

CALCULUS I – Worksheet #39

1. Find all absolute and relative maximums and minimums

for $y = 2x^3 - 3x^2 - 12x$ on $[-2,3]$

2. Find all critical points, inflection points, and sketch $y=x^4-4x^3$.

3. Find all intervals where $y = x^4 - 4x^3 + 4x^2$ is increasing and decreasing.

4. $f(x) = x^4 - 4x^2$ has: (A) 1 max, 2 min (B) 1 min, 2 max (C) 1 min, 1 max
(D) 2 max, 0 min (E) 2 min, 0 max

5. The number of inflection points of the curve in problem 4 is:
(A) 0 (B) 1 (C) 2 (D) 3 (E) 4

6. The total number of relative maximum and minimum points of the function whose derivative is $f'(x) = x^2(x+1)^3(x-4)^3$ is (A) 0 (B) 1 (C) 2 (D) 3 (E) 4

7. The sum of one number and twice another is 24. Find the two numbers so that their product is a maximum.

8. A square piece of tin has 12 inches on a side. An open box is formed by cutting out equal square pieces at the corners and bending upward the projecting portions which remain. Find the maximum volume that can be obtained.

9. Find all absolute and relative maximums and minimums for $y = x^3 - 3x + 1$ on $[-2,3]$.

10. Find the volume of the solid formed if the area bounded by $y = 4x - x^2$ and the x-axis is revolved around the y-axis.
