

SIIT MAS210 First Semester 2006 - Quiz 4 - Dr. Ruben

Each correct answer is 25 points. Each wrong answer is -6 points

Problem 1. Given the functions $f(z) = e^z$ and $g(z) = \operatorname{Re} z$, which of the following is true?

- (1) $f(z)$ is analytic at all complex points z and $g(z)$ is not analytic at any complex point z
- (2) $f(z)$ is not analytic and $g(z)$ is analytic at all complex points z
- (3) both $f(z)$ and $g(z)$ are analytic at all complex points z
- (4) neither $f(z)$ nor $g(z)$ are analytic at all complex points z
- (5) $f(z)$ is analytic only inside the circle $z = e^{it}$, $0 < t < 2\pi$ and $g(z)$ is analytic on the complex plane

Problem 2. If $z = \sqrt{2} + i\sqrt{2}$ then $\ln z =$

- (1) $\ln z = \ln \sqrt{2} + i\sqrt{2}$
- (2) $\ln z = \frac{1}{2} + i\pi$
- (3) $\ln z = \ln 2 + i\pi/4$
- (4) $\ln z = \ln(\sqrt{3}/2) + i$
- (5) $\ln z = e^2 + 2i$

Problem 3. Let $z = 1 - (\pi/2)i$. Then $e^z =$

- (1) $e^z = e^1 - e^i$
- (2) $e^z = e^{1-i}$
- (2) $e^z = e(\cos 1 - i \sin 1)$
- (3) $e^z = -ie$
- (4) $e^z = \sqrt{2}(\cos 1 - \sin(\pi/4))$
- (5) $e^z = \ln(1 - i)$

Problem 4. Let $f(z) = ze^{-z}$. Then $f'(-i) =$

- (1) $f'(-i) = e^i(1 + i)$
- (2) $f'(-i) = 1 + e^{-i}$
- (2) $f'(-i) = \cos(\pi/2) + i \sin(\pi/2)$
- (3) $f'(-i) = -ie^i$
- (4) $f'(-i) = \ln(i) + i \arg(\pi/4)$
- (5) $f'(-i) = e^{-1}$