

Integration

1. Antiderivatives or Reversing the process of *Differentiation*

$$C'(x) = 100 \xrightarrow{\text{Integration}} C(x) = 100x$$

$$C(x) = 100x + 500$$

$$C(x) = 100x + 1000$$

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$C(x) = 100x + k$ where k is a constant

2. Notation of Antiderivative

Antiderivatives of f :

$$\underbrace{\int}_{\text{Integral sign}} \underbrace{f'(x)}_{\text{integrand}} \underbrace{dx}_{\text{differential}} = f(x) + k$$

where k is constant of integration

3. Differentiation Rule

$$\frac{d}{dx}(ax) = a$$

$$\frac{d}{dx}(x^n) = nx^{n-1}$$

$$\frac{d}{dx}(\cos x) = -\sin x$$

$$\frac{d}{dx}(\sin x) = \cos x$$

$$\frac{d}{dx}(\tan x) = \sec^2 x$$

$$\frac{d}{dx}(\cot x) = -\csc^2 x$$

$$\frac{d}{dx}(\sec x) = \sec x \tan x$$

$$\frac{d}{dx}(\csc x) = -\csc x \cot x$$

Integration Rule

$$\int ax \, dx = \frac{ax^2}{2} + c$$

$$\int x^n \, dx = \frac{x^{n+1}}{n+1} + c$$

$$\int \sin x \, dx = -\cos x + c$$

$$\int \cos x \, dx = \sin x + c$$

$$\int \sec^2 x \, dx = \tan x + c$$

$$\int \csc^2 x \, dx = -\cot x + c$$

$$\int \sec x \tan x \, dx = \sec x + c$$

$$\int \csc x \cot x \, dx = -\csc x + c$$