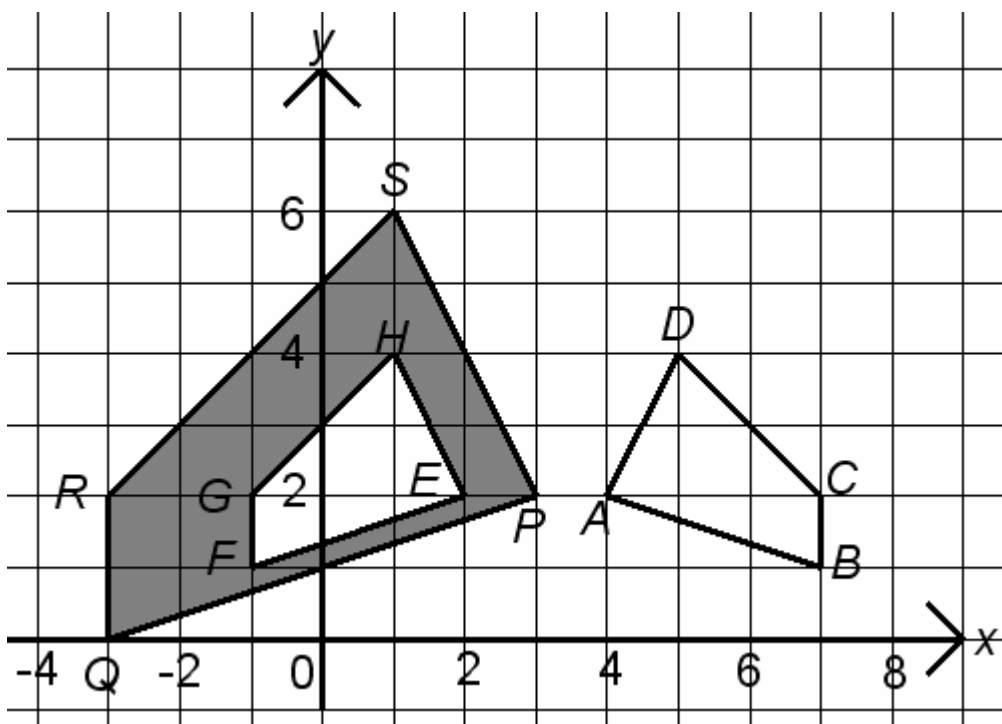


DIAGRAM 4(ii)

$EFGH$  is the image of  $ABCD$  under transformation  $\mathbf{V}$ .

$PQRS$  is the image of  $EFGH$  under transformation  $\mathbf{W}$ .

- i) Describe in full the transformation:
  - a.  $\mathbf{V}$ ,
  - b.  $\mathbf{W}$ .
- ii) Given that quadrilateral  $PQRS$  represents a region of area  $45.6 \text{ cm}^2$ , calculate the area, in  $\text{cm}^2$ , of the region represented by the shaded region.

5. a) Transformation **T** is a translation  $\begin{pmatrix} -3 \\ 2 \end{pmatrix}$  and transformation **P** is an anticlockwise rotation of  $90^\circ$  about the centre  $(1, 0)$ .

State the coordinates of the image of point  $(5, 1)$  under each of the following transformation:

- i) Rotation **P**
- ii) Translation **T**,
- iii) Combined transformation **T**<sup>2</sup>.

- b) Diagram 5 shows three quadrilaterals, *ABCD*, *EFGH* and *JKLM* drawn on a Cartesian plane.

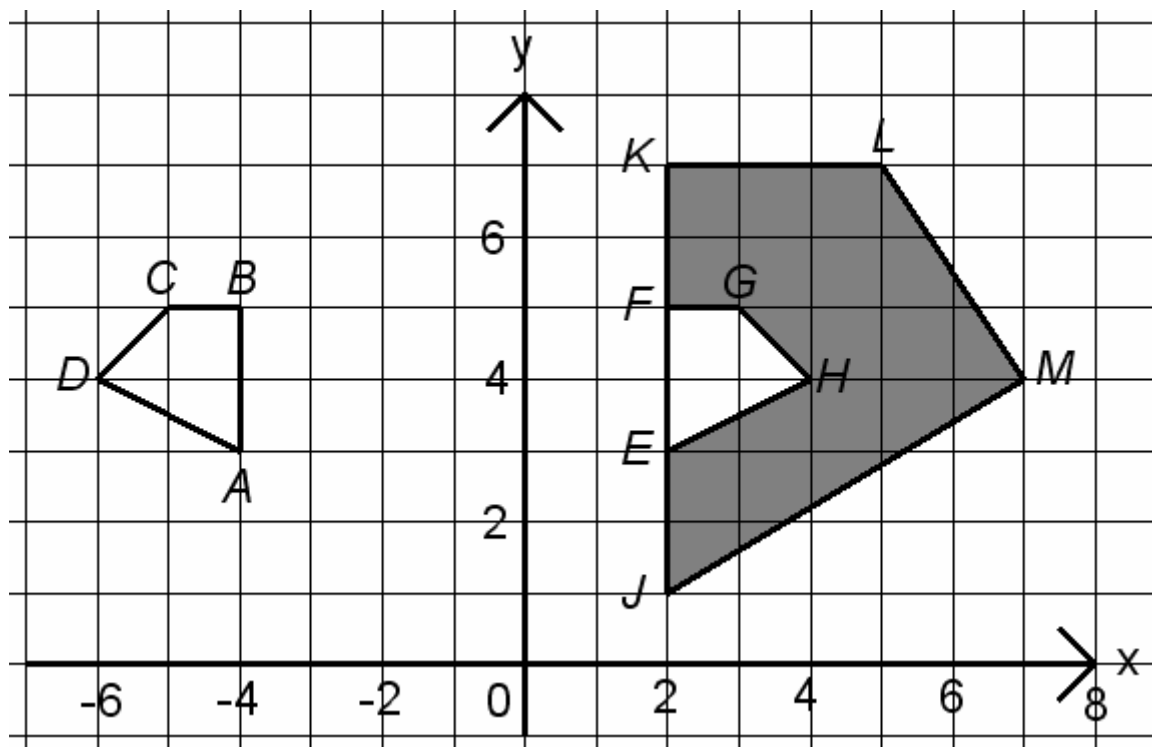


DIAGRAM 5

- i) *JKLM* is the image of *ABCD* under the combined transformation **VU**. Describe in full the transformations:
  - a. **U**,
  - b. **V**.
- ii) It is given that quadrilateral *ABCD* represents a region of area  $18 \text{ m}^2$ . Calculate the area, in  $\text{m}^2$ , of the region represented by the shaded region.

6. Diagram 6 shows quadrilaterals  $ABCD$ ,  $EFGH$  and  $JKLM$  drawn on a Cartesian plane.

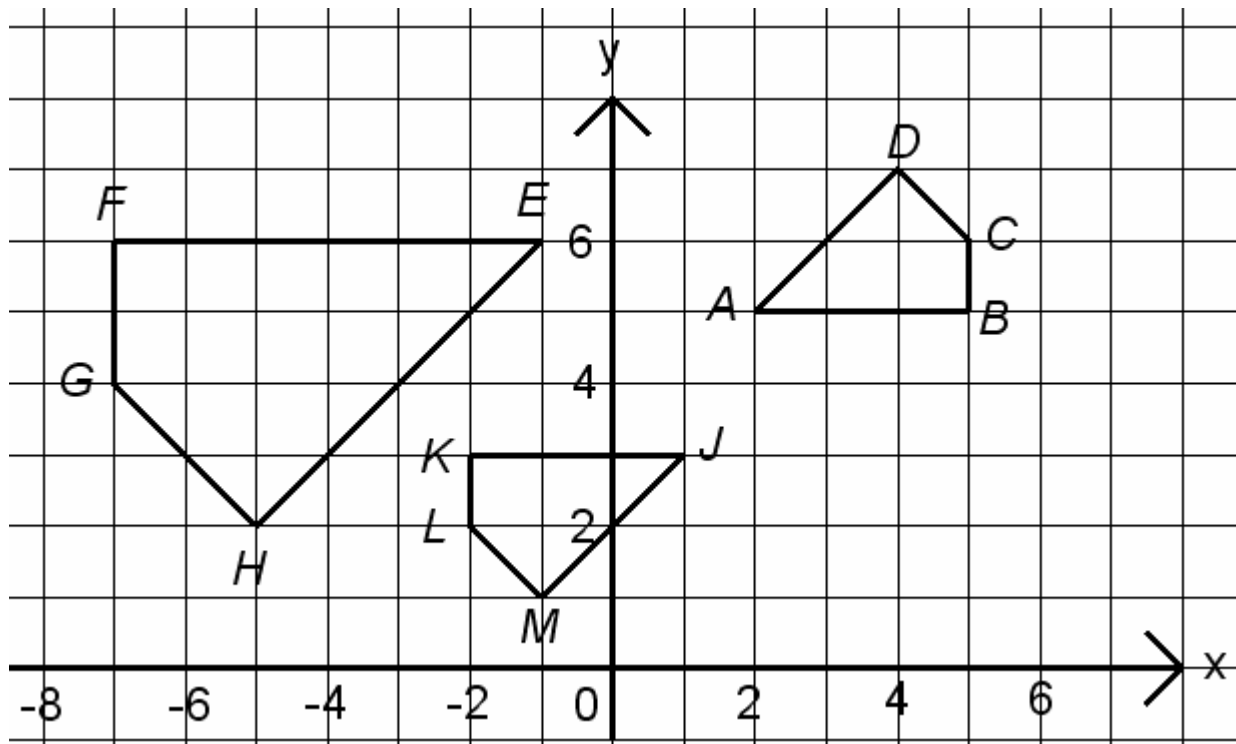


DIAGRAM 6

a) Transformation **R** is a rotation of  $90^\circ$  anticlockwise about the center  $(0, 2)$ .

Transformation **P** is a reflection in the straight line  $x = 2$ .

State the coordinates of the image of point  $A$  under each of the following transformations:

- i) **R**,
- ii) **RP**.

b)  $EFGH$  is the image of  $ABCD$  under the combined transformation **MN**.

Describe in full

- i) the transformation **M**,
- ii) the transformation **N**.

c)  $JKLM$  is the image of  $EFGH$  under an enlargement at centre  $(3, 0)$ .

- i) State the scale factor of the enlargement.
- ii) Given that  $EFGH$  represents a region of area  $112 \text{ m}^2$ , calculate the area, in  $\text{m}^2$ , of the region represented by  $JKLM$ .

7. a) Transformation **P** is a reflection in the line  $x = k$ .

Transformation **R** is a clockwise rotation of  $90^\circ$  about the centre  $(0, 4)$ .

Transformation **T** is a translation  $\begin{pmatrix} 5 \\ -3 \end{pmatrix}$ .

i) The point  $(8, 6)$  is the image of the point  $(-4, 6)$  under the transformation **P**.

State the value of  $k$ .

ii) Find the coordinates of the image of point  $(2, 8)$  under the following combined transformation:

a. **T**<sup>2</sup>,

b. **TR**.

c) Diagram 7 shows the three pentagons, *ABCDE*, *FGHIJ* and *KLMNJ*, drawn on a Cartesian plane.

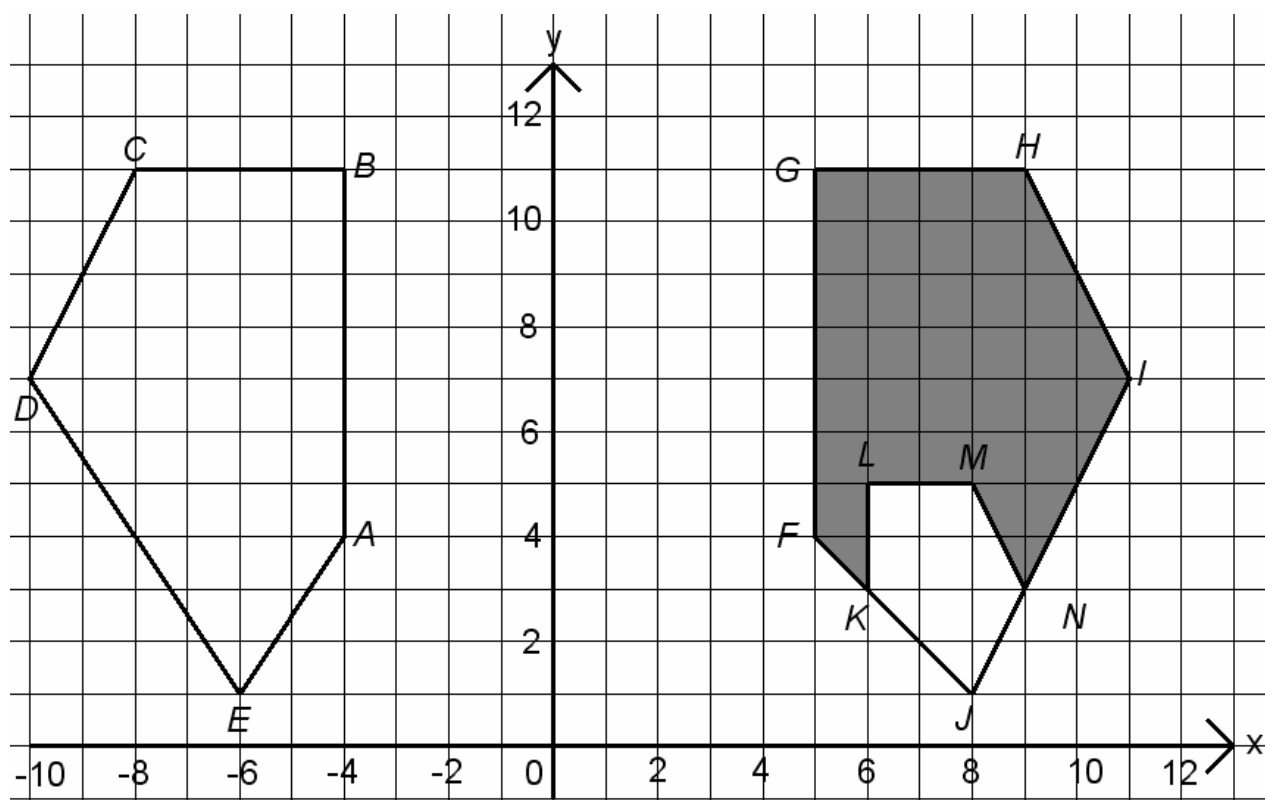


DIAGRAM 7

i) *KLMNJ* is the image of *ABCDE* under a combined transformation **VU**.

Describe in full the transformation

a) **U**,

b) **V**.

ii) It is given that pentagon *KLMNJ* represents a region of area  $42.5 \text{ m}^2$ .

Calculate the area, in  $\text{m}^2$ , of the region represented by the shaded region.