

1. Solve

(a) $\frac{1}{2}(x-3) \leq x+6$ or $4x-9 \leq \frac{1}{3}(x+7)$.

(b) $x^2 - 4x - 77 \geq 0$.

(c) $\frac{4x-3}{x+6} \geq 2$.

(d) $|x-1| + |2x+4| = 10$.

(e) $|x^2 - 2x| \geq 3$.

(f) $|3|x-1| + 2| < 7$.

(g) $x^2 + 2|x-2| - 11 \leq 0$

2. Let α and β be the roots of the quadratic equation $x^2 - 2(k+1)x + 2(k-1) = 0$, where k is a real number.

(a) Prove that α and β are real and unequal.

(b) Express $(\alpha - 5)(\beta - 5)$ in terms of k .

(c) (i) If $\alpha < 5 < \beta$, show that $k > \frac{13}{8}$.

(ii) If in addition that $\frac{1}{\alpha} + \frac{1}{\beta} > 2$, find the possible integral value of k .