

## Calculus I – Worksheet #24

For Problems 1~ 4, find the area between the curves:

1.  $x = y^2 - 4$      $x = 4 - 2y$                       2.  $x = y^2$ ,  $y = 3x - 2$

2.  $y = x^3$      $y = x$                                       4.  $y = x^2 - 1$      $y = 3$

5. Approximate the area under  $y = 3x^2 + 2$  on  $[0, 4]$  using

- A) 4 rectangles whose height is given using the left endpoint
- B) 4 rectangles whose height is given using the right endpoint
- C) 4 rectangles whose height is given using the midpoint
- D) 4 trapezoids

6. A balloon is being filled with helium at the rate of  $4ft^3/\text{min}$ . The rate, in square feet per minute, at which the surface area is increasing when the volume is  $\frac{32p}{3} ft^3$  is

- A)  $4p$       B) 2      C) 4      D) 1      E)  $2p$

7. If  $c$  is the number defined by Rolle's theorem, then,  $f(x) = 2x^3 - 6x$  on  $[0, \sqrt{3}]$ ,  $c$  is

- A) 1      B) -1      C)  $\sqrt{2}$       D) 0      E)  $\sqrt{3}$

8. The average value of  $\cos x$  over the interval  $\frac{p}{3} \leq x \leq \frac{p}{2}$  is

- A)  $\frac{3}{p}$       B)  $\frac{1}{2}$       C)  $\frac{3(2-\sqrt{3})}{p}$       D)  $\frac{3}{2p}$       E)  $\frac{2}{3p}$

9. Let:  $f(x) = \frac{\sqrt{x+4} - 3}{x-5}$  if  $x \neq 5$  and let  $f$  be continuous at  $x = 5$ , Then  $c = ?$

$f(5) = c$

- A)  $\frac{-1}{6}$       B) 0      C)  $\frac{1}{6}$       D) 1      E) 6

10. Find the average value of  $x^2 - 1$  on  $[0, \sqrt{3}]$

11. Find the average value of  $f(x) = \frac{-x^2}{2}$  on  $[0, 3]$

12. Find the average value of  $f(x) = -3x^2 - 1$  on  $[0, 1]$