

Solutions for Homework #6

Section 5.1: 34, 35, 36, 37, 41, 42, 43, 44, 53, 54

#34 In this problem, the sample space (outcome space) S consists of the 365 days of the year, all equally likely. All you have to do in each part is to apply $P(E) = \frac{N(E)}{N(S)}$, with

$N(S)$ being 365. (Note: In reality, it is not quite true that all 365 days are equally likely. But that is the assumption we are asked to base our computation on in this exercise.)

- (a) $\frac{12}{365}$. This means that if you randomly pick a person from the population, and do so a large number of times, then in the long run it is expected that in roughly $12/365$ of the cases the person has a birthday on the first day of a month (Jan 1, Feb 1, ..., Dec 1).
- (b) $\frac{7}{365}$. (The interpretation is similar to that in (a). Note that the 7 comes from the fact that only Jan, Mar, May, Jun, Jul, Oct, Dec have the 31st day.)
- (c) $\frac{31}{365}$ (Again, you give the interpretation, similar to (a)).
- (d) $\frac{1}{365}$ (You give the interpretation.)
- (e) No. (The probability that you hit on the right answer is only $1/365$, which is lower than the usual cutoff of 0.05 for “unusual” events.)
- (f) No!!! The key is that the 365 days are, in reality, not equally likely. It is known that some portions of the year somehow are more popular.

#35 (a) {SS, Ss, sS, ss} (b) $\frac{1}{4}$. (c) This means the probability of Ss or sS, so $\frac{2}{4}$, i.e. $\frac{1}{2}$.

#36 (a) {SS, Ss, sS, ss} (b) $\frac{1}{4}$. (c) $\frac{3}{4}$

#37

(a)

| | | Probability |
|------------------|------|-------------|
| Never | 125 | 0.0261725 |
| Rarely | 324 | 0.0678392 |
| Sometimes | 552 | 0.1155779 |
| Most of the time | 1257 | 0.2631910 |
| Always | 2518 | 0.5272194 |
| sum | 4776 | 1.0000000 |

(b) Yes. That probability is 0.026, which is lower than the usual cutoff of 0.05 for “unusual” events.

#41 A, B, C, F

#42 A

#43 B

#44 F

#53 Answer: 0.5. This is because, by the very definition of the median, 50% of the population has an income greater than the median income.

#54 Answer: 0.17

Section 5.2: 27, 29, 30, 31, 37, 39

#27 First, let's work out the sum of the second column:

(a) $\frac{2832 + 1843}{7401} = \frac{4675}{7401} \approx 0.632$

(b) $1 - 0.632 = 0.368$

(c) $P(\text{less than 45 years old}) = 1 - P(\text{45 years old or older})$

$= 1 - \frac{117}{7401} \approx 1 - 0.016 = 0.984$

(d) $P(\text{at least 20 years old}) = 1 - P(\text{younger than 20 years old})$

$= 1 - \frac{93}{7401} \approx 1 - 0.013 = 0.987$

| Age | | Number of Multiple Births |
|------|----|---------------------------|
| 15 - | 19 | 93 |
| 20 - | 24 | 511 |
| 25 - | 29 | 1628 |
| 30 - | 34 | 2832 |
| 35 - | 39 | 1843 |
| 40 - | 44 | 377 |
| 45 - | 54 | 117 |
| sum | | 7401 |

#29 (a) $\frac{13+13}{52} = \frac{1}{2}$ (b) $\frac{13+13+13}{52} = \frac{3}{4}$ (c) $\frac{4+13-1}{52} = \frac{16}{52} = \frac{4}{13}$

#30 (a) $\frac{4+4}{52} = \frac{8}{52} = \frac{2}{13}$ (b) $\frac{4+4+4}{52} = \frac{12}{52} = \frac{3}{13}$ (c) $\frac{4+13-1}{52} = \frac{16}{52} = \frac{4}{13}$

#31

(a) $1 - P(\text{Nov. 8}) = 1 - \frac{1}{365} = \frac{364}{365}$

(b) $1 - P(\text{1st day of a month}) = 1 - \frac{12}{365} = \frac{353}{365}$

(c) $1 - P(\text{31st day of a month}) = 1 - \frac{7}{365} = \frac{358}{365}$

(d) $1 - P(\text{December}) = 1 - \frac{31}{365} = \frac{334}{365}$

#37

(a) $\frac{1014}{137244} \approx 0.007$

(b) $\frac{7866}{137244} \approx 0.057$

(c) $\frac{141}{137244} \approx 0.001$

(d) $\frac{782 + 91 + 141 + 7725}{137244} = \frac{8739}{137244} \approx 0.064$

| | Died from cancer | Did not die from cancer | |
|----------------------|------------------|-------------------------|---------|
| Never smoke cigars | 782 | 120,747 | 121,529 |
| Former cigar smoker | 91 | 7,757 | 7,848 |
| Current cigar smoker | 141 | 7,725 | 7,866 |
| | 1,014 | 136,229 | 137,243 |

Of course, this is the same as $\frac{1014}{137244} + \frac{7866}{137244} - \frac{141}{137244} = \frac{8739}{137244} \approx 0.064$

#39

(a) $\frac{231}{375} \approx 0.616$ (b) $\frac{94}{375} \approx 0.251$ (c) $\frac{64}{375} \approx 0.171$

(d) $\frac{231}{375} + \frac{94}{375} - \frac{64}{375} = \frac{261}{375} \approx 0.696$ or, simply

$\frac{57 + 49 + 64 + 61 + 16 + 14}{375} = \frac{231 + 16 + 14}{375} = \frac{261}{375} \approx 0.696$