# MAT 123: Introduction to Calculus <br> Exam 2, Fall 2007 

Tuesday, November 13, 8:30pm - 9:30pm
Directions: Do not turn this page over until you are directed to do so. Please fill in your name, Stony Brook ID number, and your recitation number on the lines below. Please then circle the recitation/evening lecture you belong to in the chart below. There are a total of 8 pages to this exam, not including the cover sheet. Be sure to have all of them. There are seven questions on this exam. Point values for each question are shown in brackets to the right of the question number. There are 100 possible points one can earn on this exam. You may not leave the exam room until 9:00pm at the earliest. You may not use a calculator or any other electronical device for this exam. You may not consult any outside resources, including fellow test-takers, notes, and textbooks. You will also not receive any information from the proctors regarding the wording of any of the exam questions.

Name: $\qquad$ ID\#: $\qquad$ Rec\#: $\qquad$

| R01 | Michael | M | 2:20p | R02 | Claudio | W | 11:45a | R03 | Deanna | Tu | 2:20p |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| R04 | James | Tu | $11: 20 \mathrm{a}$ | R05 | Michael | M | $11: 45 \mathrm{a}$ | R06 | Michael | F | $8: 30 \mathrm{a}$ |
| R07 | Deanna | M | $2: 20 \mathrm{p}$ | R08 | Paul | M | $12: 50 \mathrm{p}$ | R10 | Suren | Tu | $3: 50 \mathrm{p}$ |
| R11 | Jason | M | $11: 45 \mathrm{a}$ | R12 | Suren | Tu | $5: 20 \mathrm{p}$ | R13 | Dustin | W | $2: 20 \mathrm{p}$ |
| R14 | William | W | $6: 50 \mathrm{p}$ | R15 | Jason | Tu | $2: 20 \mathrm{p}$ | R16 | Sarah | Th | $2: 20 \mathrm{p}$ |
| R17 | Claudio | W | $10: 40 \mathrm{a}$ | R20 | Sarah | F | $12: 50 \mathrm{p}$ | R21 | Danielle | W | $10: 40 \mathrm{a}$ |
| R22 | Frank | Tu | $8: 20 \mathrm{a}$ | R23 | Katherine | M | $12: 50 \mathrm{p}$ | R24 | Danielle | W | $11: 45 \mathrm{a}$ |
| R25 | Daniel | M | $2: 20 \mathrm{p}$ | R26 | Deb | Th | $12: 50 \mathrm{p}$ | R27 | Raquel | Tu | $11: 20 \mathrm{a}$ |
| R30 | Adam | Th | $3: 50 \mathrm{p}$ | R31 | Adam | Th | $6: 50 \mathrm{p}$ | R33 | William | Th | $11: 20 \mathrm{a}$ |
| R34 | Krystle | Tu | 12:50p | R35 | Krystle | M | 10:40a | ELC90 | Peter | MW | $6: 50 \mathrm{p}$ |
| ELC91 | Nick | TuTh | $6: 50 \mathrm{p}$ |  |  |  |  |  |  |  |  |


| Question | 1 | 2 | 3 | 4 | 5 | 6 | 7 | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Possible Pts | 10 | 20 | 10 | 10 | 30 | 10 | 10 | 100 |
| Pts Awarded |  |  |  |  |  |  |  |  |

1. Match the following five equations:

$$
(2 \times 5=10 \text { points. })
$$

(a) $y=2^{-x}$
(b) $y=-2^{-x}$
(c) $y=\log (x)$
(d) $y=2^{x}$
(e) $y=-2^{x}$
with the following five graphs:

this graph corresponds to the equation.......
this graph corresponds to the equation.......
this graph corresponds to the equation. $\qquad$
this graph corresponds to the equation.......
this graph corresponds to the equation.......
2. Evaluate the following expression:

$$
(5 \times 4=20 \text { points })
$$

(a) $\log _{5} 25$
(b) $\ln \left(e^{5}\right)$
(c) $3^{\left(\log _{3} 7\right)}$
(d) $\log _{3}\left(3^{7}\right)$
3. Solve for $x$ :

$$
5^{2 x+1}=7^{x-1}
$$

4. Solve for $x$ :

$$
\log _{9}(x-5)+\log _{9}(x+3)=1
$$

5. Consider the following rational function

$$
f(x)=\frac{3 x-6}{x+1}
$$

(a) Find $x$ intercept of $f(x)$. [5 points]
(b) Find $y$ intercept of $f(x)$. [5 points]
(c) Find all horizontal asymptotes of $f(x)$ [5 points]
(d) Find all vertical asymptotes of $f(x)$
[5 points]
(e) Using all the information above, sketch the graph of $f(x)$.
[10 points]
6. An open box is made from a square piece of cardboard 24 inches on a side by cutting identical squares from the corners and turning up the sides. See the picture below:

(a) Express the volume of the box, $V$, as a function of the length of the side of the square cut from each corner, $x$.
[8 points]
(b) Find the domain of the function, $V(x)$, that you found in the previous step
[2 points]

$$
(2 \times 5=10 \text { points })
$$

7. If $\log _{a} b=2$ and $\log _{a} c=4$, find the numeric value of the following two expressions:
(a) $\log _{a}\left(b^{2} c^{3}\right)$
(b) $\log _{b} c$
