

CHAPTER 5 • STUDY GUIDE AND ASSESSMENT

SKILLS AND CONCEPTS

OBJECTIVES AND EXAMPLES

Lesson 5-1 Identify angles that are coterminal with a given angle.

If a 585° angle is in standard position, determine a coterminal angle that is between 0° and 360° . State the quadrant in which the terminal side lies.

First, determine the number of complete rotations (k) by dividing 585 by 360.

$$\frac{585}{360} = 1.625$$

Use $\alpha + 360k^\circ$ to find the value of α .

$$\alpha + 360(1)^\circ = 585^\circ$$

$$\alpha = 225^\circ$$

The coterminal angle (α) is 225° . Its terminal side lies in the third quadrant.

REVIEW EXERCISES

Change each measure to degrees, minutes, and seconds.

11. 57.15°

12. -17.125°

If each angle is in standard position, determine a coterminal angle that is between 0° and 360° . State the quadrant in which the terminal side lies.

13. 860°

14. 1146°

15. -156°

16. 998°

17. -300°

18. 1072°

19. 654°

20. -832°

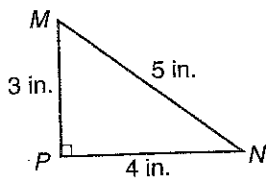
Find the measure of the reference angle for each angle.

21. -284°

22. 592°

Lesson 5-2 Find the values of trigonometric ratios for acute angles of right triangles.

Find the values of the six trigonometric ratios for $\angle M$.



$$\sin M = \frac{4}{5}$$

$$\sin M = \frac{\text{side opposite}}{\text{hypotenuse}}$$

$$\cos M = \frac{3}{5}$$

$$\cos M = \frac{\text{side adjacent}}{\text{hypotenuse}}$$

$$\tan M = \frac{4}{3}$$

$$\tan M = \frac{\text{side opposite}}{\text{side adjacent}}$$

$$\csc M = \frac{5}{4}$$

$$\csc M = \frac{\text{hypotenuse}}{\text{side opposite}}$$

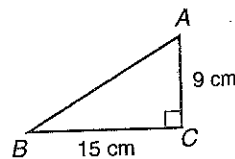
$$\sec M = \frac{5}{3}$$

$$\sec M = \frac{\text{hypotenuse}}{\text{side adjacent}}$$

$$\cot M = \frac{3}{4}$$

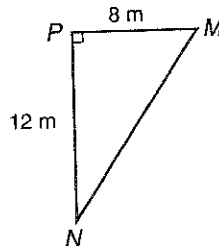
$$\cot M = \frac{\text{side adjacent}}{\text{side opposite}}$$

23. Find the values of the sine, cosine, and tangent for $\angle A$.

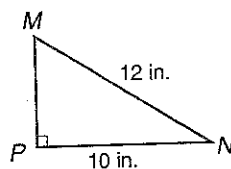


Find the values of the six trigonometric functions for each $\angle M$.

24.



25.



26. If $\sec \theta = \frac{7}{5}$, find $\cos \theta$.

CHAPTER 5 • STUDY GUIDE AND ASSESSMENT

OBJECTIVES AND EXAMPLES

Lesson 5-6 Find the area of a triangle if the measures of two sides and the included angle or the measures of two angles and a side are given.

Find the area of $\triangle ABC$ if $a = 6$, $b = 4$, and $C = 54^\circ$.

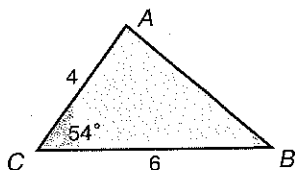
Draw a diagram.

$$K = \frac{1}{2}ab \sin C$$

$$K = \frac{1}{2}(6)(4) \sin 54^\circ$$

$$K \approx 9.708203932$$

The area of $\triangle ABC$ is about 9.7 square units.



REVIEW EXERCISES

Solve each triangle. Round to the nearest tenth.

45. $B = 70^\circ$, $C = 58^\circ$, $a = 84$

46. $c = 8$, $C = 49^\circ$, $B = 57^\circ$

Find the area of each triangle. Round to the nearest tenth.

47. $A = 20^\circ$, $a = 19$, $C = 64^\circ$

48. $b = 24$, $A = 56^\circ$, $B = 78^\circ$

49. $b = 65.5$, $c = 89.4$, $A = 58.2^\circ$

50. $B = 22.6^\circ$, $a = 18.4$, $c = 6.7$

Lesson 5-7 Solve triangles by using the Law of Sines.

In $\triangle ABC$, if $A = 51^\circ$, $C = 32^\circ$, and $c = 18$, find a .

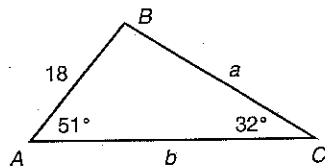
Draw a diagram.

$$\frac{a}{\sin A} = \frac{c}{\sin C}$$

$$\frac{a}{\sin 51^\circ} = \frac{18}{\sin 32^\circ}$$

$$a = \frac{(\sin 51^\circ)18}{\sin 32^\circ}$$

$$a \approx 26.4$$



Find all solutions for each triangle. If no solutions exist, write *none*. Round to the nearest tenth.

51. $A = 38.7^\circ$, $a = 172$, $c = 203$

52. $a = 12$, $b = 19$, $A = 57^\circ$

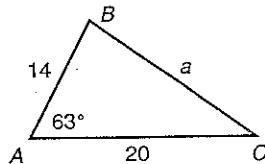
53. $A = 29^\circ$, $a = 12$, $c = 15$

54. $A = 45^\circ$, $a = 83$, $b = 79$

Lesson 5-8 Solve triangles by using the Law of Cosines.

In $\triangle ABC$, if $A = 63^\circ$, $b = 20$, and $c = 14$, find a .

Draw a diagram.



$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$a^2 = 20^2 + 14^2 - 2(20)(14) \cos 63^\circ$$

$$a^2 \approx 341.77$$

$$a \approx 18.5$$

Solve each triangle. Round to the nearest tenth.

55. $A = 51^\circ$, $b = 40$, $c = 45$

56. $B = 19^\circ$, $a = 51$, $c = 61$

57. $a = 11$, $b = 13$, $c = 20$

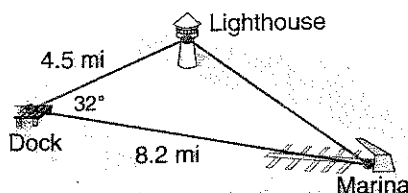
58. $B = 24^\circ$, $a = 42$, $c = 6.5$

APPLICATIONS AND PROBLEM SOLVING

59. Camping Haloke and his friends are camping in a tent. Each side of the tent forms a right angle with the ground. The tops of two ropes are attached to each side of the tent 8 feet above the ground. The other ends of the two ropes are attached to stakes on the ground. (Lesson 5-4)

- a. If the rope is 12 feet long, what angle does it make with the level ground?
- b. What is the distance between the bottom of the tent and each stake?

60. Navigation Hugo is taking a boat tour of a lake. The route he takes is shown on the map below. (Lesson 5-8)



- a. How far is it from the lighthouse to the marina?
- b. What is the angle between the route from the dock to the lighthouse and the route from the lighthouse to the marina?

ALTERNATIVE ASSESSMENT

OPEN-ENDED ASSESSMENT

1. A triangle has an area of 125 square centimeters and an angle that measures 35° . What are possible lengths of two sides of the triangle?
2.
 - a. Give the lengths of two sides and a nonincluded angle so that no triangle exists. Explain why no triangle exists for the measures you give.
 - b. Can you change the length of one of the sides you gave in part a so that two triangles exist? Explain.

PORTFOLIO

Explain how you can find the area of a triangle when you know the length of all three sides of the triangle.

Additional Assessment See p. A60 for Chapter 5 practice test.



Unit 2 *inter*NET Project

THE CYBERCLASSROOM

Does anybody out there know anything about trigonometry?

- Search the Internet to find at least three web sites that offer lessons on trigonometry. Some possible sites are actual mathematics courses offered on the Internet or webpages designed by teachers.
- Compare the Internet lessons with the lessons from this chapter. Note any similarities or differences.
- Select one topic from Chapter 5. Combine the information from your textbook and the lessons you found on the Internet. Write a summary of this topic using all the information you have gathered.