



An ordered sequence of 4 decorated  $n$ -gons defines a simplex of dimension 3, in the barycentric subdivision of the real moduli. To decorate, or to label an  $n$ -gon means to add a couple of diagonals and to attach numbers on every edge.