

Development Economics
City University, Spring 2007
Problem set 1

Harrod Domar and Solow

A) Assume that in a given country, the production function $f(\cdot)$ is such that output per capita, y , depends on the level of capital per capita, k , in the following way:

$$y = f(k) = k^\alpha$$

where $0 < \alpha < 1$.

- 1) if one additional unit of k is used, by how much does y increase?
- 2) Show that $f(\cdot)$ is a concave function.
- 3) Does the production function exhibit constant, diminishing, or increasing returns to per capita capital?
- 4) Explain in words what the type of returns to scale you've chosen at question 3 means.
- 5) What does this imply for the growth of y in the Solow model?

B) Now, let $\alpha = 1$, so that $y = f(k) = k$.

- 1) if one additional unit of k is used, by how much does y increase?
- 2) Does the production function exhibit constant, diminishing, or increasing returns to per capita capital?

C) « According to the Harrod Domar model, income per capita cannot grow without technological progress ». Is this statement true or false?

D) « According to the Solow model, government policies that encourage savings, by making more funds available for investment, boost growth ». Is this statement true or false?