

信號經過處理後，測量重建(reconstructed)信號的好壞，計算原始信號能量對於誤差信號能量的比值，稱為訊雜比(Signal-to-Noise, SNR)。此處所探討的信號是指「影像」，SNR的計算方式如下：

X 為二維(2-Dimension)原始影像，高度為 N，寬度為 M

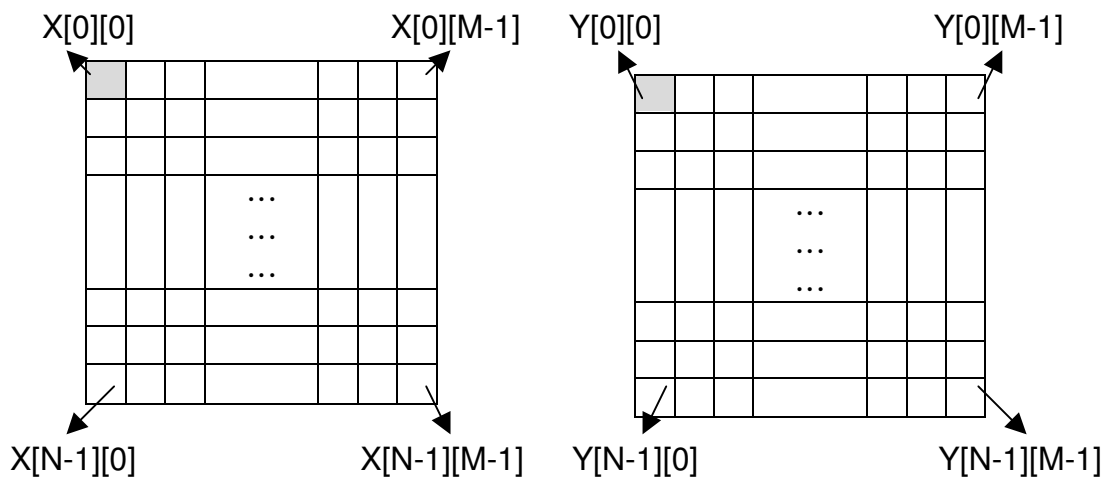
原始影像 pixel  $X[i][j]$  ,  $i = 0 \sim N-1$  ,  $j = 0 \sim M-1$

Y 為二維(2-Dimension)重建影像，高度為 N，寬度為 M

重建影像 pixel  $Y[i][j]$  ,  $i = 0 \sim N-1$  ,  $j = 0 \sim M-1$

d 為原始影像與重建影像的誤差

$d[i][j] = X[i][j] - Y[i][j]$  ,  $i = 0 \sim N-1$  ,  $j = 0 \sim M-1$



(1) signal-to-noise ratio(SNR)

$$SNR(db) = 10 \log_{10} \frac{\sigma_x^2}{\sigma_d^2}$$

Average squared value of the source

$$\sigma_x^2 = \frac{1}{NM} \sum_{i=0}^{N-1} \sum_{j=0}^{M-1} X[i][j]^2$$

Mean squared error(MSE)

$$\sigma_d^2 = \frac{1}{NM} \sum_{i=0}^{N-1} \sum_{j=0}^{M-1} d[i][j]^2 = \frac{1}{NM} \sum_{i=0}^{N-1} \sum_{j=0}^{M-1} (X[i][j] - Y[i][j])^2$$

(2) peak-signal-to-noise ratio(PSNR)

$$PSNR(db) = 10 \log_{10} \frac{X_{peak}^2}{\sigma_d^2}$$

$X_{peak}$  the peak value of the signal

```
double SNR( unsigned char *original,    // The original image
            unsigned char *result,     // The reconstructed image
            unsigned int width,        // Width
            unsigned int height)      // Height
{
    unsigned int i,j;
    double SumOfSquareSignal = 0.0, SumOfSquareError = 0.0,Error;

    for ( i = 0 ; i < height ; i++ ) {
        for ( j = 0 ; j < width ; j++ ) {
            SumOfSquareSignal += original[i*width+j]* original[i*width+j];
            Error = original[i*width+j] - result[i*width+j];
            SumOfSquareError += Error * Error;
        }
    }
    return 10*log10(SumOfSquareSignal / SumOfSquareError);
}
```

```
double PSNR( unsigned char *original,    // The original image
             unsigned char *result,     // The reconstructed image
             unsigned int width,        // Width
             unsigned int height)      // Height
{
    unsigned int i,j;
    double SumOfSquareError = 0.0,Error;

    for ( i = 0 ; i < height ; i++ ) {
        for ( j = 0 ; j < width ; j++ ) {
            Error = original[i*width+j] - result[i*width+j];
            SumOfSquareError += Error * Error;
        }
    }
    SumOfSquareError = SumOfSquareError/(double)(width * height);
    // Assume maximum 255
    return 10*log10( 255*255 / SumOfSquareError);
}
```