

**Additional Practice****Investigation 1****Samples and Populations**

Another peanut butter survey was conducted more recently than the survey you studied in Investigation 1. The data for natural and regular brands are presented in the table.

**Peanut Butter Comparisons**

Brand	Quality Rating	Sodium per Serving (mg)	Price per Serving	Regular/Natural	Creamy/Chunky	Name Brand/Store Brand
Arrowhead Mills	85	0	36	natural	creamy	name
Laura Scudder's (Southeast)	79	165	25	natural	creamy	name
Adams (West)	73	173	23	natural	creamy	name
Smucker's	73	180	26	natural	creamy	name
Nature's Cupboard (Safeway)	68	240	26	natural	creamy	store
Laura Scudder's Nutty (Southeast)	84	165	26	natural	chunky	name
Arrowhead Mills	83	0	37	natural	chunky	name
Smucker's	79	180	26	natural	chunky	name
Adams (West)	75	135	23	natural	chunky	name
Nature's Cupboard (Safeway)	72	195	26	natural	chunky	store
Jif	85	225	19	regular	creamy	name
Simply Jif	85	98	19	regular	creamy	name
Peter Pan	82	225	17	regular	creamy	name
Skippy	82	225	18	regular	creamy	name
Kroger	79	195	15	regular	creamy	store
Skippy Roasted Honey Nut	79	180	19	regular	creamy	name
America's Choice	77	225	17	regular	creamy	store
Reese's	68	173	19	regular	creamy	name
Townhouse (Safeway)	68	240	18	regular	creamy	store
Peter Pan Very Low Sodium	57	15	18	regular	creamy	name
Peter Pan Whipped	49	173	17	regular	creamy	name
Jif Extra Crunchy	88	195	19	regular	chunky	name
Skippy Super Chunk	87	210	19	regular	chunky	name
Peter Pan Extra Crunchy	86	180	17	regular	chunky	name
Reese's	86	120	19	regular	chunky	name
Skippy Roasted Honey Nut	86	180	19	regular	chunky	name
Kroger	84	195	15	regular	chunky	store
Simply Jif Extra Crunchy	83	75	19	regular	chunky	name
America's Choice Krunchy	80	188	17	regular	chunky	store
Townhouse (Safeway)	72	195	18	regular	chunky	store

Source: "Peanut Butter: It's Not Just for Kids Anymore." *Consumer Reports* (September 1995): pp. 576–579.

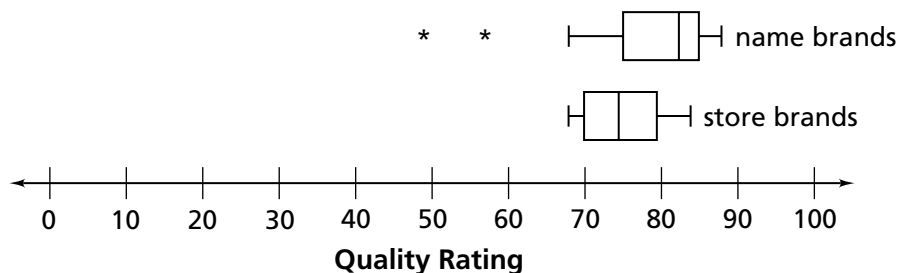
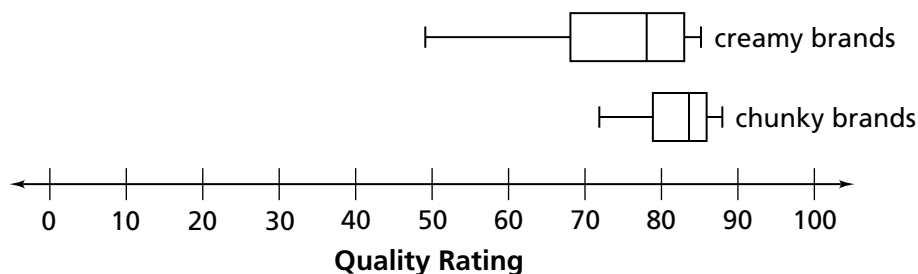
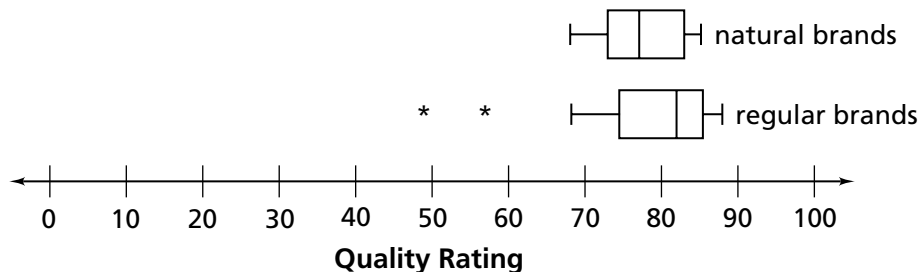
## Additional Practice *(continued)*

### Investigation 1

#### Samples and Populations

1. The box plots below show the quality ratings of natural versus regular brands, creamy versus chunky brands, and name brands versus store brands. Based on these box plots, what characteristics would you look for if you wanted to choose a peanut butter based on quality rating? Explain your reasoning.

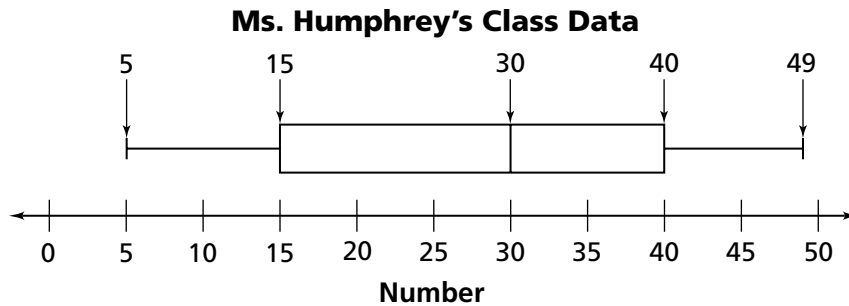
#### Quality Comparisons



2. Make box plots to compare the peanut butters based on price. Mark any outliers with an asterisk (\*). Which characteristic(s) help identify low-price peanut butters? Explain your reasoning.

**Additional Practice** *(continued)***Investigation 1****Samples and Populations**

Ms. Humphrey asked each of the 21 students in her class to choose a number between 1 and 50. Ms. Humphrey recorded the data and made this box plot:



3. What is the median number that was chosen?
4. What percent of students in Ms. Humphrey's class chose numbers above 15? Explain your reasoning.
5. About how many students chose numbers between 30 and 40? Explain.
6. What were the least and the greatest numbers chosen?
7. Is it possible to determine from the box plot whether one of the students chose the number 27? Explain.
8. Is it possible to determine from the box plot whether one of the students chose the number 4? Explain.

**Additional Practice** *(continued)***Investigation 1****Samples and Populations**

For Exercises 9–12, refer to the table on the next page.

9. Finish computing the values for the fifth column.
10. What does it mean when the ratio of wingspan to body length is 1? Greater than 1? Less than 1?
11. Compute the five-number summary for jet planes and the five-number summary for propeller planes of the ratio of wingspan to body length. Explain what the medians tell you about the relationship between wingspan and body length for jet planes and for propeller planes.
12. Make box plots from your five-number summaries. Explain what your plots reveal about how jet planes and propeller planes compare based on ratio of wingspan to body length.

**Additional Practice** *(continued)***Investigation 1****Samples and Populations****Airplane Data**

Plane	Engine Type	Body Length (m)	Wingspan (m)	Wingspan-to-Length Ratio
Boeing 707	jet	46.6	44.4	0.953
Boeing 747	jet	70.7	59.6	0.843
Ilyushin IL-86	jet	59.5	48.1	
McDonnell Douglas DC-8	jet	57.1	45.2	
Antonov An-124	jet	69.1	73.3	
British Aerospace 146	jet	28.6	26.3	
Lockheed C-5 Galaxy	jet	75.5	67.9	
Antonov An-225	jet	84.0	88.4	
Airbus A300	jet	54.1	44.9	
Airbus A310	jet	46.0	43.9	
Airbus A320	jet	37.5	33.9	
Boeing 737	jet	33.4	28.9	
Boeing 757	jet	47.3	38.1	
Boeing 767	jet	48.5	47.6	
Lockheed Tristar L-1011	jet	54.2	47.3	
McDonnell Douglas DC-10	jet	55.5	50.4	
Aero/Boeing Spacelines Guppy	propeller	43.8	47.6	
Douglas DC-4 C-54 Skymaster	propeller	28.6	35.8	
Douglas DC-6	propeller	32.2	35.8	
Lockheed L-188 Electra	propeller	31.8	30.2	
Vickers Viscount	propeller	26.1	28.6	
Antonov An-12	propeller	33.1	38.0	
de Havilland DHC Dash-7	propeller	24.5	28.4	
Lockheed C-130 Hercules/L-100	propeller	34.4	40.4	
British Aerospace 748/ATP	propeller	26.0	30.6	
Convair 240	propeller	24.1	32.1	
Curtiss C-46 Commando	propeller	23.3	32.9	
Douglas DC-3	propeller	19.7	29.0	
Grumman Gulfstream I/I-C	propeller	19.4	23.9	
Ilyushin IL-14	propeller	22.3	31.7	
Martin 4-0-4	propeller	22.8	28.4	
Saab 340	propeller	19.7	21.4	

Source: William Berk and Frank Berk. *Airport Airplanes*. Plymouth, Mich.: Plymouth Press, 1993.

# Skill: Histograms

## Investigation 1

### Samples and Populations

1. Would the data below be better displayed on a histogram with 3-minute intervals or 5-minute intervals? Explain.

Time to Walk to School															
Time (min.)	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
Tally															

2. Make a histogram for the time it takes the group of students in Exercise 1 to walk to school.

3. Make a histogram for the data. Use the intervals in the table.

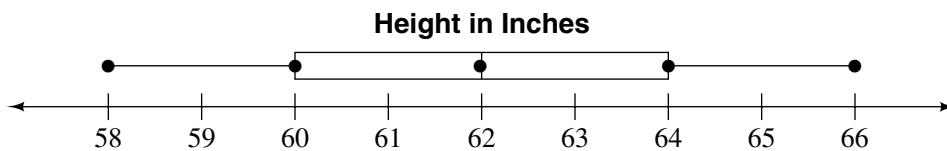
Hours Spent Doing Homework	
Number of Hours	Frequency
1 – 1.75	1
2 – 2.75	1
3 – 3.75	2
4 – 4.75	6
5 – 5.75	8
6 – 6.75	3
7 – 7.75	2
8 – 8.75	1

## Skill: Box-and-Whisker Plots

### Investigation 1

#### Samples and Populations

Use the box-and-whisker plot to find each value.



1. the median height
  
2. the lower quartile
  
3. the upper quartile
  
4. the greatest height
  
5. the shortest height
  
6. the range of heights

**Skill: Box-and-Whisker Plots** *(continued)*

**Investigation 1**

**Samples and Populations**

Make a box-and-whisker plot for each set of data.

7. **Cargo Airlines in the U.S. (1991)**

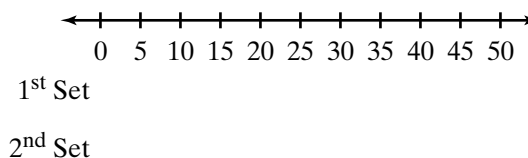
Airline	Freight ton-miles (1,000,000s)
Federal Express	3,622
Northwest	1,684
United	1,214
American	884
Delta	668
Continental	564
Pan American	377
Trans World	369
United Parcel Service	210

8. **Immigration to the U.S. (1981–1990)**

Country	Number (1,000s)
Mexico	1,656
Philippines	549
China	347
Korea	334
Vietnam	281
Dominican Republic	252
India	251
El Salvador	214
Jamaica	208
United Kingdom	159

Use box-and-whisker plots to compare data sets. Use a single number line for each comparison.

9. 1st set: 7 12 25 3 1 29 30 7 15 2 5  
 10 29 1 10 30 18 8 7 29
- 2nd set: 37 17 14 43 27 19 32 1 8 48  
 26 16 28 6 25 18





**Additional Practice****Investigation 2****Samples and Populations**

**Aaron wants to learn about how much time students at his school spend playing sports. He asks all the boys on the basketball team and all the girls on the volleyball team to estimate how many hours per week they spend playing sports.**

1. Is Aaron's sample a voluntary-response sample, a systematic sample, or a convenience sample? Explain your reasoning.
  
  
  
  
  
  
  
  
  
  
2. Suppose Aaron asked all the students in his mathematics class to estimate how many hours per week they spend playing sports.
  - a. Would this be a voluntary-response sample, a systematic sample, or a convenience sample? Explain your reasoning.
  
  
  
  
  
  
  
  
  
  
  - b. Would you expect the median number of hours spent playing sports for students in Aaron's mathematics class to be higher or lower than his sample from the basketball and volleyball teams? Explain your reasoning.
  
  
  
  
  
  
  
  
  
  
3. There are 1,232 students enrolled at Aaron's school. The principal's office has an alphabetical list of all the students' names. Suppose Aaron asked every 20th student on the list to estimate the number of hours he or she spends playing sports each week. Would this be a voluntary-response sample, a systematic sample, or a convenience sample? Explain.
  
  
  
  
  
  
  
  
  
  
4. Aaron placed an ad in the school newspaper with a form for students to complete and return. The form asked how much time the students spent playing sports each week. Aaron received 53 responses. Is this a voluntary-response sample, a systematic sample, or a convenience sample? Explain.

**Additional Practice** *(continued)***Investigation 2****Samples and Populations**

**For Exercises 5–7, use this information: Marci works on the yearbook staff at Metropolis Middle School. Of the 92 businesses in the downtown area, 41 purchased advertising space in the yearbook last year.**

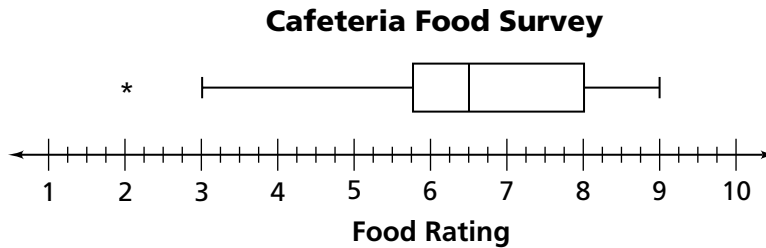
5. Suppose Marci wants to investigate why businesses did not advertise in the yearbook last year. Describe a sampling strategy she could use to call 10 businesses.
  
  
  
  
  
  
  
  
  
  
6. Suppose Marci wants to investigate how satisfied advertisers are with yearbook ads. Describe a sampling strategy she could use to call 10 businesses.
  
  
  
  
  
  
  
  
  
  
7. Suppose Marci wants to investigate how likely a typical downtown business is to advertise in the upcoming yearbook. Describe a sampling strategy she could use to call 10 businesses.
  
  
  
  
  
  
  
  
  
  
8. The principal of a nearby school, Megalopolis Middle School, decided to conduct a survey of the 1,107 enrolled students. She asked three teachers how many students they thought should be surveyed. One teacher said to survey 200 girls and 100 boys, the second said to randomly select and survey 50 students, and the third said to survey the first 100 students to enter the building one morning next week.
  - a. Explain which of the three samples will produce data that may best represent all the students at Megalopolis.
  
  
  
  
  
  
  
  
  
  
  - b. Explain why you feel that the other two samples would not be as representative of all the students as the one you chose in part a.

## Additional Practice *(continued)*

### Investigation 2

#### Samples and Populations

In a survey of the cafeteria food at a middle school, 50 students were asked to rate how well they liked the lunches on a scale of 1 to 10, with 1 being the lowest rating and 10 being the highest rating. The box plot below was made from the collected data.



9. What is the range of students' ratings in the sample?
  
10. What percent of the students in the sample rated the cafeteria food between 5.75 and 9?
  
11. Based on the sample data, how many of the 1,000 students at the school do you estimate would rate the cafeteria food 6 or higher? Explain your reasoning.
  
12. A rating of 8 to 10 indicates "highly satisfied" on the rating scale.
  - a. What percent of students in the sample are "highly satisfied" with the cafeteria food?
  
  - b. Estimate how many students at the middle school would give the cafeteria food a "highly satisfied" rating.

## Skill: Random Samples

### Investigation 2

#### Samples and Populations

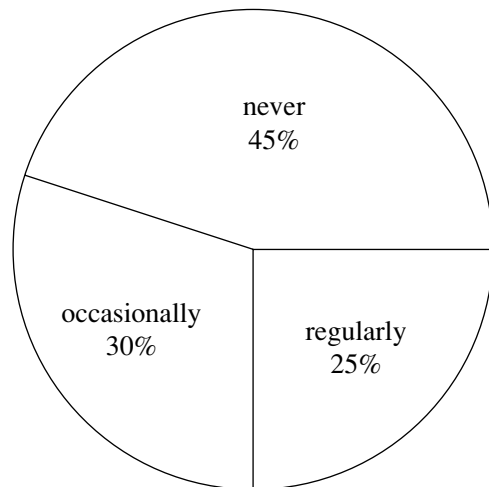
You want to survey students in your school about their exercise habits. Tell whether Exercises 1–2 are likely to give a random sample of the population.

Explain.

1. You select every tenth student on an alphabetical list of the students in your school. You survey the selected students in their first-period classes.
2. At lunchtime you stand by a vending machine. You survey every student who buys something from the vending machine.

In a mall, 2,146 shoppers (age 16 and older) were asked, “How often do you eat at a restaurant in the mall?” Here is how they responded.

3. What population does the sample represent?



4. How many people responded in each of the categories?

5. What is the sample size?

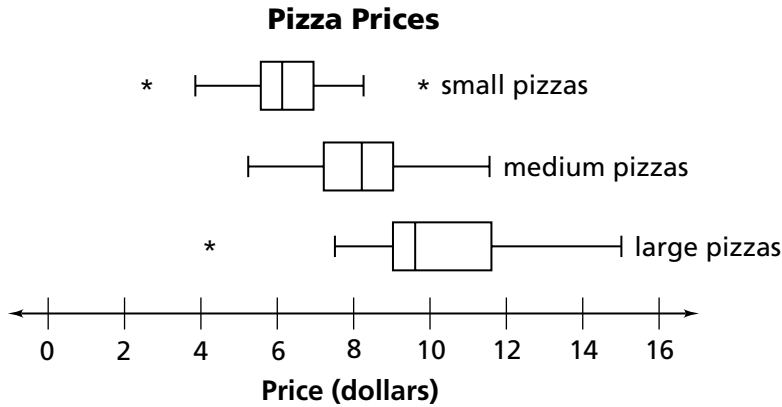
6. Can you tell if the sample is random?

# Additional Practice

## Investigation 3

### Samples and Populations

1. A group of students surveyed several pizza shops in two parts of the United States. They asked about prices and sizes of small, medium, and large cheese pizzas, and they made box plots from the data they collected.
  - a. These box plots show the prices for each size pizza, including outliers. Which size appears to be the least expensive? Explain your reasoning.



- b. One of the small pizzas had a diameter of 8 inches and a price of \$3.87. Its price per square inch is \$0.077. How was this calculated?

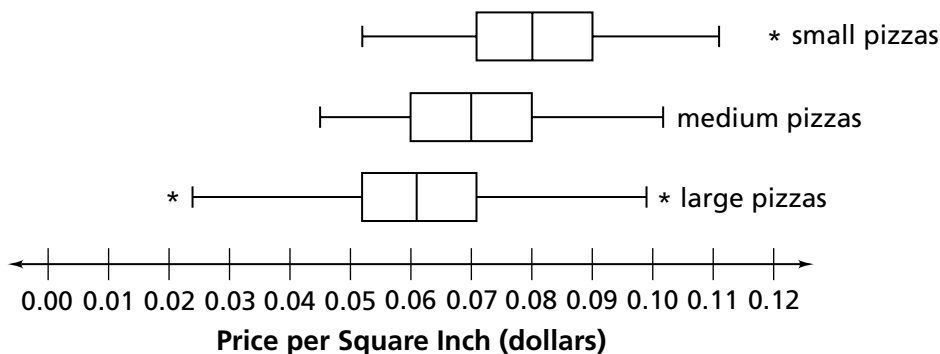
**Additional Practice** *(continued)*

**Investigation 3**

**Samples and Populations**

- c. These box plots show the price per square inch of pizza for each size. Which size appears to be the best buy? Explain.

**Pizza Prices per Square Inch**



- d. Consider your responses to parts (a) and (c). Which set of box plots better reflects the actual price of a pizza? Explain.

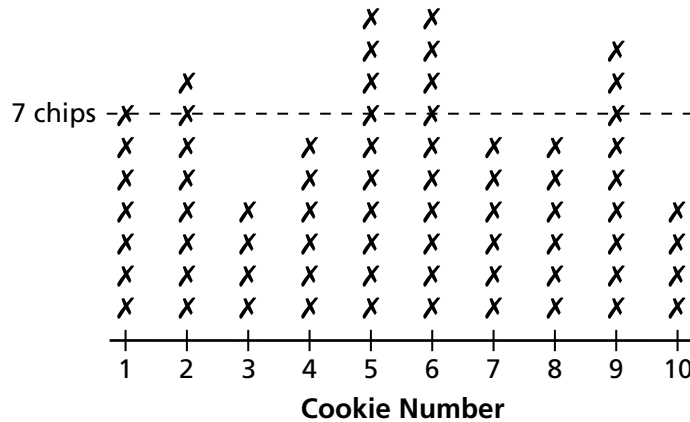
## Additional Practice *(continued)*

### Investigation 3

#### Samples and Populations

2. Suppose Jeff and Ted decide to change their advertising slogan to “Seven giant chips in every cookie!” They mix 70 chips into a batch of dough and make 10 cookies from the dough. When they remove the cookies from the oven and inspect them, they count the number of chips in each cookie. Their results are shown below. Notice that only 5 of the 10 cookies contained 7 chips or more.

**Chips in a Batch of 10 Cookies**



- a. Conduct a simulation to determine the number of chips needed to be added to a batch of 10 cookies until each cookie has at least 7 chips. Carry out the simulation five times so that you have five data values for the number of chips needed.
- b. What is the minimum number of chips Jeff and Ted should use to be confident that each cookie will have at least 7 chips? Support your answer with statistics and graphs.

**Additional Practice** *(continued)*

**Investigation 3**

**Samples and Populations**

3. After testing many samples, an egg shipper determined that approximately 3 in every 100 cartons of eggs will contain at least one cracked egg. The company ships 200,000 cartons of eggs every month. Estimate how many cartons of eggs each month will contain at least one cracked egg.
4. From a shipment of 500 batteries, a sample of 25 was selected at random and tested. If 2 batteries in the sample were found to be dead, how many dead batteries would be expected in the entire shipment?





**Additional Practice****Investigation 4****Samples and Populations**

Use the tables below, which display the results of a study of 47 half-ounce boxes of two brands of raisins.

**Vine Hill Raisins**

Number in Box	Mass (grams)	Number in Box	Mass (grams)
29	14.78	38	16.3
35	16.59	38	16.85
35	16.01	38	17.33
35	16.55	38	17.57
36	16.99	40	16.2
38	16.34	40	16.78
38	16.3	40	17.35
39	17.83	41	17.43
39	16.66	41	16.64
39	18.36	41	16.62
39	16.93	31	14.7
40	16.25	34	16.04
40	17.92	35	16.81
40	17.12	36	16.86
40	17.37	36	16.75
42	16.95	36	17.18
42	17.45	36	15.77
44	18.48	36	16.28
35	15.64	37	16.25
36	16.88	37	17.42
36	16.36	37	16.25
36	16.3	37	15.63
37	17.25	37	17.74
37	15.61		

**Suntime Raisins**

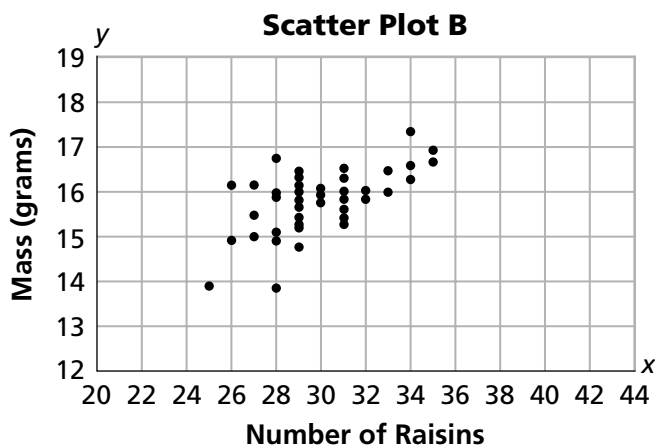
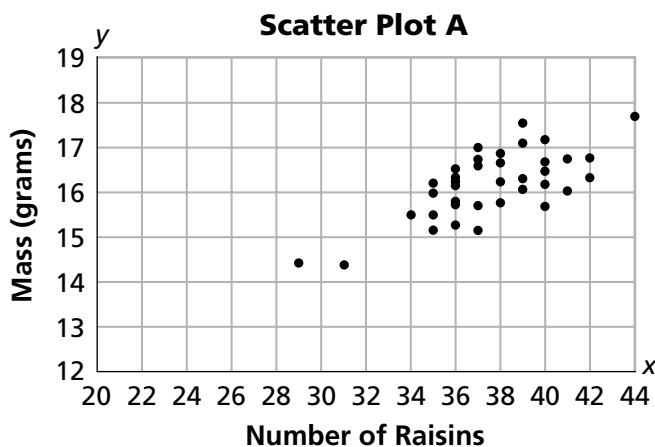
Number in Box	Mass (grams)	Number in Box	Mass (grams)
25	14.15	31	16.13
26	16.74	31	16.6
27	15.42	32	16.6
27	16.74	33	16.55
27	15.98	33	17.11
28	17.43	34	16.88
28	16.44	34	18.1
28	16.55	35	17.63
28	15.55	35	17.32
28	15.33	26	15.34
29	16.75	28	14.11
29	16.19	29	16.94
29	16.36	29	15.16
29	17.1	29	15.75
29	16.58	29	15.65
30	16.36	30	16.5
30	16.29	31	15.83
31	15.9	31	17.17
29	16.18	32	16.6
29	15.91	32	16.59
30	16.66	32	16.38
31	15.73	33	17.11
31	16.38	34	17.24
31	16.92		

## Additional Practice *(continued)*

### Investigation 4

#### Samples and Populations

1. The two scatter plots below show the data from the tables. Which scatter plot shows the data for Suntime raisins? Which shows the data for Vine Hill raisins? Explain your reasoning.



2. Is this statement true or false: “Vine Hill raisins typically have more raisins in a box than do Suntime raisins.” Explain your reasoning using the two graphs.
3. Is there a relationship between the number of raisins in a box and the mass in grams? Explain.

**Additional Practice** *(continued)***Investigation 4****Samples and Populations**

For Exercises 4–6, use the data below.

**Chicken Sandwiches From Restaurant Chains**

Size (oz)	Calories	Fat (g)	Carbohydrates (g)
8	360	7	44
10	370	8	53
8	380	4	57
9	400	5	57
8	400	16	37
8	470	20	51
8	470	20	46
10	500	24	52
8	510	19	57
10	540	30	42
9	550	23	55
10	550	30	46
10	570	25	48
12	580	19	58
11	640	29	61
13	660	29	56
12	720	30	65
13	740	30	78
12	910	40	86
15	950	56	76

4. a. Make a scatterplot for size vs. calories.

**Additional Practice** *(continued)*

**Investigation 4**

**Samples and Populations**

- b. Describe any relationship you see between the size of the sandwich and calories. Explain your reasoning.
5. a. Make a scatterplot for size of sandwich vs. fat.
- b. What is the relationship between sandwich size and fat content? Explain.
6. a. Make a scatterplot for size vs. carbohydrates.
- b. What is the relationship between size of a sandwich and the carbohydrates? Explain.

**Additional Practice** *(continued)*

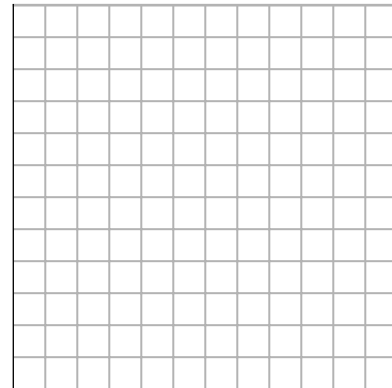
**Investigation 4**

**Samples and Populations**

7. a. Make a scatterplot of the data below for price vs. weight.

**Bike Comparisons**

Type of Bike	Price	Weight (lb)
Front Suspension Mountain Bike	\$450	29.5
Front Suspension Mountain Bike	\$440	29.5
Front Suspension Mountain Bike	\$440	30.5
Front Suspension Mountain Bike	\$450	31.5
Front Suspension Mountain Bike	\$440	31.0
Front Suspension Mountain Bike	\$500	30.5
Front Suspension Mountain Bike	\$500	31.5
Front Suspension Mountain Bike	\$400	32.0
Comfort Bike	\$300	33.0
Comfort Bike	\$300	32.5
Comfort Bike	\$300	35.5
Comfort Bike	\$300	32.0
Comfort Bike	\$280	31.5
Comfort Bike	\$290	33.0
Comfort Bike	\$285	33.5



b. Is there a strong or weak relationship between the weight of a bike and the price for the bike? Explain your reasoning.

c. If you pay more, are likely to get a heavier or lighter bike?

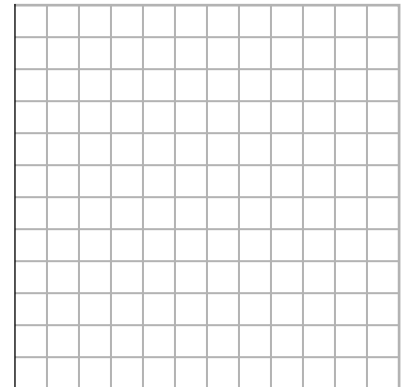
# Skill: Scatter Plots

## Investigation 4

### Samples and Populations

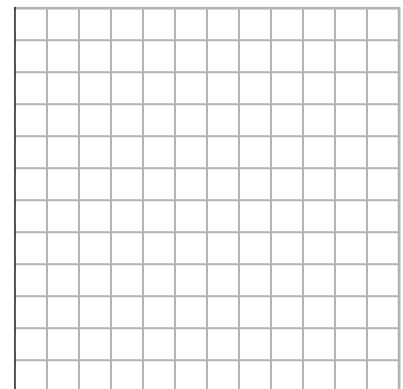
1. Make a scatter plot showing the number of homeowners on one axis and vacation homeowners on the other axis. If there is a trend, draw a trend line.

Residents of Maintown		
Year	Homeowners	Vacation Homeowners
1997-98	2,050	973
1996-97	1,987	967
1995-96	1,948	1,041
1994-95	1,897	1,043
1993-94	1,862	1,125
1992-93	1,832	1,126



2. Make a scatter plot for the data. If there is a trend, draw a trend line.

Arm Span vs. Height		
Person #	Arm Span	Height
1	156	162
2	157	160
3	159	162
4	160	155
5	161	160
6	161	162
7	162	170
8	165	166
9	170	170
10	170	167
11	173	185
12	173	176



**Skill: Scatter Plots** *(continued)*

**Investigation 4**

**Samples and Populations**

Decide whether the data in each scatter plot follow a linear pattern. If they do, find the equation of a trend line.

