

**Formulas:**

Descriptive Statistics	Descriptive Parameters
mean of a sample $\bar{x} = \frac{\sum x}{n}$	mean of a population $\mu = \frac{\sum x}{N}$
proportion of a sample $\hat{p} = \frac{\text{successes}}{\text{events}}$	proportion of a population $\theta = \frac{\text{successes}}{\text{events}}$
standard deviation of a sample $S_x = \sqrt{\frac{\sum (x - \bar{x})^2}{n - 1}}$	standard deviation of a population $\sigma = \sqrt{\frac{\sum (x - \mu)^2}{n}}$
standard deviation of a sample proportion $\sigma_{\hat{p}} = \sqrt{\frac{\hat{p}(1 - \hat{p})}{n}}$	standard deviation of a population proportion $\sigma_{\theta} = \sqrt{\frac{\theta(1 - \theta)}{n}}$
standard deviation of sample means $\sigma_{\bar{x}} = \frac{S_x}{\sqrt{n}}$	standard deviation of sample means $\sigma_{\mu} = \frac{\sigma}{\sqrt{n}}$

**Probability:**

$$P(X > a) = 1 - P(X < a)$$

$$P(a < X < b) = P(X < b) - P(X < a)$$

**Z Scores** In a generalized form

standardized test statistic = ( statistic - parameter ) / ( standard deviation of statistic )

Some examples of standardized test statistic ( z-scores ):

$$Z = \frac{x - \mu}{\sigma} \quad Z = \frac{x - \bar{x}}{S_x}$$

### Formulas for Confidence Intervals:

<p>Confidence Interval for Population Proportion</p> $\hat{p} \pm Z^* \sqrt{\frac{\hat{p}(1 - \hat{p})}{n}}$	<p>Constraints ( Technical Conditions that must be met ):</p> <ol style="list-style-type: none"> <li>1. Data must be from a Simple Random Sample <math>n \times \hat{p} \geq 10</math></li> <li>2. <math>n(1 - \hat{p}) \geq 10</math></li> </ol>
<p>Confidence Interval for Population Means ( large sample )</p> $\bar{x} \pm Z^* \left( \frac{Sx}{\sqrt{n}} \right)$	<p>Constraints ( Technical Conditions that must be met ):</p> <ol style="list-style-type: none"> <li>1. Data must be from a Simple Random Sample</li> <li>2. Population normally distributed and n is at least 30 OR n is at least 50.</li> </ol>
<p>Confidence Interval for Population Means ( small sample )</p> $\bar{x} \pm t^* \left( \frac{Sx}{\sqrt{n}} \right)$	<p>Constraints ( Technical Conditions that must be met ):</p> <ol style="list-style-type: none"> <li>1. Data must be from a Simple Random Sample</li> <li>2. Population normally distributed or <math>n \geq 30</math></li> <li>3. <math>df = n - 1</math></li> </ol>

### Formulas for Tests of Significance:

<p>Large Sample Test for a Proportion</p> <p><math>H_0: \theta = \_ \_ \_</math></p> $z = \frac{\hat{p} - \theta}{\sigma_{\theta}}$	<p>Constraints ( Technical Conditions that must be met ):</p> <ol style="list-style-type: none"> <li>1. Data must be from a Simple Random Sample <math>n \times \theta \geq 10</math></li> <li>2. <math>n(1 - \theta) \geq 10</math></li> </ol>
<p>Sample Test for a Mean</p> <p><math>H_0: \mu = \_ \_ \_</math></p> $t = \frac{\bar{x} - \mu}{\sigma_{\mu}}$	<p>Constraints ( Technical Conditions that must be met ):</p> <ol style="list-style-type: none"> <li>1. Data must be from a Simple Random Sample</li> <li>2. Population normally distributed and n is at least 30 OR n is at least 50.</li> <li>3. <math>df = n - 1</math></li> </ol>

<p>Large Sample Test for Difference of Proportions  <i>Ho: <math>\theta_1 = \theta_2</math></i></p> $z = \frac{\hat{p}_1 - \hat{p}_2}{\sqrt{\frac{\hat{p}(1-\hat{p})}{n_1} + \frac{\hat{p}(1-\hat{p})}{n_2}}}$ <p>where <math>\hat{p}_1 = \frac{x_1}{n_1}</math> and <math>\hat{p}_2 = \frac{x_2}{n_2}</math> and</p> $\hat{p} = \frac{x_1 + x_2}{n_1 + n_2}$	<p>Constraints  ( Technical Conditions that must be met ):</p> <ol style="list-style-type: none"> <li>1. The two samples are independently selected simple random samples from the populations of interest.</li> <li>2. That <math>n_1\hat{p} \geq 5</math> and <math>n_1(1 - \hat{p}) \geq 5</math> and <math>n_2\hat{p} \geq 5</math> and <math>n_2(1 - \hat{p}) \geq 5</math></li> <li>3. <math>df = n_1-1</math> or <math>n_2-1</math> whichever one is smaller</li> </ol>
<p>Large Sample Test for a Difference of Population Means  <i>Ho: <math>\mu_1 = \mu_2</math></i></p> $t = \frac{\bar{x}_1 - \bar{x}_2}{\sqrt{\frac{Sx_1^2}{n_1} + \frac{Sx_2^2}{n_2}}}$	<p>Constraints  ( Technical Conditions that must be met ):</p> <ol style="list-style-type: none"> <li>1. The two samples are independently selected simple random samples from the populations of interest.</li> <li>2. Either that both populations are large ( 30 or larger ) or that both populations are normally distributed.</li> <li>3. <math>df = n_1-1</math> or <math>n_2-1</math> , whichever one is smaller</li> </ol>
<p>Chi-Square Test - Goodness of Fit</p> $\chi^2 = \sum \frac{(Observed - Expected)^2}{Expected}$ <p><math>df = n - 1</math></p>	<p>Constraints  ( Technical Conditions that must be met ):</p> <ol style="list-style-type: none"> <li>1. The observations are a simple random sample from the population of interest.</li> <li>2. All expected values are five or larger.</li> </ol>
<p>Chi-Square Test - Independence</p> $\chi^2 = \sum_{i,j} \frac{(Observed_{i,j} - Expected_{i,j})^2}{Expected_{i,j}}$ <p><math>df = (r - 1) (c - 1)</math></p>	<p>Constraints  ( Technical Conditions that must be met ):</p> <ol style="list-style-type: none"> <li>1. The observations are a simple random sample from the population of interest.</li> <li>2. All expected counts in the contingency table are five or larger.</li> </ol>
<p>F-Test Testing Two Population Standard Deviations.  <i>Ho: <math>\sigma_1 = \sigma_2</math></i></p> $F = \frac{Sx_1^2}{Sx_2^2}$ <p><math>df = n_1-1, n_2 - 1</math></p>	<p>Constraints  ( Technical Conditions that must be met ):</p> <ol style="list-style-type: none"> <li>1. The observations are from simple random samples from the population of interest.</li> <li>2. The sample data are independent.</li> <li>3. The populations are normally distributed.</li> <li>4. Place the sample with the larger standard deviation in the numerator.</li> </ol>