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# **Fuzzy Fault Currents: Theory and Applications**

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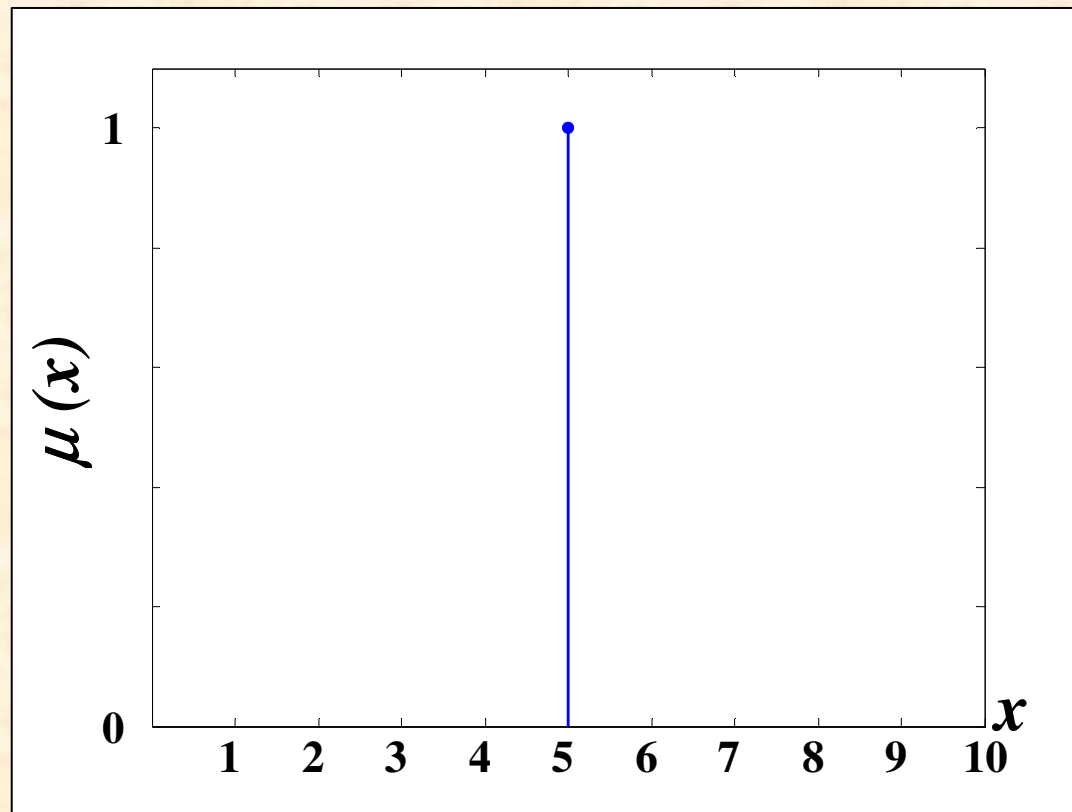
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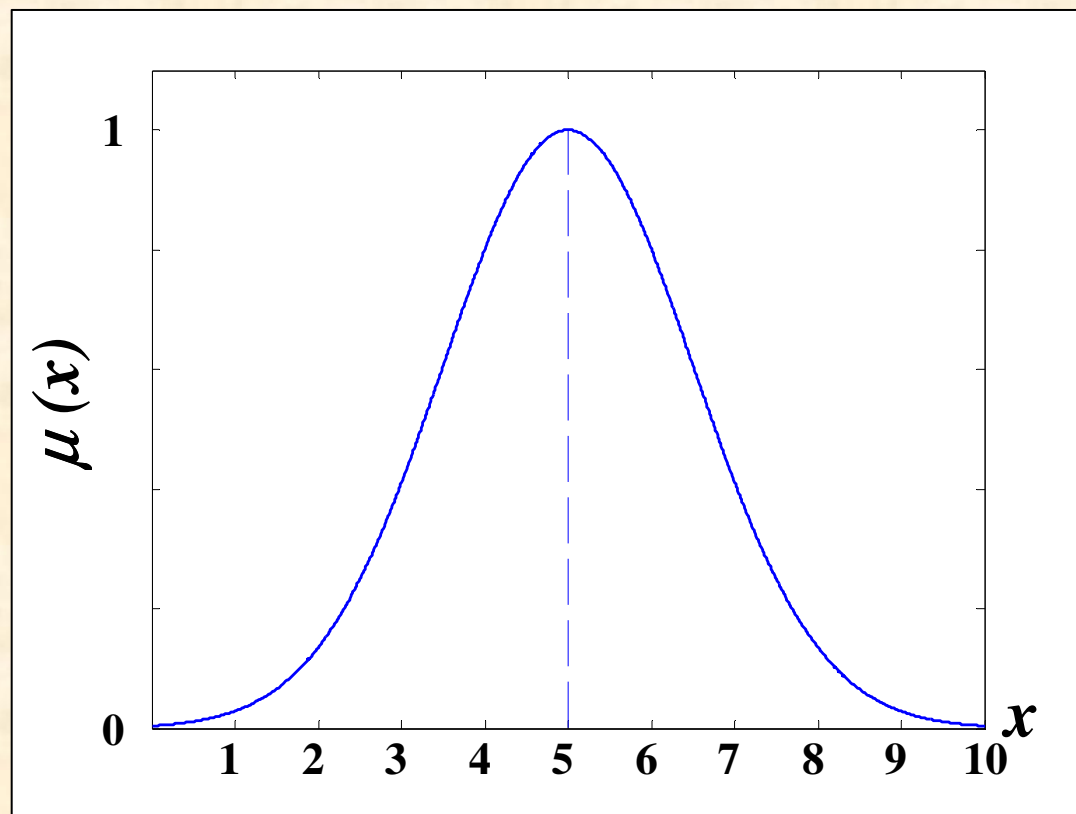
# CRISP NUMBER

$$\mu_A(x) = \begin{cases} 1 & \text{if } x \in A \\ 0 & \text{if } x \notin A \end{cases}$$



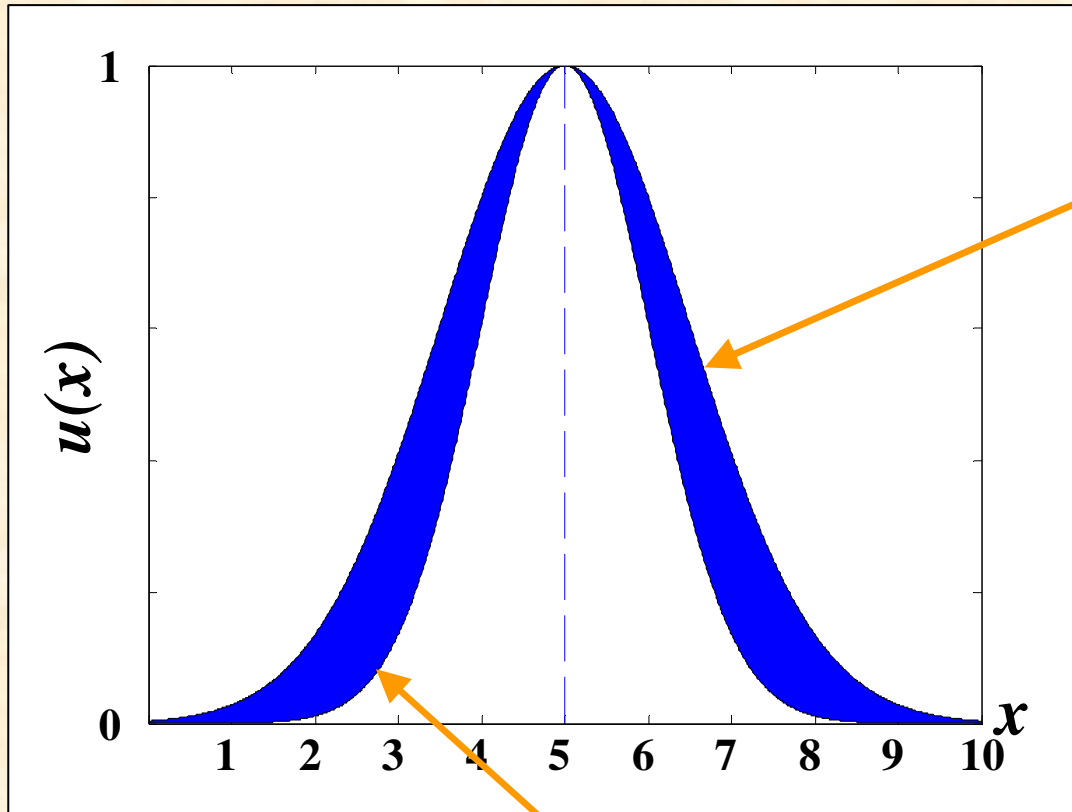
# TYPE-1 FUZZY NUMBER

$$A = \int_{x \in X} \frac{\mu_A(x)}{x}$$



# TYPE-2 FUZZY NUMBER

Upper membership function



$$\bar{\mu}_A(x)$$

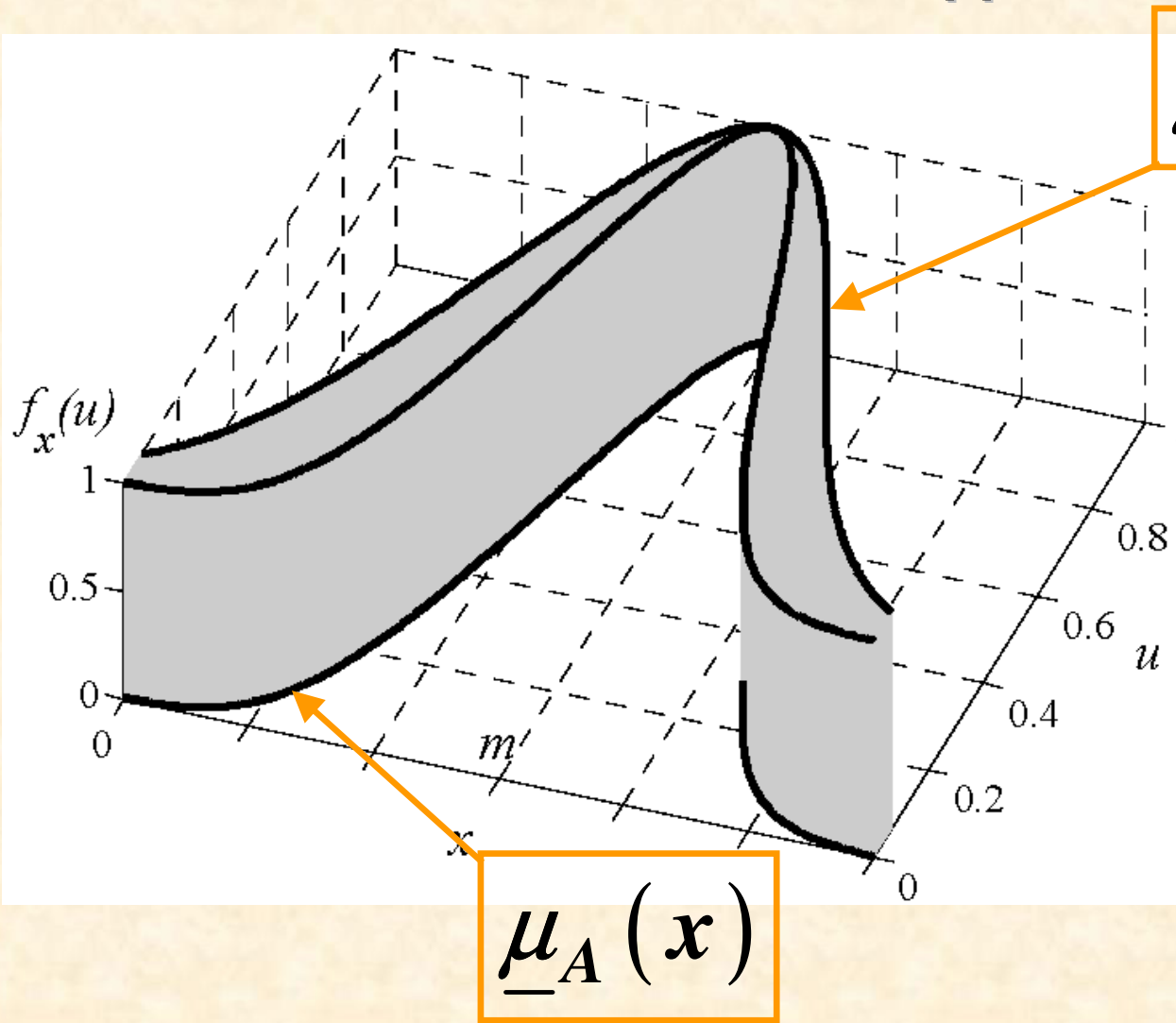
$$\tilde{A} = \int_{x \in X} \frac{\mu_{\tilde{A}}(x)}{x}$$

$$\underline{\mu}_A(x)$$

Lower membership function

# INTERVAL TYPE-2 FUZZY NUMBER

Upper membership function

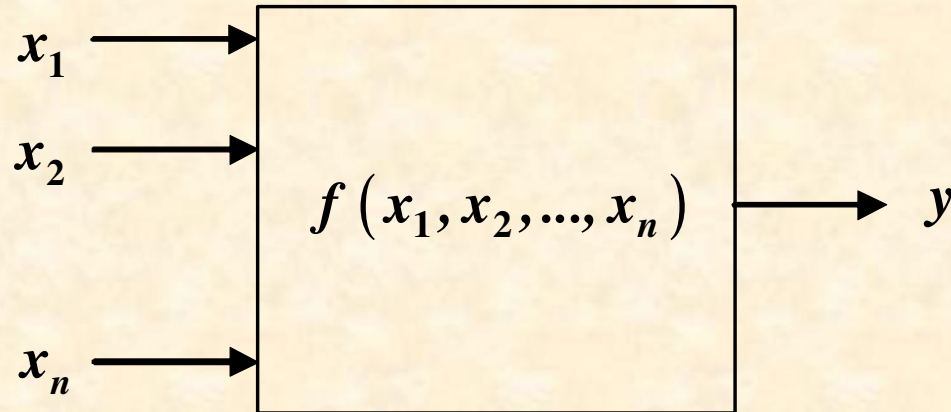


$$\tilde{A} = \int_{x \in X} \frac{\mu_{\tilde{A}}(x)}{x}$$

Lower membership function

# FUZZY EXTENSION PRINCIPLE

Mathematical tool for calculating functions of fuzzy variables



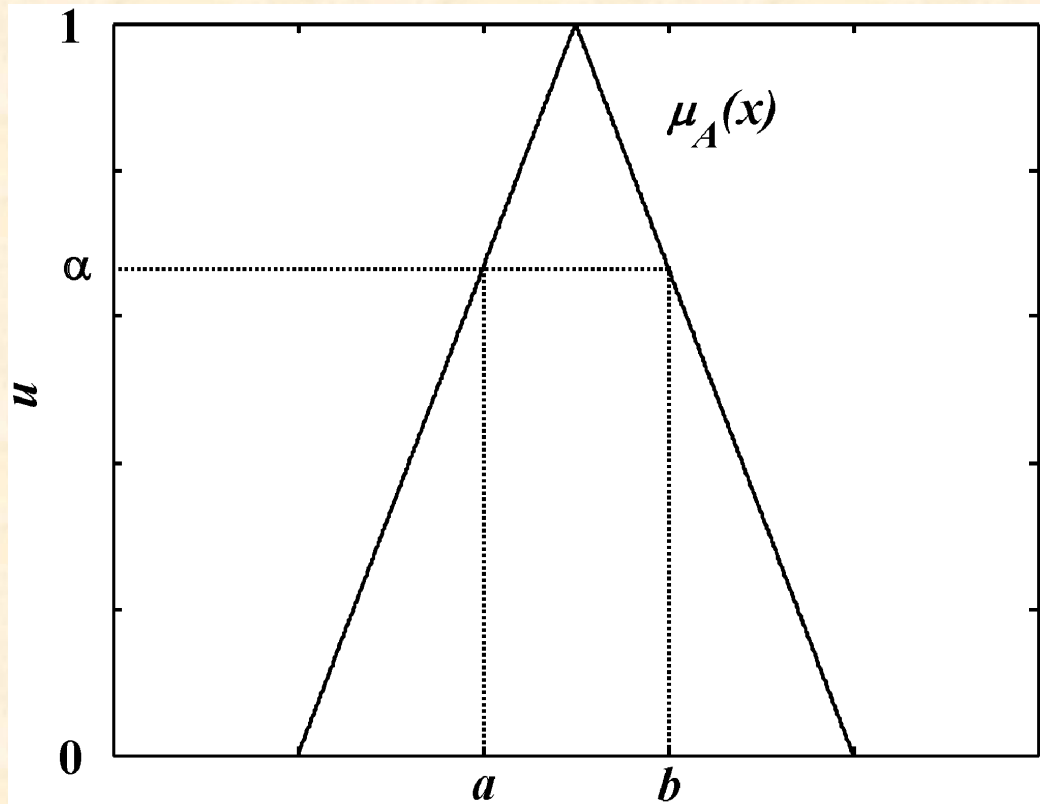
**For type-1 fuzzy numbers:**

The fuzzy extension principle is implemented by using the vertex method

**For interval type-2 fuzzy numbers:**

The fuzzy extension principle is implemented by using the vertex method and performing calculations only with the upper and lower membership functions

# VERTEX METHOD



$$r = 2$$

$$c_1 = (a_1, b_1)$$

$$c_2 = (a_1, b_2)$$

$$c_3 = (a_2, b_1)$$

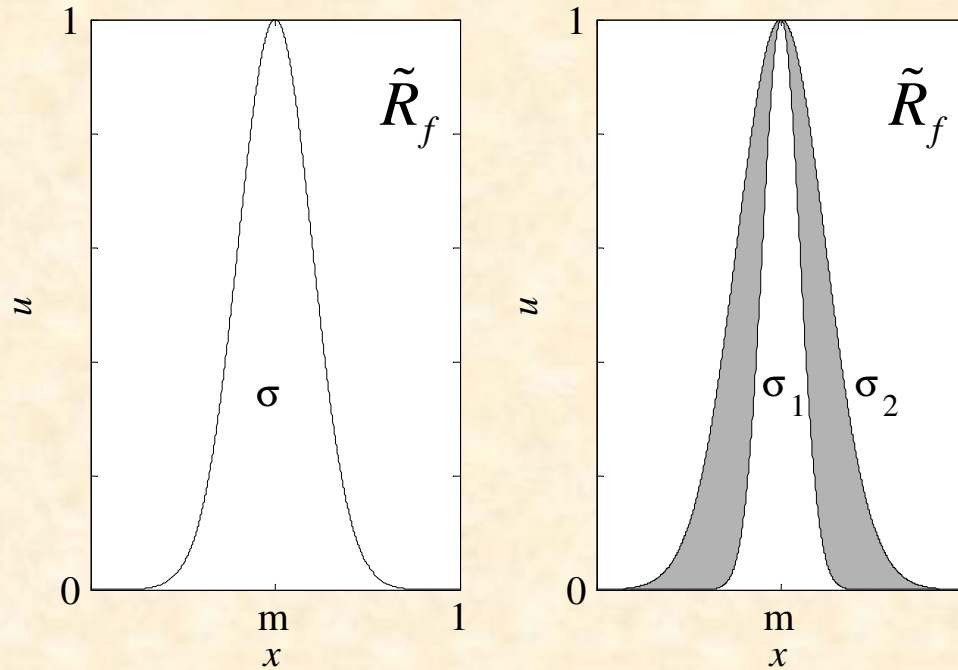
$$c_4 = (a_2, b_2)$$

$$I_{i\alpha} = [a_i, b_i], \quad i = 1, 2, \dots, r \quad N = 2^r, \quad j = 1, 2, \dots, N$$

$$B_\alpha = f(I_{1\alpha}, I_{2\alpha}, \dots, I_{r\alpha}) = \left[ \min_j (f(c_j)), \max_j (f(c_j)) \right]$$

# FUZZY FAULT CURRENTS (FFC)

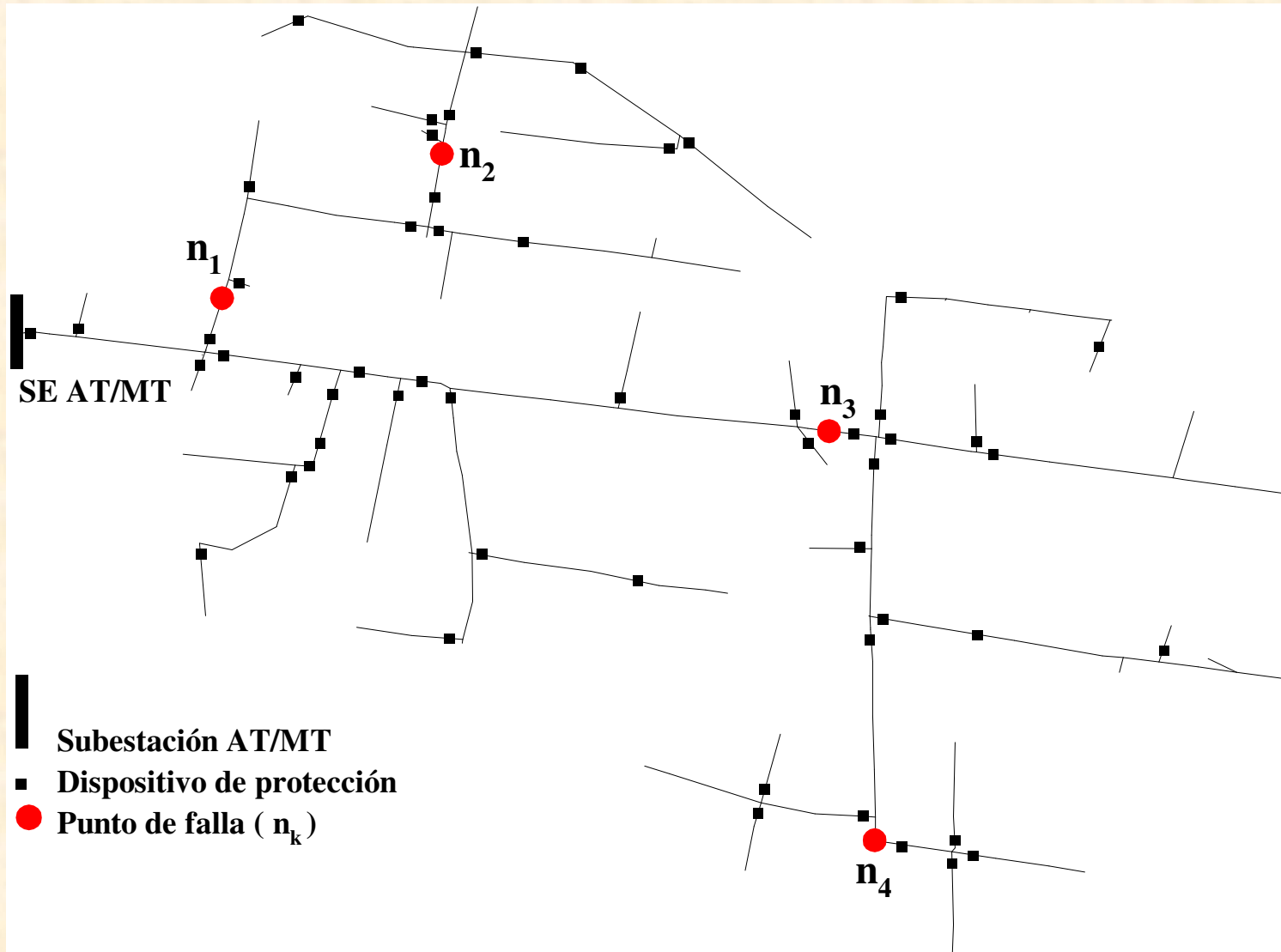
$R_f$  and  $U_{pf}$  are modelled as type-1 or interval type-2 fuzzy numbers



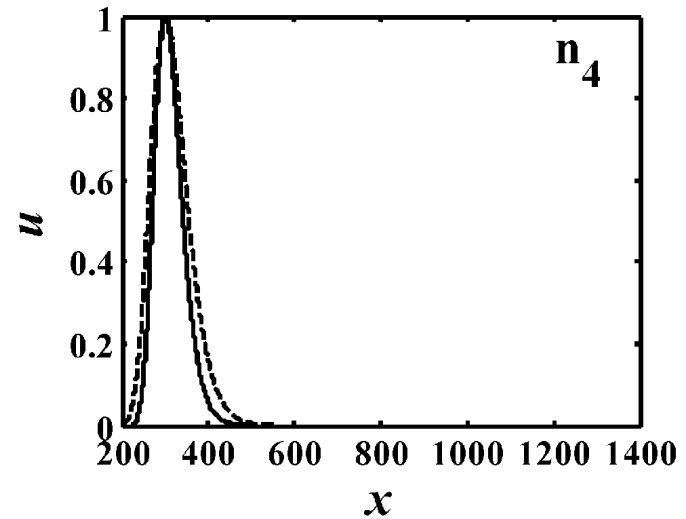
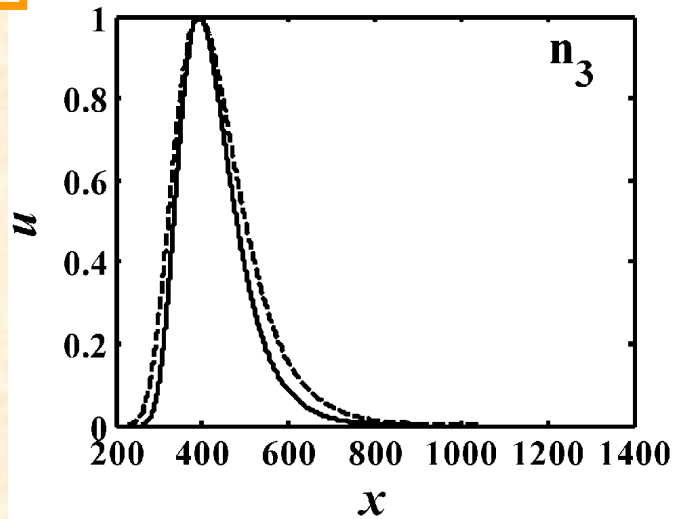
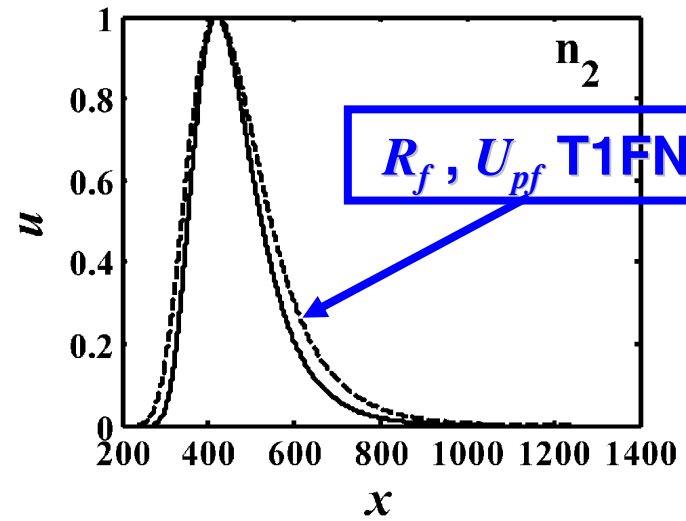
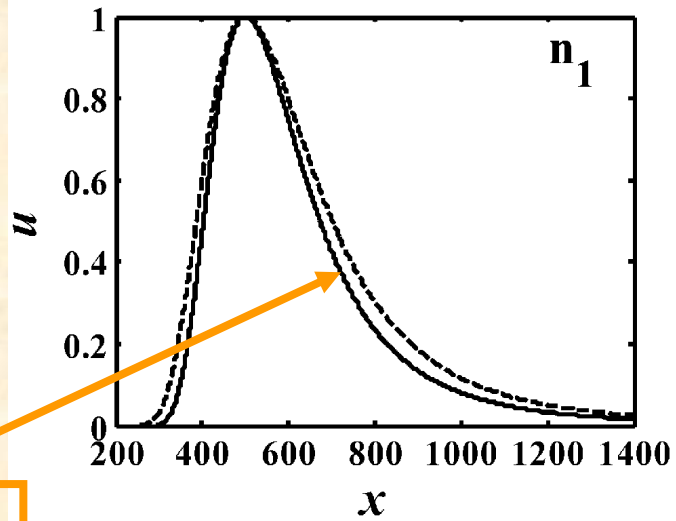
Then the fuzzy extension principle and vertex method are used to calculate fault currents using classical fault equations

$$I_{fk} = 3U_{pfk} / \sqrt{\left(2R_k^+ + R_k^0 + 3R_f\right)^2 + \left(2X_k^+ + X_k^0\right)^2}$$

# RESULTS



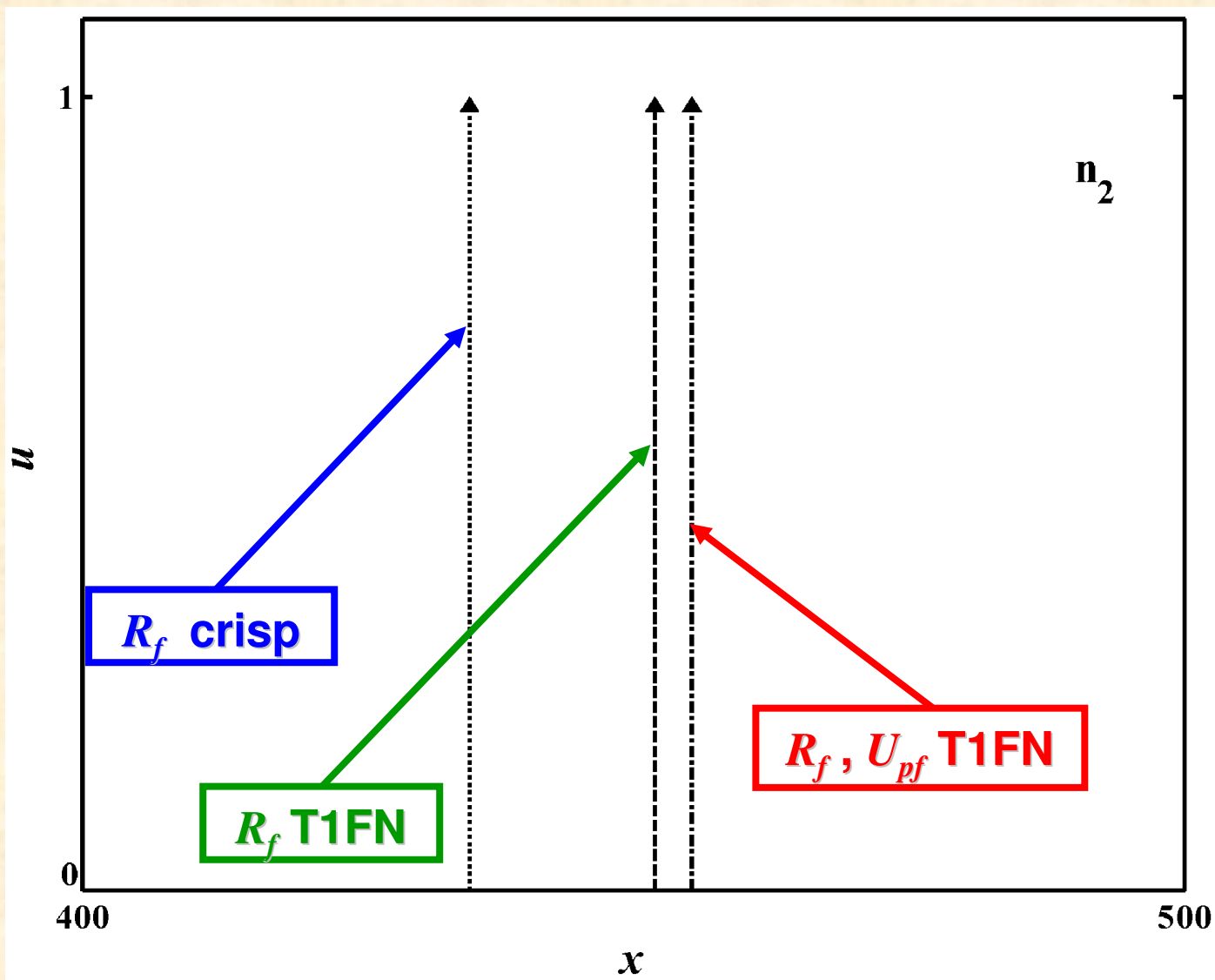
# TYPE-1 FUZZY FAULT CURRENTS



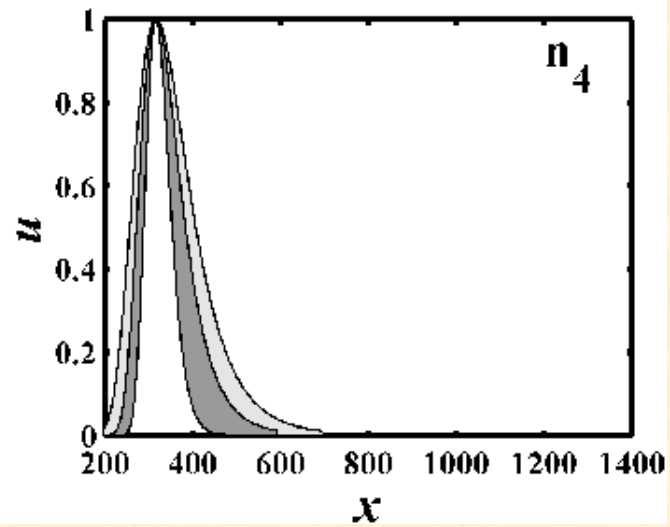
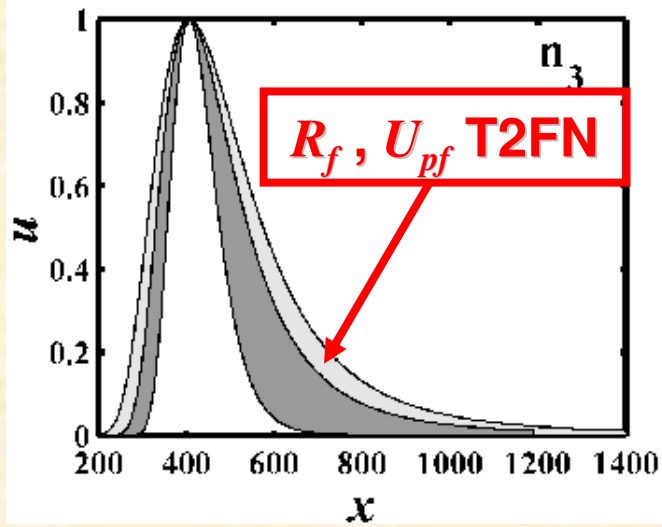
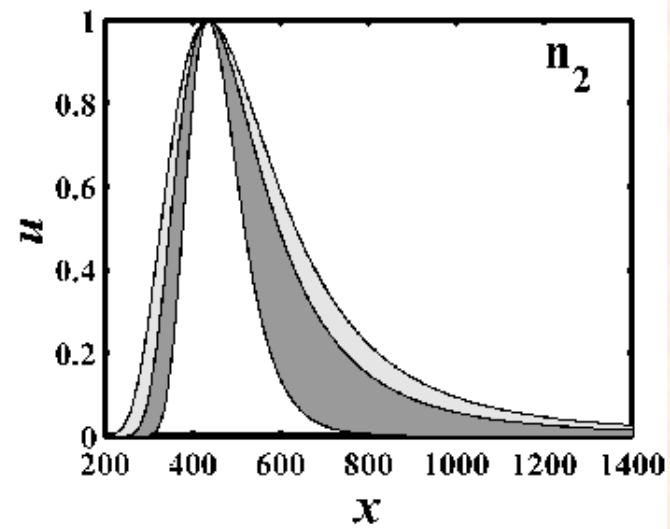
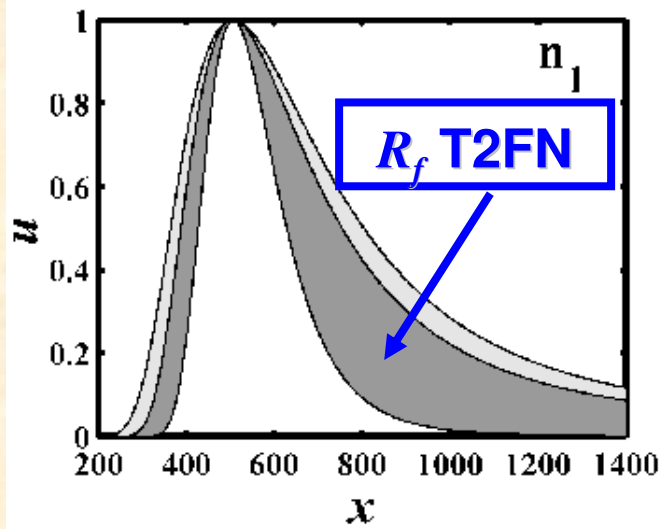
$R_f$  T1FN

$R_f, U_{pf}$  T1FN

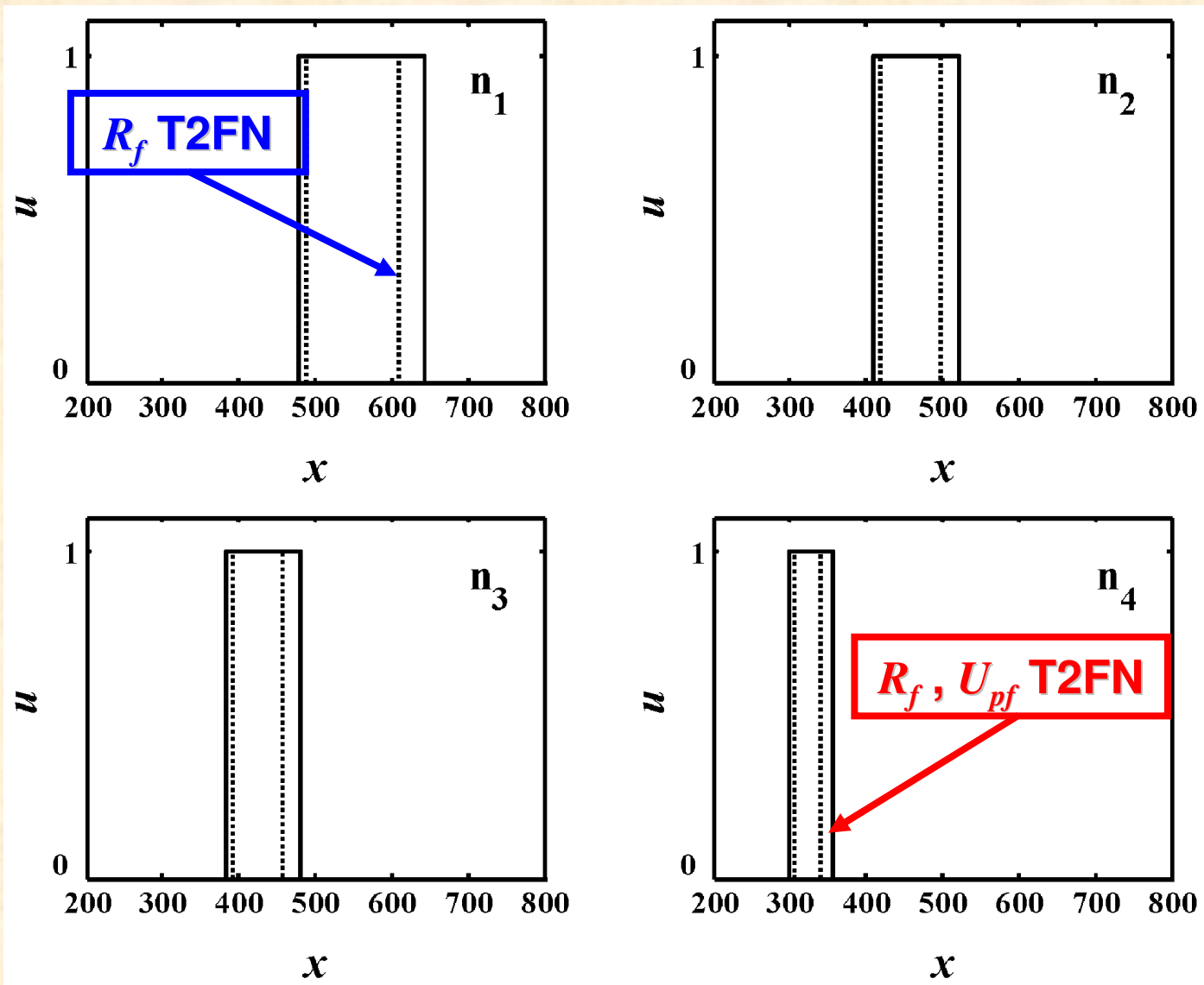
## DEFUZZIFIED VALUES (TYPE-1 FFC)



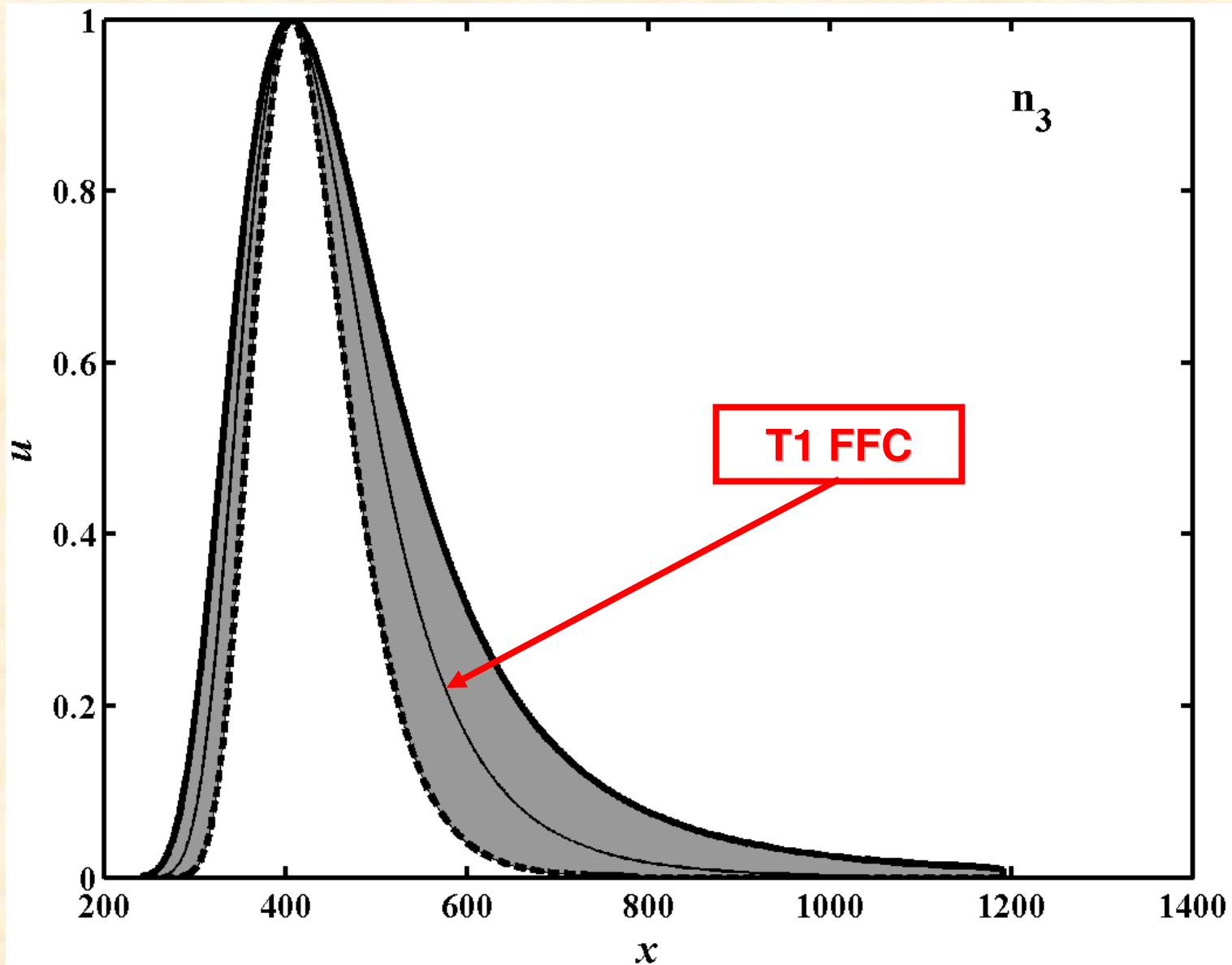
# TYPE-2 FUZZY FAULT CURRENTS



# CENTROIDS (TYPE-2 FFC)



# COMPARISON BETWEEN TYPE-1 AND TYPE-2 FFC



# COMPARISON BETWEEN CRISP, TYPE-1 AND TYPE-2 FFC

